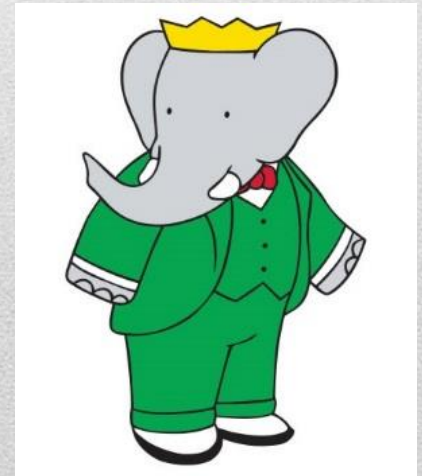


# Modeling exotic XYZP states

Alessandro Pilloni

BaBar collaboration meeting, SLAC, December 13<sup>th</sup>, 2016

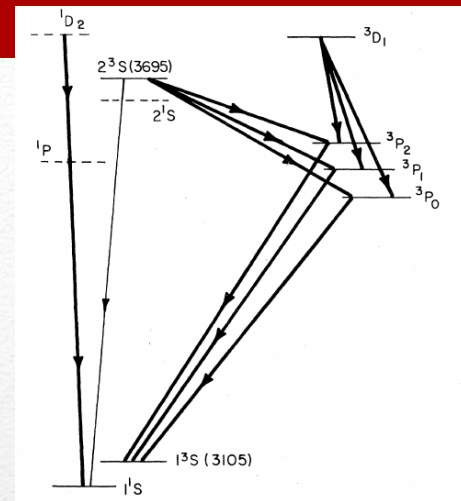
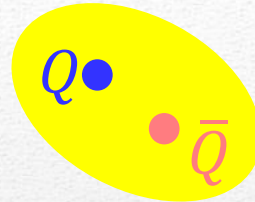
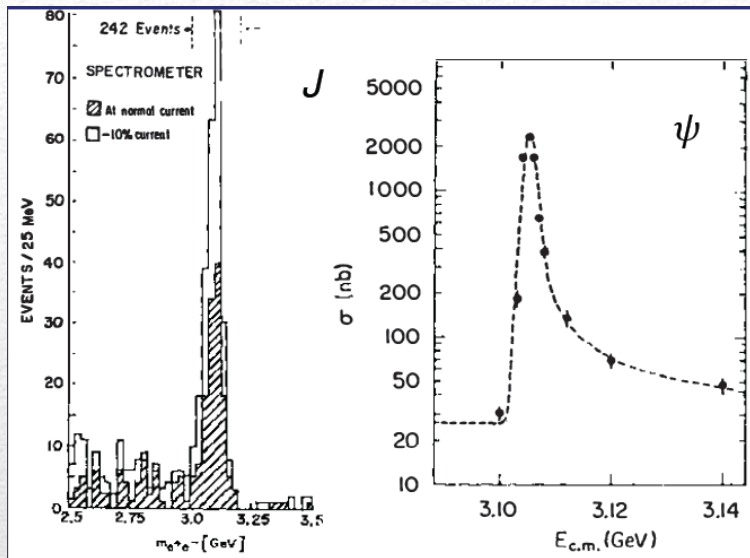


# Outline

- The exotic landscape: XYZP
- Compact tetraquarks
- Production of exotics
- Hybridized Tetraquarks
- Amplitude analysis @JPAC
- Conclusions



# Quarkonium orthodoxy



## Potential models

(meaningful when  $M_Q \rightarrow \infty$ )

$$V(r) = -\frac{C_F \alpha_s}{r} + \sigma r \quad (\text{Cornell potential})$$

Solve NR Schrödinger eq.  $\rightarrow$  spectrum

## Effective theories

(HQET, NRQCD, pNRQCD...)

Integrate out heavy DOF



(spectrum), decay & production rates

$$\alpha_s(M_Q) \sim 0.3$$

(perturbative regime)

OZI-rule, QCD multipole

Heavy quark spin flip suppressed by quark mass,  
approximate heavy quark spin symmetry (HQSS)

# Multiscale system

Systematically integrate out the heavy scale,

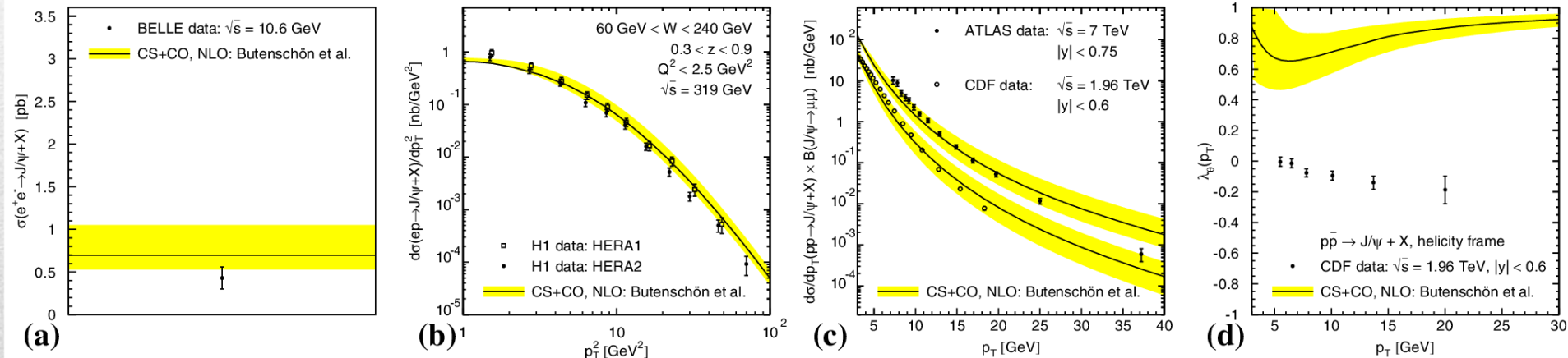
$$m_Q \gg \Lambda_{QCD}$$

$$m_Q \gg m_Q v \gg m_Q v^2$$

$$\text{Full QCD} \longrightarrow \text{NRQCD} \longrightarrow \text{pNRQCD}$$

$$m_b \sim 5 \text{ GeV}, m_c \sim 1.5 \text{ GeV}$$

$$v_b^2 \sim 0.1, v_c^2 \sim 0.3$$



Factorization (to be proved)  
of universal LDMEs

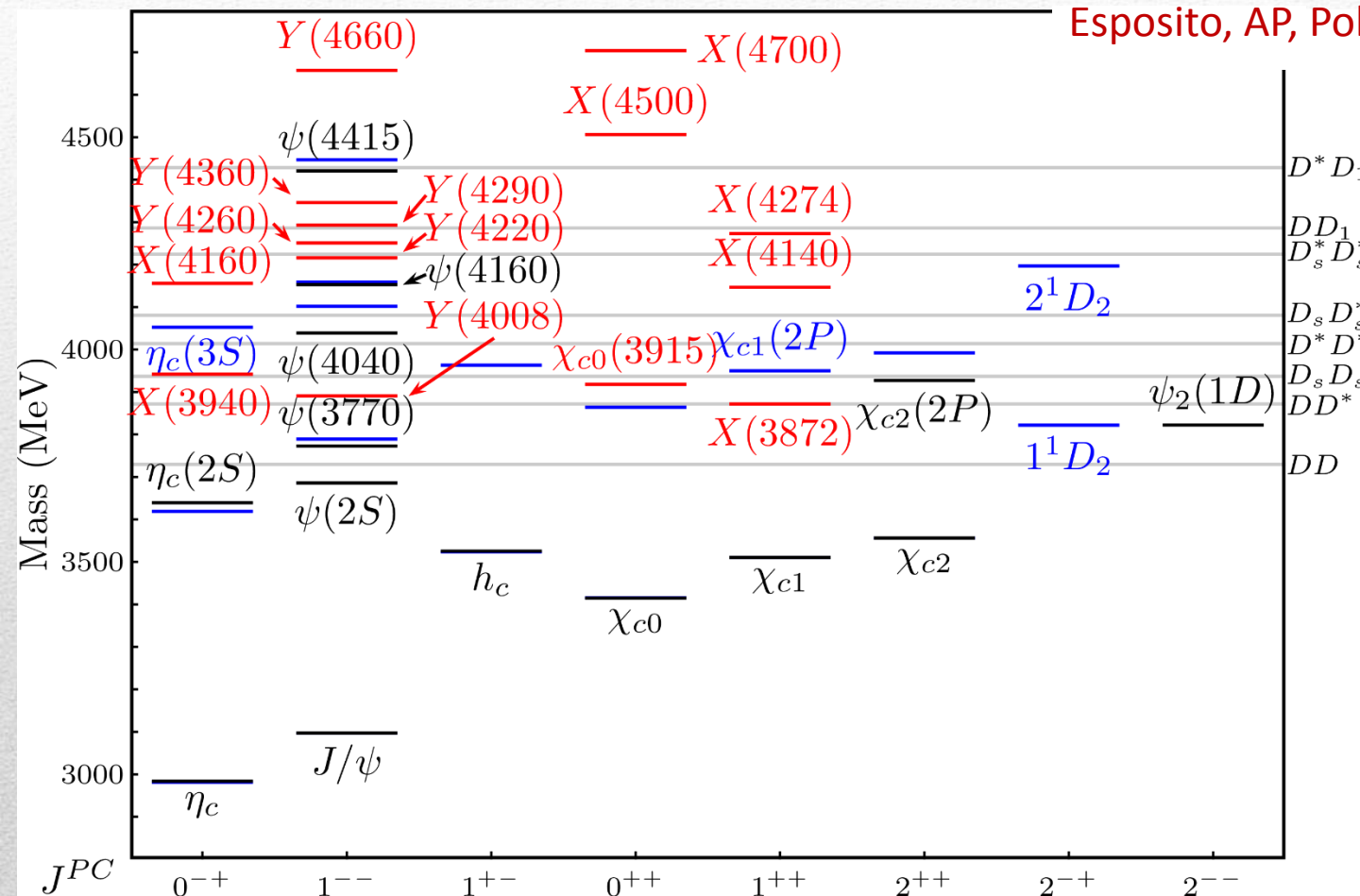
Good description of many production channels,  
some known puzzles (polarizations)



# Exotic landscape

Esposito, Guerrieri, Piccinini, AP, Polosa, JIMPA30, 1530002

Esposito, AP, Polosa, Phys.Rept. in press



A host of **unexpected resonances** have appeared

decaying mostly into charmonium + light

**Hardly reconciled** with usual charmonium interpretation

# Pentaquarks!

LHCb, PRL 115, 072001

LHCb, PRL 117, 082003

Two states seen in  $\Lambda_b \rightarrow (J/\psi p) K^-$ ,  
evidence in  $\Lambda_b \rightarrow (J/\psi p) \pi^-$

$$M_1 = 4380 \pm 8 \pm 29 \text{ MeV}$$

$$\Gamma_1 = 205 \pm 18 \pm 86 \text{ MeV}$$

$$M_2 = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$$

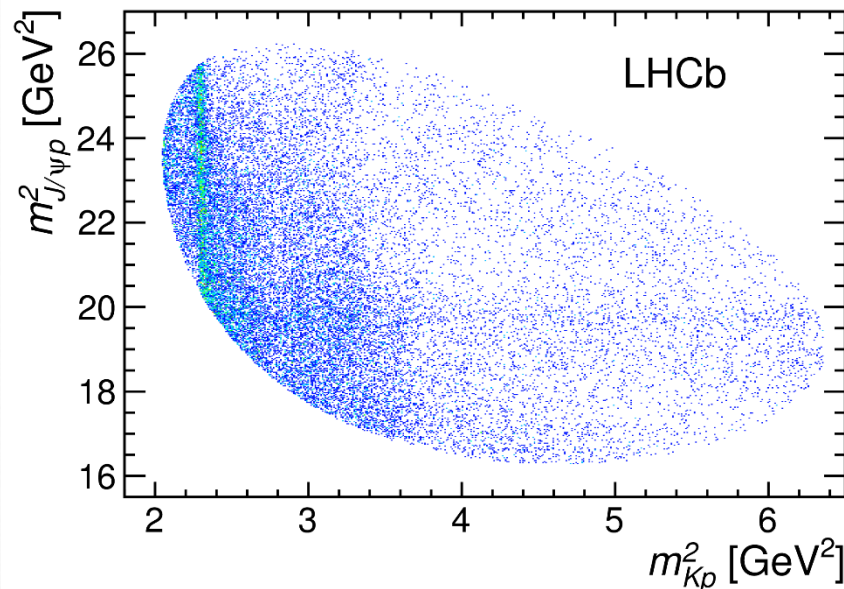
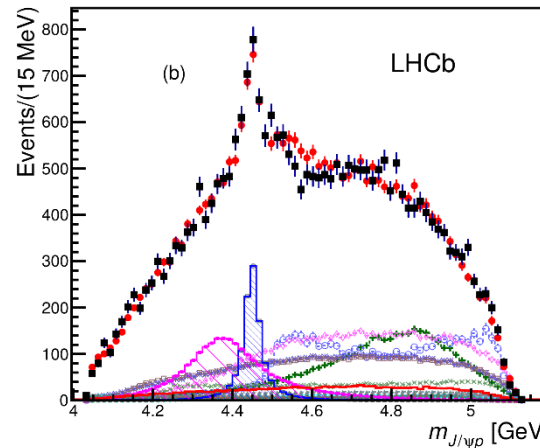
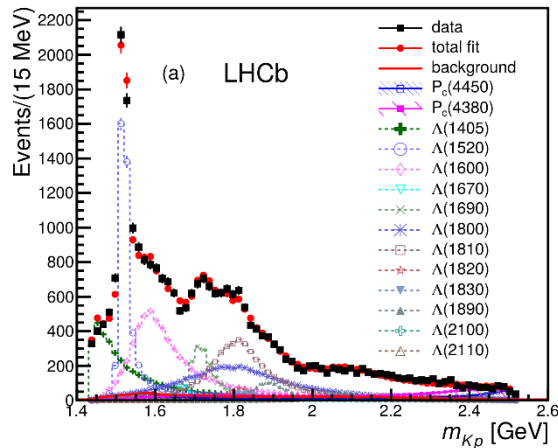
$$\Gamma_2 = 39 \pm 5 \pm 19 \text{ MeV}$$

Quantum numbers

$$J^P = \left( \frac{3}{2}^-, \frac{5}{2}^+ \right) \text{ or } \left( \frac{3}{2}^+, \frac{5}{2}^- \right) \text{ or } \left( \frac{5}{2}^+, \frac{3}{2}^- \right)$$

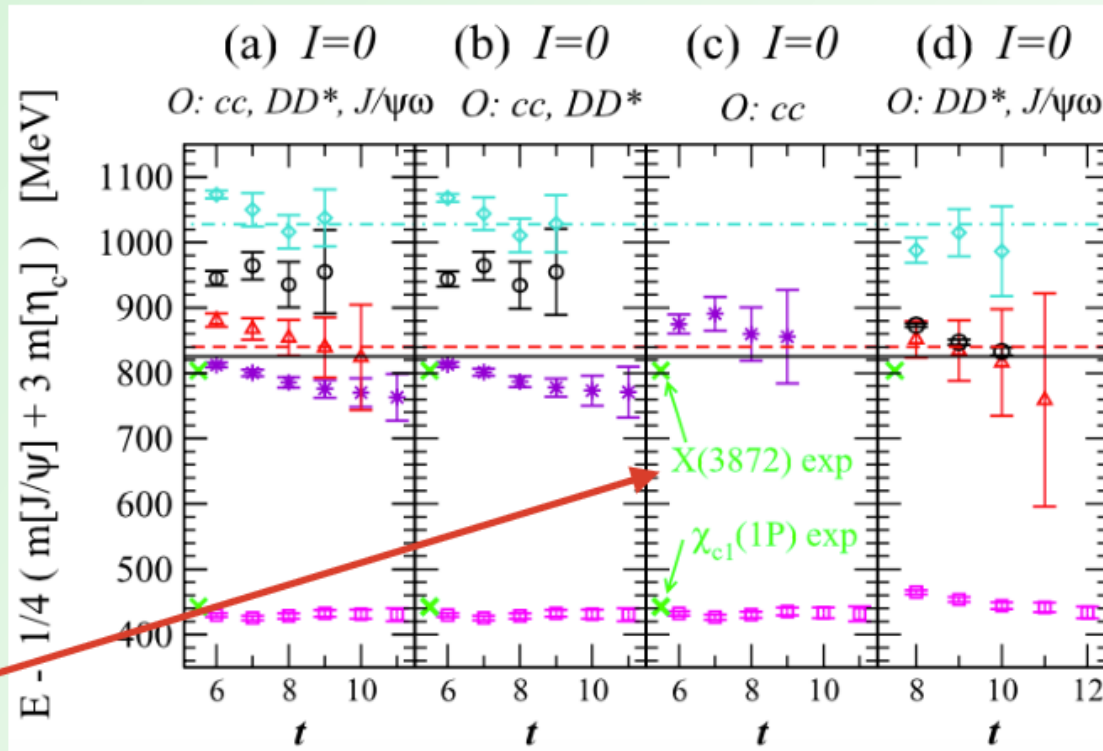
Opposite parities needed for the  
interference to correctly describe angular  
distributions, **low mass region**  
**contaminated by  $\Lambda^*$  (model dependence?)**

No obvious threshold nearby





# X(3872) on the lattice: spectrum



Status of other XYZ on the lattice is even less clear

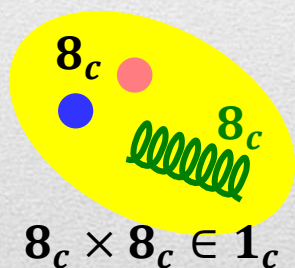
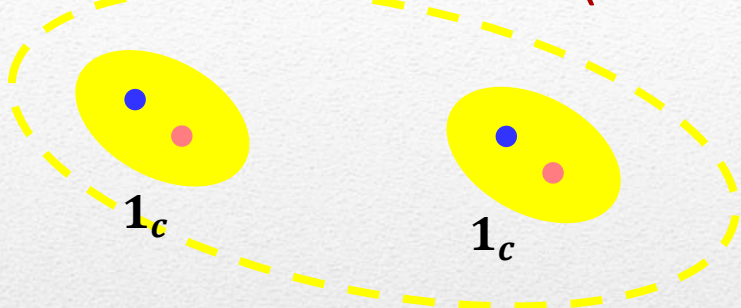
Where is the  $\chi_{c1}(2P)$  ?

$J^{PC} = 1^{++} \ I = 0$  channel

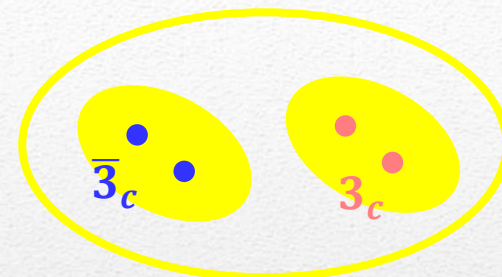
Prelovsek *et al.* PRL 111 (2013) 192001 arXiv: 1307.5172

# Proposed models

Molecule of hadrons (loosely bound)



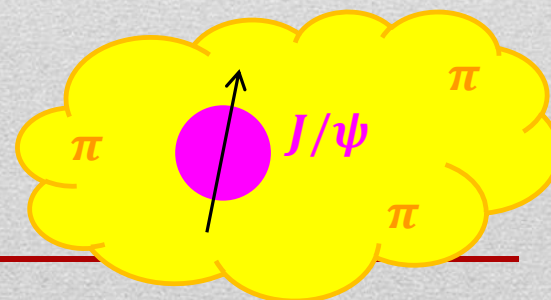
Glueball, Hybrids  
(with valence gluons),  
Born-Oppenheimer 4q



$$3_c \times \bar{3}_c \in 1_c$$

Diquark-antidiquark  
(tetraquark)

Hadrocharmonium  
(Van der Waals forces)



$$1_c \times 1_c \in 1_c$$

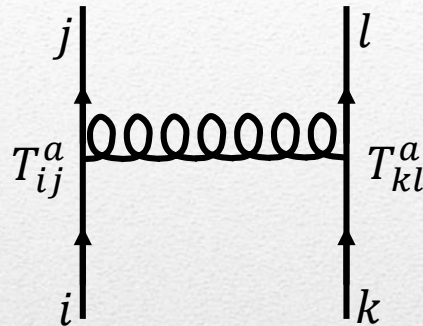
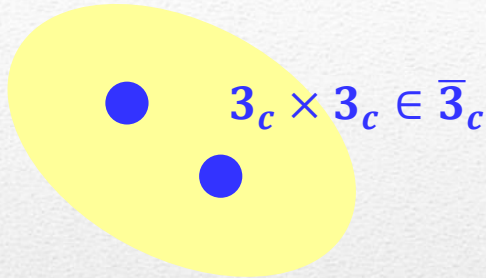
Cusp (kinematical effect)





# Diquarks

Attraction and repulsion in 1-gluon exchange approximation is given by



$$R = \frac{1}{2} (C_2(R_{12}) - C_2(R_1) - C_2(R_2))$$

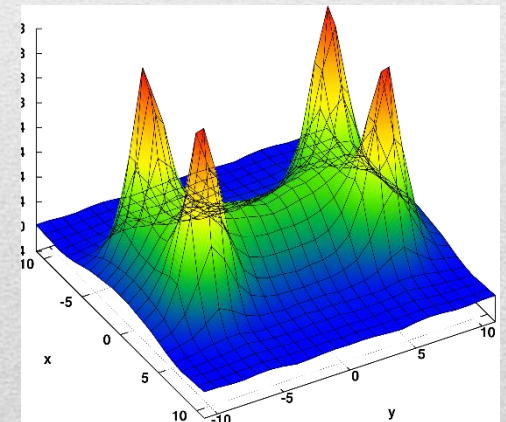
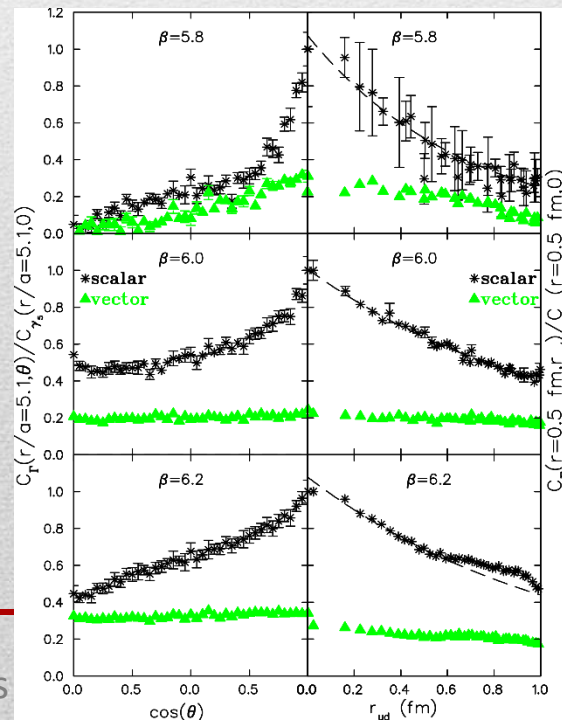
$$R_1 = -\frac{4}{3}, R_8 = +\frac{1}{6}$$

$$R_3 = -\frac{2}{3}, R_6 = +\frac{1}{3}$$

The singlet  $\mathbf{1}_c$  is attractive

A diquark in  $\bar{\mathbf{3}}_c$  is attractive

Evidence (?) of diquarks in LQCD,  
Alexandrou, de Forcrand, Lucini,  
PRL 97, 222002



H-shape with a 4 quark system  
Cardoso, Cardoso, Bicudo,  
PRD84, 054508

# Tetraquark

In a constituent (di)quark model, we can think of a **diquark-antidiquark compact state**

$$[cq]_{S=0}[\bar{c}\bar{q}]_{S=1} + h.c.$$

Maiani, Piccinini, Polosa, Riquer PRD71 014028

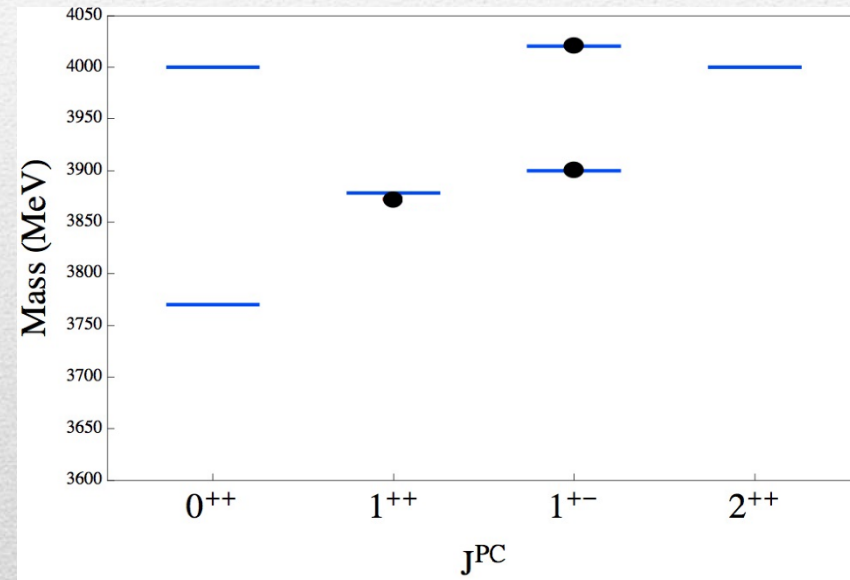
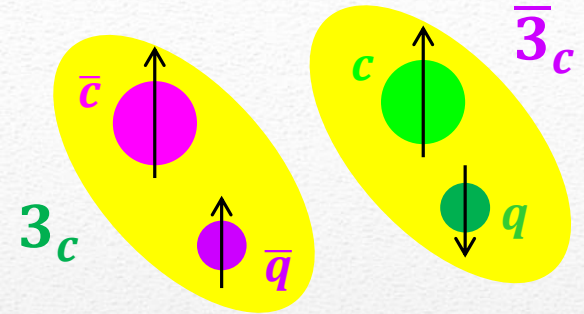
Faccini, Maiani, Piccinini, AP, Polosa, Riquer PRD87 111102

Maiani, Piccinini, Polosa, Riquer PRD89 114010

Spectrum according to **color-spin hamiltonian**  
(all the terms of the Breit-Fermi hamiltonian are absorbed into a constant diquark mass):

$$H = \sum_{dq} m_{dq} + 2 \sum_{i < j} \kappa_{ij} \vec{S}_i \cdot \vec{S}_j \frac{\lambda_i^a}{2} \frac{\lambda_j^a}{2}$$

Decay pattern mostly driven by **HQSS** ✓  
Fair understanding of existing spectrum ✓  
A full nonet for each level is expected ✗



New ansatz: the diquarks are compact objects  
spacially separated from each other,  
**only  $\kappa_{cq} \neq 0$**

Existing spectrum is fitted if  $\kappa_{cq} = 67$  MeV



# Tetraquark

Maiani, Piccinini, Polosa, Riquer PRD89 114010

$J^{PC}$	$cq \bar{c}\bar{q}$	$c\bar{c} q\bar{q}$	Resonance Assig.	Decays
$0^{++}$	$ 0, 0\rangle$	$1/2 0, 0\rangle + \sqrt{3}/2 1, 1\rangle_0$	$X_0(\sim 3770 \text{ MeV})$	$\eta_c, J/\psi + \text{light mesons}$
$0^{++}$	$ 1, 1\rangle_0$	$\sqrt{3}/2 0, 0\rangle - 1/2 1, 1\rangle_0$	$X'_0(\sim 4000 \text{ MeV})$	$\eta_c, J/\psi + \text{light mesons}$
$1^{++}$	$1/\sqrt{2}( 1, 0\rangle +  0, 1\rangle)$	$ 1, 1\rangle_1$	$X_1 = X(3872)$	$J/\psi + \rho/\omega, DD^*$
$1^{+-}$	$1/\sqrt{2}( 1, 0\rangle -  0, 1\rangle)$	$1/\sqrt{2}( 1, 0\rangle -  0, 1\rangle)$	$Z = Z(3900)$	$J/\psi + \pi, h_c/\eta_c + \pi/\rho$
$1^{+-}$	$ 1, 1\rangle_1$	$1/\sqrt{2}( 1, 0\rangle +  0, 1\rangle)$	$Z' = Z(4020)$	$J/\psi + \pi, h_c/\eta_c + \pi/\rho$
$2^{++}$	$ 1, 1\rangle_2$	$ 1, 1\rangle_2$	$X_2(\sim 4000 \text{ MeV})$	$J/\psi + \text{light mesons}$

$$\Delta H = \frac{B_c \vec{L}^2}{2} - 2a \vec{L} \cdot \vec{S}$$

$L = 1$	$P(S_{c\bar{c}} = 1) : P(S_{c\bar{c}} = 0)$	Assignment	Radiative Decay
$Y_1$	3:1	$Y(4008)$	$\gamma + X_0$
$Y_2$	1:0	$Y(4260)$	$\gamma + X$
$Y_3$	1:3	$Y(4290)/Y(4220)$	$\gamma + X'_0$
$Y_4$	1:0	$Y(4630)$	$\gamma + X_2$

actually observed  
BESIII PRL 112,  
092001

Radial excitations

$$Z(2S) = Z(4430)$$

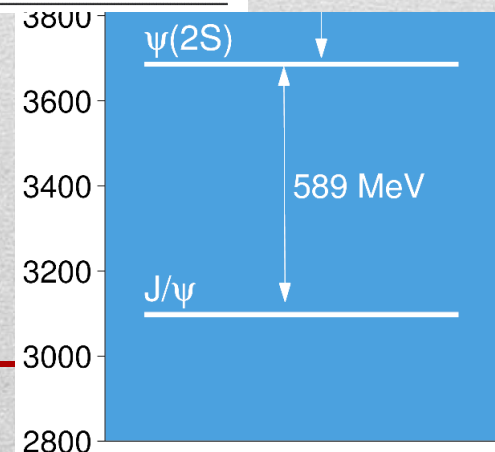
$$Y_1(2P) = Y(4360)$$

$$Y_2(2P) = Y(4660)$$

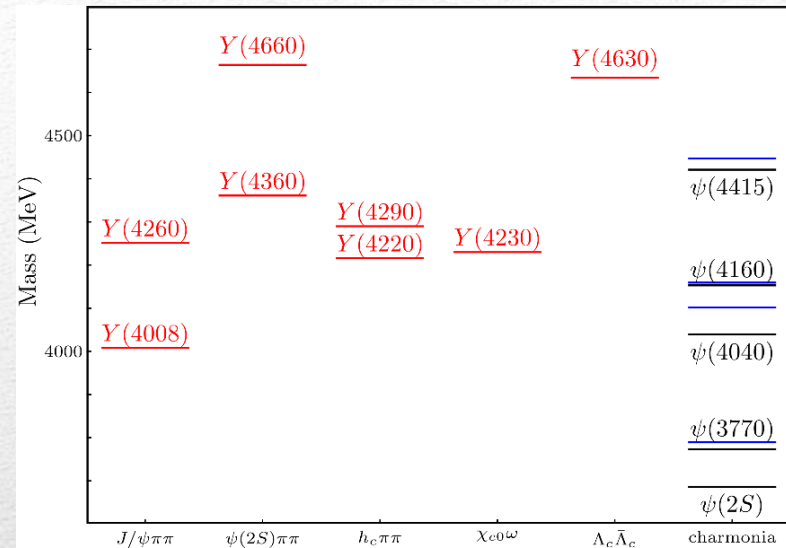
Decay in  $\psi(2S)$  preferably

$$M_{Z(4430)} - M_{Z_c} = 586^{+17}_{-26} \text{ MeV}$$

to compare with charmonium



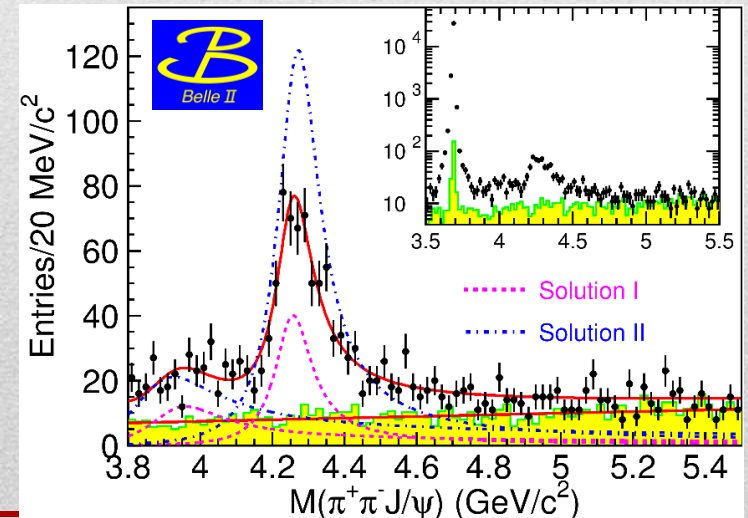
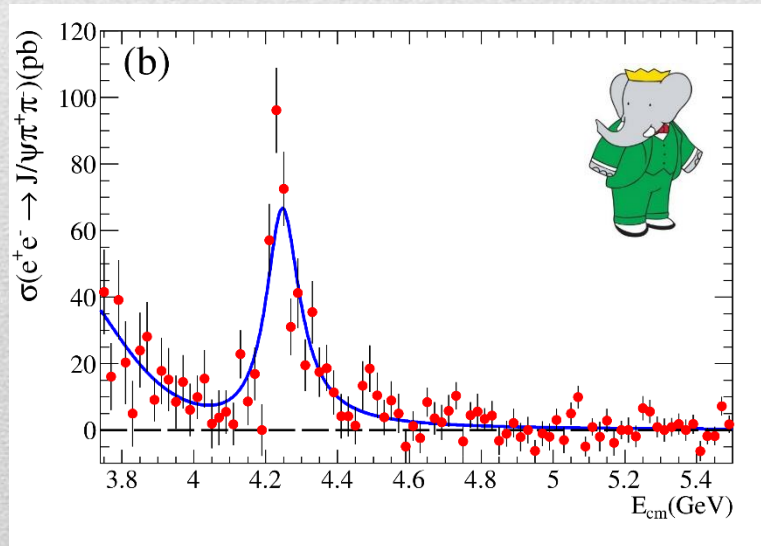
# Vector $Y$ states



Lots of unexpected  $J^{PC} = 1^{--}$  states found in ISR/direct production (and nowhere else!)

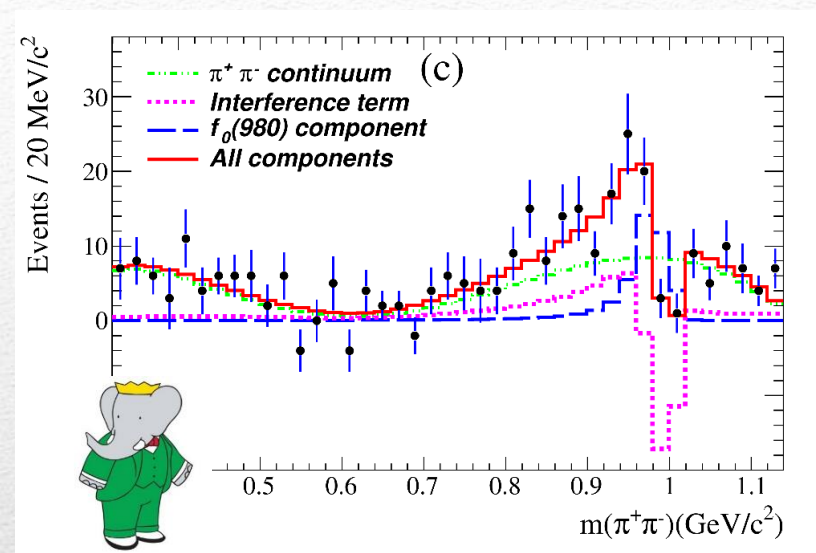
Seen in few final states, mostly  $J/\psi \pi \pi$  and  $\psi(2S) \pi \pi$

Not seen decaying into open charm pairs





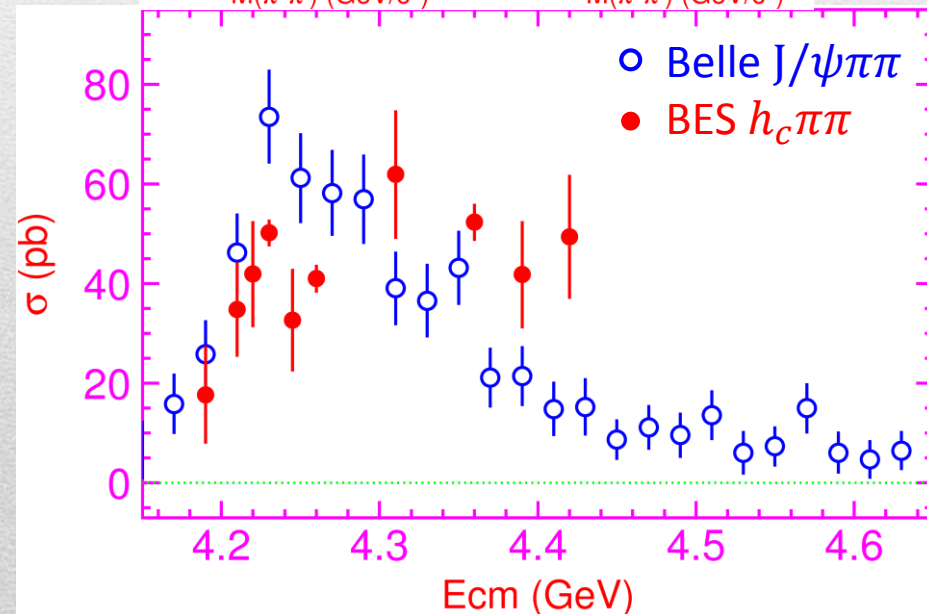
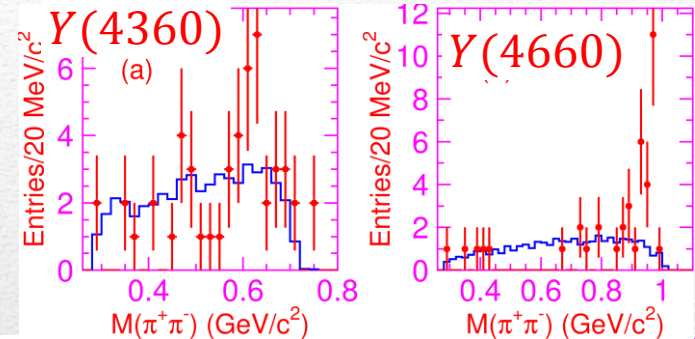
# Vector $Y$ states



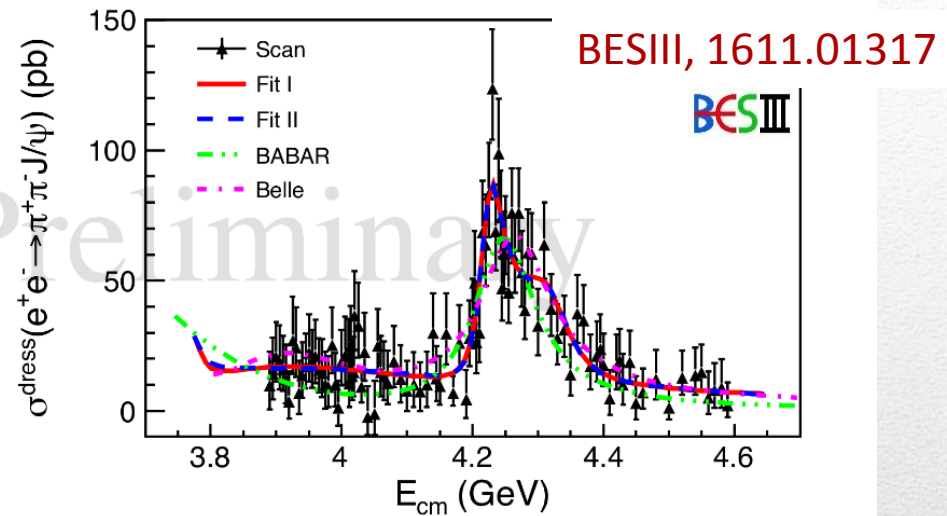
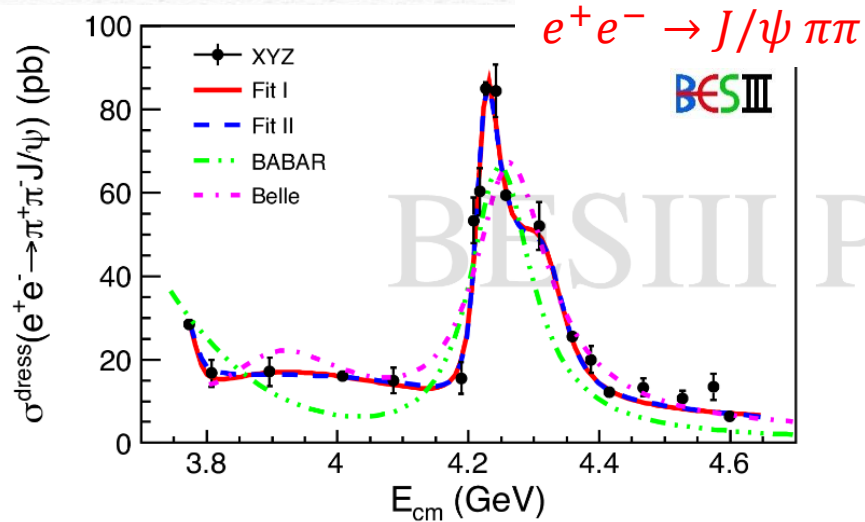
Sizeable HQSS violation

The lineshape in  $h_c \pi\pi$  looks pretty different  
Different states contributing?

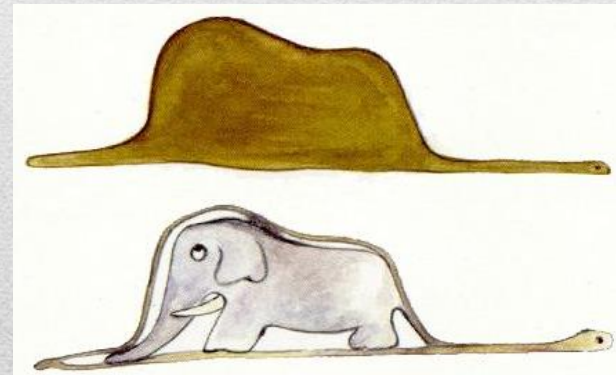
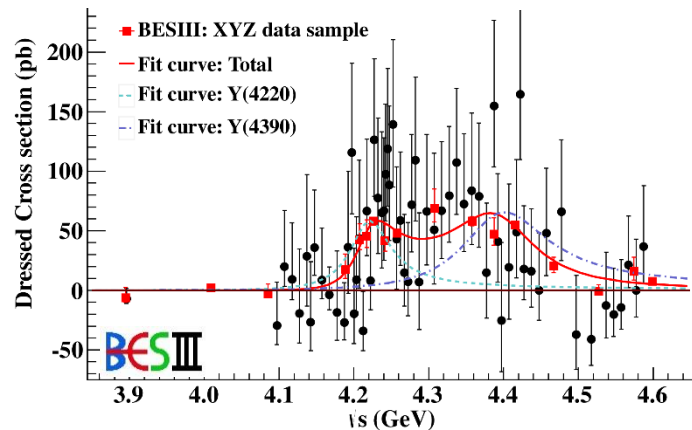
A component  $Y(4260) \rightarrow J/\psi f_0(980)$   
might explain why  $Y(4260) \rightarrow \psi(2S)\pi\pi$



# Vector $Y$ states in BESIII



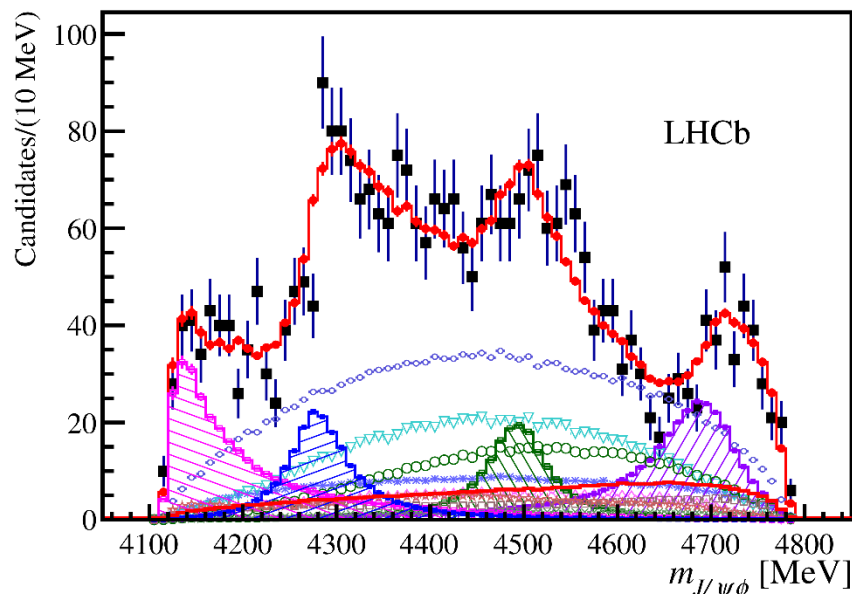
$e^+e^- \rightarrow h_c \pi\pi$  BESIII, 1611.07044



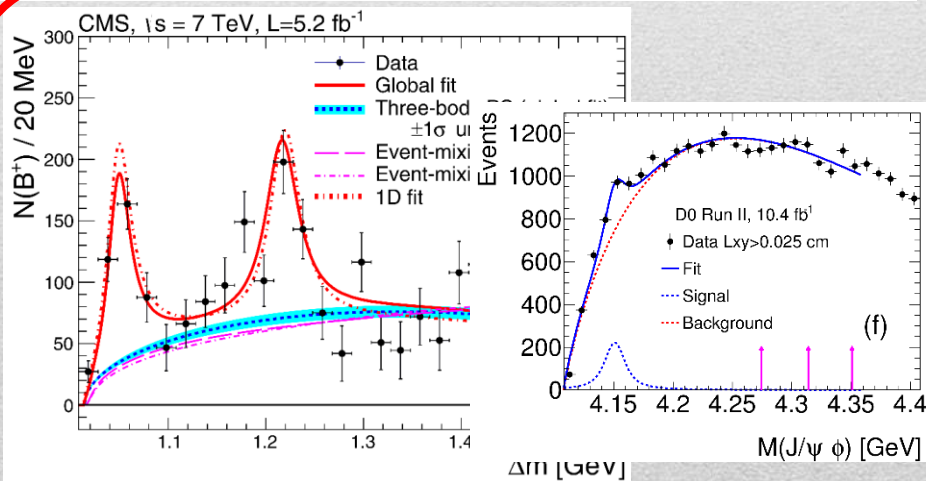
New data by BESIII seem to draw different conclusions, waiting for a sounder combined analysis



# Tetraquark: the $c\bar{c}s\bar{s}$ states



$$\begin{array}{ccc}
 \begin{array}{c} 0^{++} \\ \text{X(4274)} \end{array} + \kappa & \begin{array}{c} 1^{+-} \\ + \kappa \end{array} & \begin{array}{c} 2^{++} \\ \text{X(4274)} \end{array} + \kappa \\
 \\
 \begin{array}{c} 1^{++} \\ \text{X(4140)} \end{array} - \kappa & \begin{array}{c} 1^{+-} \\ - \kappa \end{array} & \\
 \\
 0^{++} - 3\kappa & & \uparrow + 2 m_{[cs]} = M
 \end{array}$$



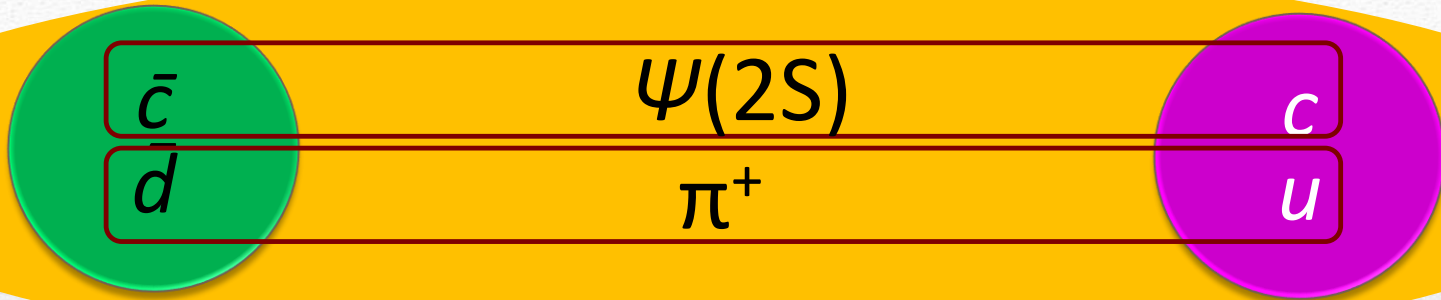
Good description of the spectrum **but** one has to assume the axial assignment for the X(4274) to be incorrect (two unresolved states with  $0^{++}$  and  $2^{++}$ )

Maiani, Polosa and Riquer, PRD 94, 054026

Much narrower than LHCb! Look for prompt!

# Dynamical movie

$Z^+(4430)$



Brodsky, Hwang, Lebed PRL 113 112001

- Since this is still a  $\mathbf{3} \leftrightarrow \bar{\mathbf{3}}$  color interaction, just use the Cornell potential:

$$V(r) = -\frac{4}{3} \frac{\alpha_s}{r} + br + \frac{32\pi\alpha_s}{9m_{cq}^2} \left( \frac{\sigma}{\sqrt{\pi}} \right)^3 e^{-\sigma^2 r^2} \mathbf{S}_{cq} \cdot \mathbf{S}_{\bar{c}\bar{q}},$$

e.g. Barnes *et al.*, PRD 72, 054026

- Use that the kinetic energy released in  $\bar{B}^0 \rightarrow K^- Z^+(4430)$  converts into potential energy until the diquarks come to rest
- Hadronization most effective at this point (WKB turning point)

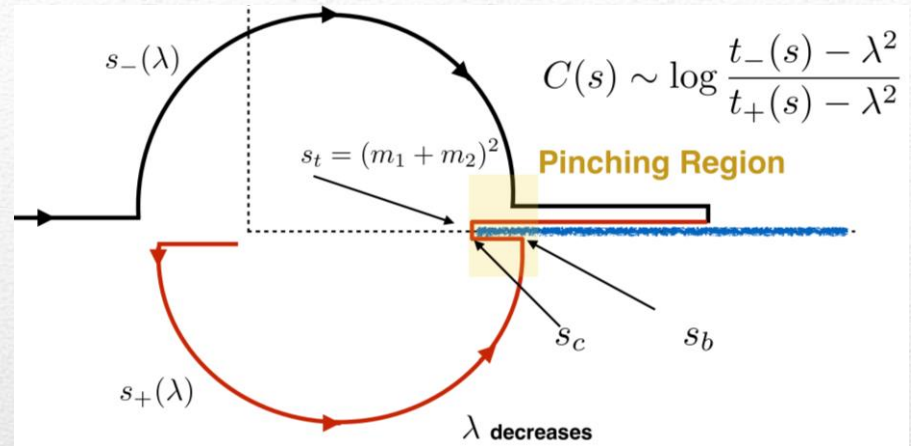
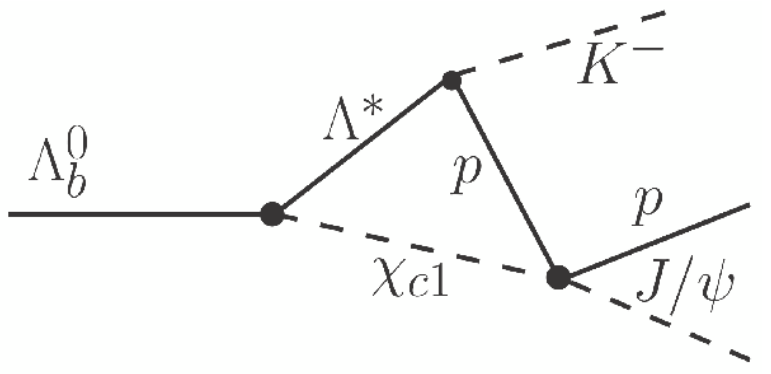
$$r_Z = 1.16 \text{ fm}, \langle r_{\psi(2S)} \rangle = 0.80 \text{ fm}, \langle r_{J/\psi} \rangle = 0.39 \text{ fm}$$

$$\frac{B(Z^+(4430) \rightarrow \psi(2S)\pi^+)}{B(Z^+(4430) \rightarrow J/\psi \pi^+)} \sim 72$$

( $> 10 \text{ exp.}$ )



# Other models: triangle singularity



Logarithmic branch points due to exchanges in the cross channels can simulate a resonant behavior, only in **very special kinematical conditions** (Coleman and Norton, Nuovo Cim. 38, 438), However, this effects **cancels in Dalitz projections, no peaks** (Schmid, Phys.Rev. 154, 1363)

$$f_{0,i}(s) = b_{0,i}(s) + \frac{t_{ij}}{\pi} \int_{s_i}^{\infty} ds' \frac{\rho_j(s') b_{0,j}(s')}{s' - s}$$

...but the cancellation can be spread in different channels, you might still see peaks in other channels only!

Szczepaniak, PLB747, 410-416

Szczepaniak, PLB757, 61-64

Guo, Meissner, Wang, Yang PRD92, 071502

# Pentaquark photoproduction

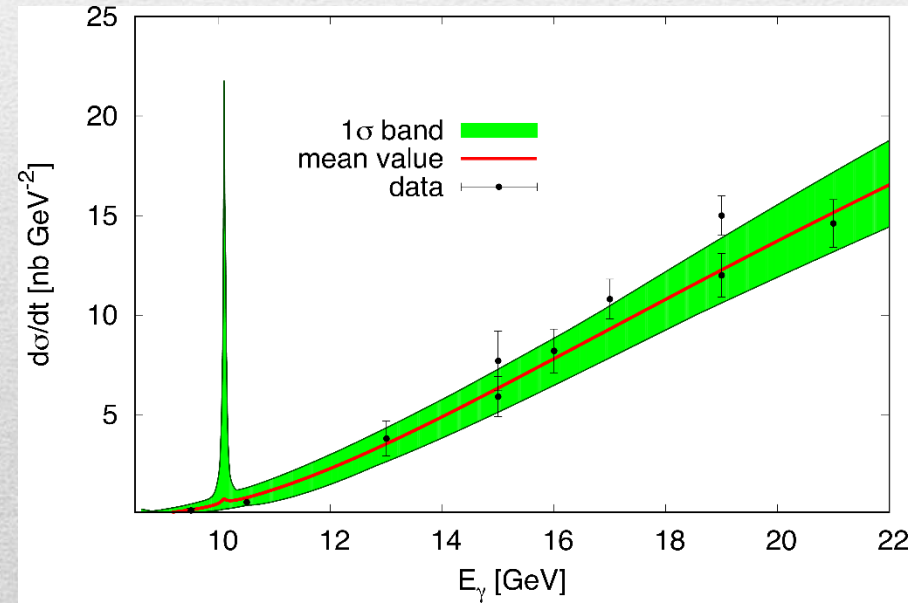
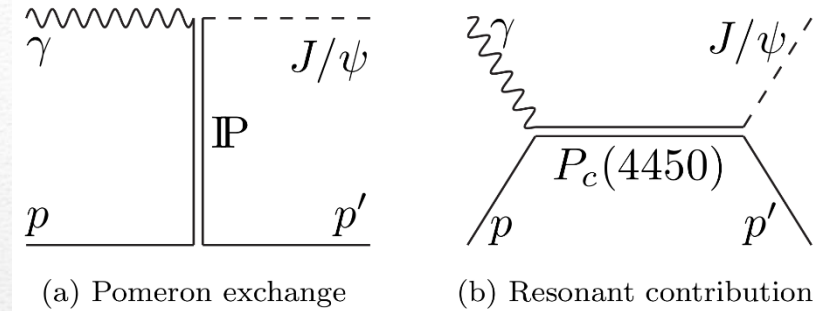
To exclude any rescattering mechanism,  
we propose to search the  $P_c(4450)$  state in  
**photoproduction**

We use the (few) existing data and  
**VMD + pomeron inspired bkg**  
to estimate the cross section

$$J^P = (3/2)^-$$

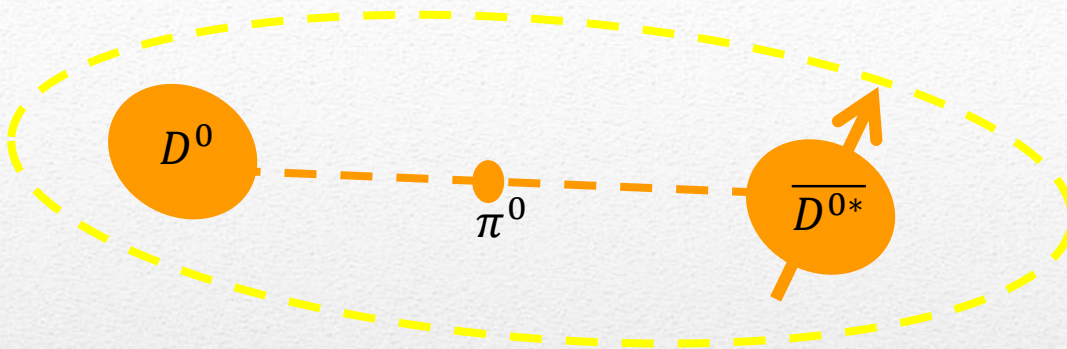
$\sigma_s$ (MeV)	0	60	120
$A$	$0.156^{+0.029}_{-0.020}$	$0.157^{+0.039}_{-0.021}$	$0.157^{+0.037}_{-0.022}$
$\alpha_0$	$1.151^{+0.018}_{-0.020}$	$1.150^{+0.018}_{-0.026}$	$1.150^{+0.015}_{-0.023}$
$\alpha'$ (GeV $^{-2}$ )	$0.112^{+0.033}_{-0.054}$	$0.111^{+0.037}_{-0.064}$	$0.111^{+0.038}_{-0.054}$
$s_t$ (GeV $^2$ )	$16.8^{+1.7}_{-0.9}$	$16.9^{+2.0}_{-1.6}$	$16.9^{+2.0}_{-1.1}$
$b_0$ (GeV $^{-2}$ )	$1.01^{+0.47}_{-0.29}$	$1.02^{+0.61}_{-0.32}$	$1.03^{+0.49}_{-0.31}$
$\mathcal{B}_{\psi p}$ (95% CL)	$\leq 29 \%$	$\leq 30 \%$	$\leq 23 \%$

**A. Blin, AP *et al.* (JPAC), PRD94, 034002**





# Other models: Molecule



Tornqvist, Z.Phys. C61, 525

Braaten and Kusunoki, PRD69 074005

Swanson, Phys.Rept. 429 243-305

$$X(3872) \sim \bar{D}^0 D^{*0}$$

$$Z_c(3900) \sim \bar{D}^0 D^{*+}$$

$$Z'_c(4020) \sim \bar{D}^{*0} D^{*+}$$

$$Y(4260) \sim \bar{D} D_1$$

A **deuteron-like meson pair**, the interaction is mediated by the exchange of light mesons

- Some model-independent relations (**Weinberg's theorem**) ✓
- Good description of **decay patterns** (mostly to constituents) and X(3872) **isospin violation** ✓
- States appear **close to thresholds** ✓ (but **Z(4430)** ✗)
- Lifetime of constituents has to be  $\gg 1/m_\pi$
- Binding energy varies from  $-70$  to  $-0.1$  MeV, or even **positive** (repulsive interaction) ✗
- **Unclear spectrum** (a state for each threshold?) – **depends on potential models** ✗

$$V_\pi(r) = \frac{g_{\pi N}^2}{3} (\vec{\tau}_1 \cdot \vec{\tau}_2) \left\{ [3(\vec{\sigma}_1 \cdot \hat{r})(\vec{\sigma}_2 \cdot \hat{r}) - (\vec{\sigma}_1 \cdot \vec{\sigma}_2)] \left( 1 + \frac{3}{(m_\pi r)^2} + \frac{3}{m_\pi r} \right) + (\vec{\sigma}_1 \cdot \vec{\sigma}_2) \right\} \frac{e^{-m_\pi r}}{r}$$

Needs regularization, cutoff dependence

# Weinberg theorem

Resonant scattering amplitude

$$f(ab \rightarrow c \rightarrow ab) = -\frac{1}{8\pi E_{CM}} g^2 \frac{1}{(p_a + p_b)^2 - m_c^2}$$

with  $m_c = m_a + m_b - B$ , and  $B, T \ll m_{a,b}$

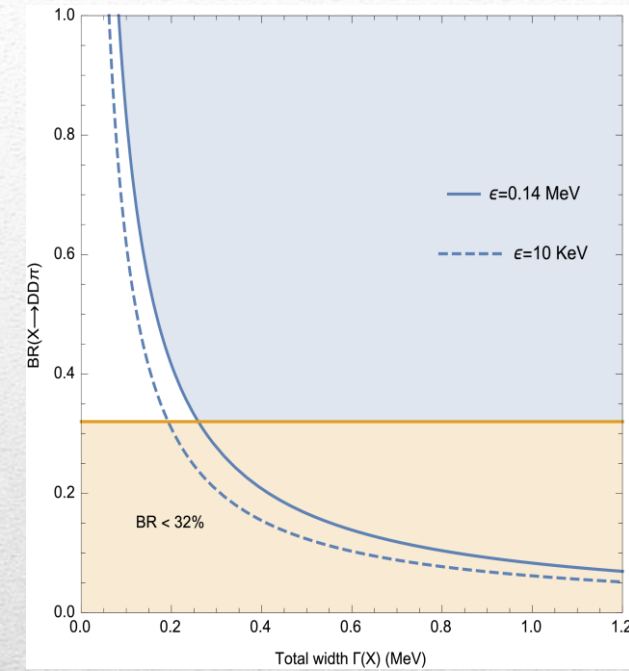
$$f(ab \rightarrow c \rightarrow ab) = -\frac{1}{16\pi(m_a + m_b)^2} g^2 \frac{1}{B + T}$$

This has to be compared with the potential scattering for slow particles ( $kR \ll 1$ , being  $R \sim 1/m_\pi$  the range of interaction) in an attractive potential  $U$  with a superficial level at  $-B$

$$f(ab \rightarrow ab) = -\frac{1}{\sqrt{2\mu}} \frac{\sqrt{B} - i\sqrt{T}}{B + T}, \quad B = \frac{g^4}{512\pi^2} \frac{\mu^5}{(m_a m_b)^2}$$

This has to be fulfilled by **EVERY molecular state**, but:

- $X(3872)$ ,  $B = 0$ ,  $g \neq 0$
- $Z_s$ ,  $B < 0$ , repulsive interaction!
- $Y(4260)$ ,  $kR \sim 1.4$

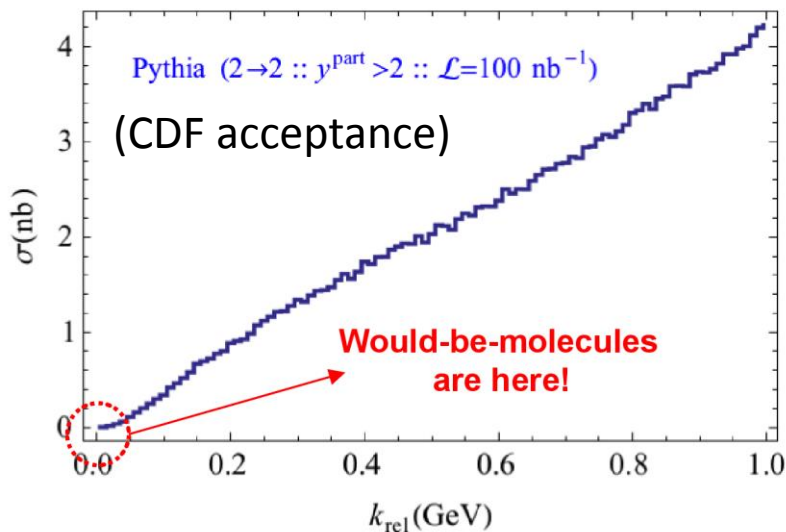


Weinberg, PR 130, 776  
Weinberg, PR 137, B672  
Polosa, PLB 746, 248



# Prompt production of $X(3872)$

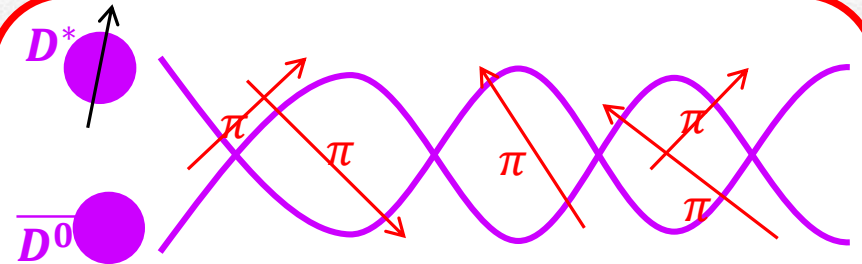
$X(3872)$  is the Queen of exotic resonances, the most popular interpretation is a  $D^0 \bar{D}^{0*}$  **molecule** (bound state, pole in the 1<sup>st</sup> Riemann sheet?) but it is copiously promptly produced at hadron colliders



$$\sigma_{MC}(p\bar{p} \rightarrow DD^* | k < k_{max}) \approx 0.1 \text{ nb}$$

$$\sigma_{exp}(p\bar{p} \rightarrow X(3872)) \approx 30 - 70 \text{ nb!!!}$$

Bignamini *et al.* PRL103 (2009) 162001



A solution can be FSI (rescattering of  $DD^*$ ), which allow  $k_{max}$  to be as large as  $5m_\pi$ ,  
 $\sigma(p\bar{p} \rightarrow DD^* | k < k_{max}) \approx 230 \text{ nb}$

Artoisenet and Braaten, PRD81, 114018

However, the rescattering is flawed by the presence of pions that interfere with  $DD^*$  propagation. Estimating the effect of these pions increases  $\sigma$ , but not enough

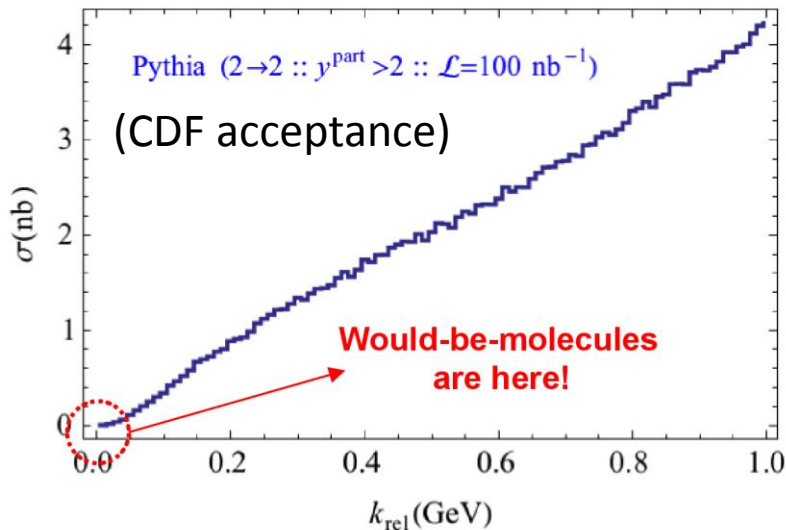
Bignamini *et al.* PLB684, 228-230

Esposito, Piccinini, AP, Polosa, JMP 4, 1569

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

# Prompt production of $X(3872)$

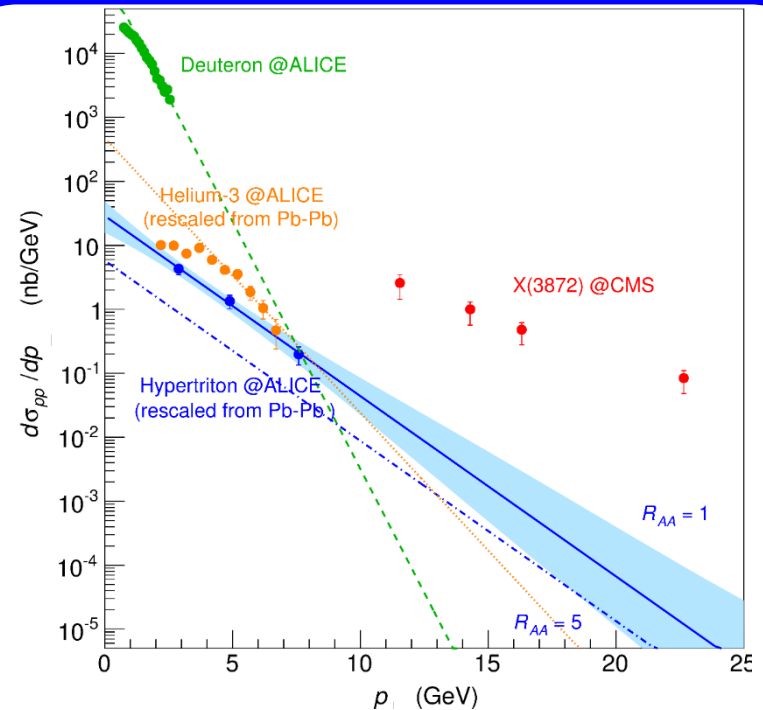
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Bignamini *et al.* PRL103 (2009) 162001



Also, a comparison to light nuclei does not favor the  $X(3872)$  to share the same nature

Esposito, Guerrieri, Maiani,  
Piccinini, AP, Polosa, Riquer, PRD92, 034028



# Counting rules

Brodsky, Lebed PRD91, 114025

- Exotic states can be produced in threshold regions in  $e^+e^-$ , electroproduction, hadronic beam facilities and are best characterized by cross section ratios
- Two examples:

$$1) \quad \frac{\sigma(e^+e^- \rightarrow Z_c^+ \pi^-)}{\sigma(e^+e^- \rightarrow \mu^+ \mu^-)} \propto \frac{1}{s^6} \text{ as } s \rightarrow \infty$$

$$2) \quad \frac{\sigma(e^+e^- \rightarrow Z_c^+ (\bar{c}c\bar{d}u) + \pi^- (\bar{u}d))}{\sigma(e^+e^- \rightarrow \Lambda_c(cud) + \bar{\Lambda}_c(\bar{c}\bar{u}\bar{d}))} \rightarrow \text{const as } s \rightarrow \infty$$

- Ratio numerically smaller if  $Z_c$  behaves like weakly-bound dimeson molecule instead of diquark-antidiquark bound state due to weaker meson color van der Waals forces

Different estimates close to thresholds, and in presence of annihilating  $q \bar{q}$

Guo, Meissner, Wang, Yang, 1607.04020

Voloshin PRD94, 074042

# Towards hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

The absence of many of the predicted states might point to the need for **selection rules**

It is unlikely that the **many close-by thresholds** play no role whatsoever

All the well assessed 4-quark resonances lie close and **above** some meson-meson thresholds:

	Thr.	$\delta$ (MeV)	$A \sqrt{\delta}$ (MeV)	$\Gamma$ (MeV)
$X(3872)$	$\bar{D}^0 D^{*0}$	$0^\dagger$	$0^\dagger$	$0^\dagger$
$Z_c(3900)$	$\bar{D}^0 D^{*+}$	7.8	27.9	27.9
$Z'_c(4020)$	$\bar{D}^{*0} D^{*+}$	6.7	25.9	24.8 <sup>¶</sup>
$X(4140)$	$J/\psi \phi$	a) 31.6	52.7	28.0
		b) 30.1	54.7	83.0
$Z_b(10610)$	$\bar{B}^0 B^{*+}$	2.7	16.6	18.4
$Z'_b(10650)$	$\bar{B}^{*0} B^{*+}$	1.8	13.4	11.5
$X(5568)$	$B_s^0 \pi^+$	61.4	78.4	21.9
$X_{bs}$	$B^+ \bar{K}^0$	5.8	24.1	—

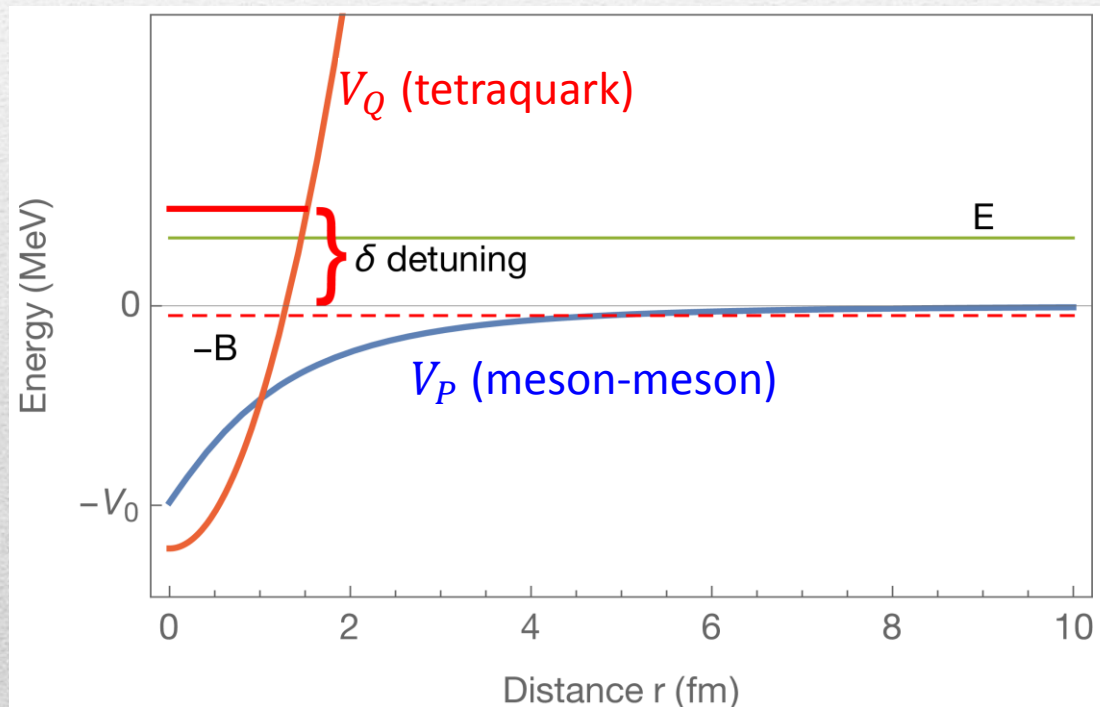
We introduce a **mechanism** that might provide “dynamical selection rules” to explain the presence/absence of resonances from the experimental data.



# Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

Feshbach mechanism occurs when two atoms can interact with **two potentials**, resp. with **continuum (meson-meson)** and **discrete (4q)** spectrum  $\rightarrow$  **hybridization**



Let  $P$  and  $Q$  be orthogonal subspaces of the Hilbert space

$$H = H_{PP} + H_{QQ}$$

We have the (weak) scattering length  $a_P$  in the open channel.

We add an off-diagonal  $H_{QP}$  which connects the two subspaces

# Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

$$\Gamma = -16\pi^3 \rho \Im(T) \sim 16\pi^4 \rho |H_{PQ}|^2 \delta \left( \frac{p_1^2}{2M} + \frac{p_2^2}{2M} - \delta \right)$$

The expected width is the average **over momenta that allow for the existence of a tetraquark**  $p < \bar{p} = 50 \div 100$  MeV

$$\Gamma \sim A\sqrt{\delta}$$

We therefore expect to see a level if:

- $\delta > 0$  the state **lies above threshold**
- $\delta < \frac{\bar{p}^2}{2M}$ , only the **closest threshold** contributes
- The states  $\psi_Q$  and  $\psi_P$  are **orthogonal**

$X(3872)^+$  falls below threshold,  $M(1^{++}) < M(D^{+*}\bar{D}^0)$

$\delta < 0$ , so  $a > 0 \rightarrow$  **Repulsive interaction**

**No charged partners of the  $X(3872)$ !**



# Hybridized tetraquarks – Selection rules

- Consider the **down quark part of the  $X(3872)$**  in the diquarkonium picture:  

$$\Psi_d = X_d = [cd]_0[\bar{c}\bar{d}]_1 + [cd]_1[\bar{c}\bar{d}]_0 \sim (D^{*-}D^+ - D^{*+}D^-) + i(\psi \times \rho^0 - \psi \times \omega^0)$$

↑  
Fierz rearrangement
- The closest threshold from below is  $\Psi_m \sim \bar{D}^0 D^{*0} \longrightarrow \underline{\Psi_d \perp \Psi_m}$  ✓
- But if we consider the **up quark part of the  $X(3872)$** :  

$$\Psi_d = X_u = [cu]_0[\bar{c}\bar{u}]_1 + [cu]_1[\bar{c}\bar{u}]_0 \sim (\bar{D}^{*0}D^0 - D^{*0}\bar{D}^0) - i(\psi \times \rho^0 + \psi \times \omega^0)$$
- But then  $\longrightarrow \underline{\Psi_d \not\perp \Psi_m}$  ✗
- Only  $X_d$  is produced via this mechanism
  - $\longrightarrow$  isospin violation
  - $\longrightarrow$  no hyperfine neutral doublet
- $X_b$**  (A) Diquark model predicts  $M(X_b) \simeq M(Z_b) \simeq (10607 \pm 2)$  MeV  
 (B) The closest orthogonal threshold is  $M(B^0 B^{*0}) = (10604.4 \pm 0.3)$  MeV  
 (C) This could either be above threshold (very narrow state) or below (no state at all)  
 (D) Experimentally the diquark model overpredicts the mass of the  $X$ :  

$$M(Z_c) - M(X) \simeq 32 \text{ MeV}$$
  
 (E) We favor the below threshold scenario  $\longrightarrow$  no  $X_b$  should be seen

A. Esposito

# Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

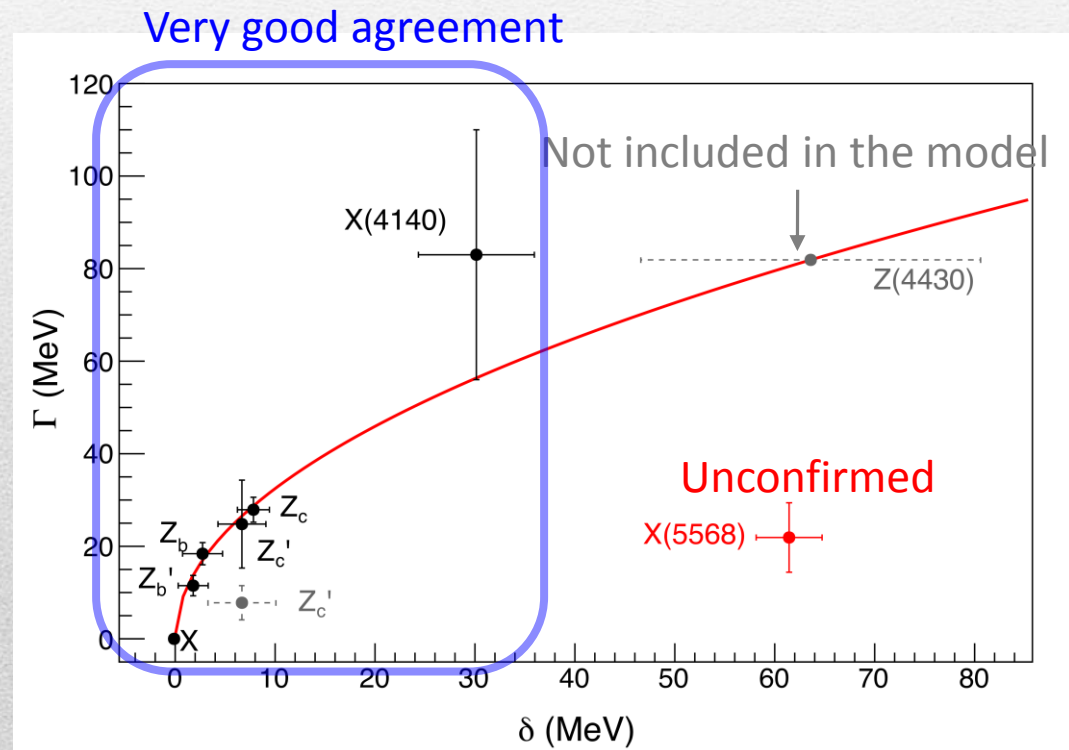
The model works only if no direct transition between closed channel levels can occur  
This prevents the straightforward generalization to  $L = 1$  and radially excited states  
(like the  $Y$ s or the  $Z(4430)$ )

In this picture, a  $[bu][\bar{s}\bar{d}]$  state with resonance parameters of the  $X(5568)$  observed by D0 is not likely

Also, one has to ensure the orthogonality between the two Hilbert subspaces  $P$  and  $Q$ .  
This might affect the estimate for the  $X(4140)$

All the resonances can be fitted with

$$A = (10.3 \pm 1.3) \text{ MeV}^{1/2}$$
$$\chi^2/\text{DOF} = 1.2/5$$






# Production of hybridized tetraquarks

Going back to  $pp(\bar{p})$  collisions, we can imagine hadronization to produce a state

$$|\psi\rangle = \alpha|[qQ][\bar{q}\bar{Q}]\rangle_c + \beta|(\bar{q}q)(\bar{Q}Q)\rangle_o + \gamma|(\bar{q}Q)(\bar{Q}q)\rangle_o$$

If  $\beta, \gamma \gg \alpha$ , an initial tetraquark state is not likely to be produced  
The open channel mesons fly apart  
(see MC simulations)



If hybridization mechanism is at work, an open state can resonate in a closed one

$\alpha$  expected to be small in Large N limit, Maiani, Polosa, Riquer JHEP 1606, 160

## No prompt production without hybridization mechanism!

Note that only the  $X(3872)$  has been observed promptly so far...

...and a narrow  $X(4140)$  not compatible with the LHCb one → **needs confirmation**

# Joint Physics Analysis Center

JPAC was funded to support the extraction of physics results from analysis of experimental data, through work on theoretical, phenomenological and data analysis tools



Former members:  
L. Dai (Bonn), I. Danilkin (Mainz),  
P. Guo (Cal. State), M. Shi (Peking)

Students, Postdocs, Faculties



Data

Amplitude  
analysis (JPAC)

Spectrum and  
properties



# Interactive tools

- Completed projects are fully documented on interactive portals
- These include description on physics, conventions, formalism, etc.
- The web pages contain source codes with detailed explanation how to use them. Users can run codes online, change parameters, display results.

<http://www.indiana.edu/~jpac/>

## Joint Physics Analysis Center

[HOME](#) [PROJECTS](#) [PUBLICATIONS](#) [LINKS](#)



This project is supported by NSF

$$\pi N \rightarrow \pi N$$

### Formalism

The pion-nucleon scattering is a function of 2 variables. The first is the beam momentum in the laboratory frame  $p_{\text{lab}}$  (in GeV) or the total energy squared  $s = W^2$  (in  $\text{GeV}^2$ ). The second is the cosine of



### Resources

- Publications:** [Mat15a] and [Wor12a]
- SAID partial waves:** compressed zip file
- C/C++:** C/C++ file
- Input file:** param.txt
- Output files:** output0.txt, output1.txt, SigTot.txt, Observables0.txt, Observables1.txt
- Contact person:** Vincent Mathieu
- Last update:** June 2016

The SAID partial waves are in the format provided online on the [SAID webpage](#) :

$p_{\text{lab}}$   $\delta$   $\epsilon(\delta)$   $1 - \eta^2$   $\epsilon(1 - \eta^2)$  Re PW Im PW SGT SGR

$\delta$  and  $\eta$  are the phase-shift and the inelasticity.  $\epsilon(x)$  is the error on  $x$ . SGT is the total cross section and SGR is the total reaction cross section.

Format of the input and output files: [\[show/hide\]](#)  
Description of the C/C++ code: [\[show/hide\]](#)

### Simulation

Range of the running variable:

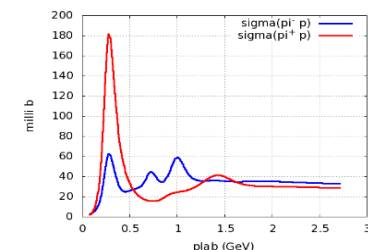
$s$ in $\text{GeV}^2$	(min max step)	1,2	:	6	:	0,01	:
$p_{\text{lab}}$ in GeV	(min max step)	0,1	:	4	:	0,01	:
$\nu$ in GeV	(min max step)	0,3	:	4	:	0,01	:
$t$ in $\text{GeV}^2$	(min max step)	-1	:	0	:	0,01	:

The fixed variable:

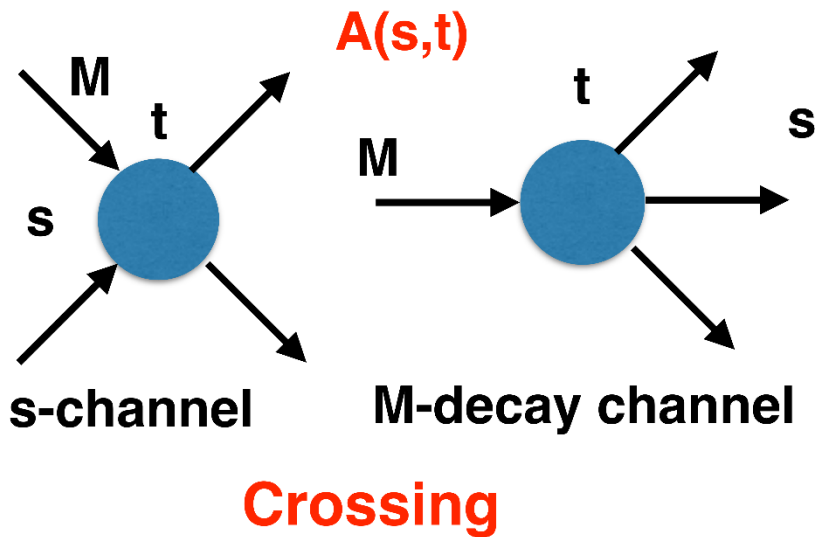
$t$  in  $\text{GeV}^2$

$p_{\text{lab}}$  in GeV

### Results



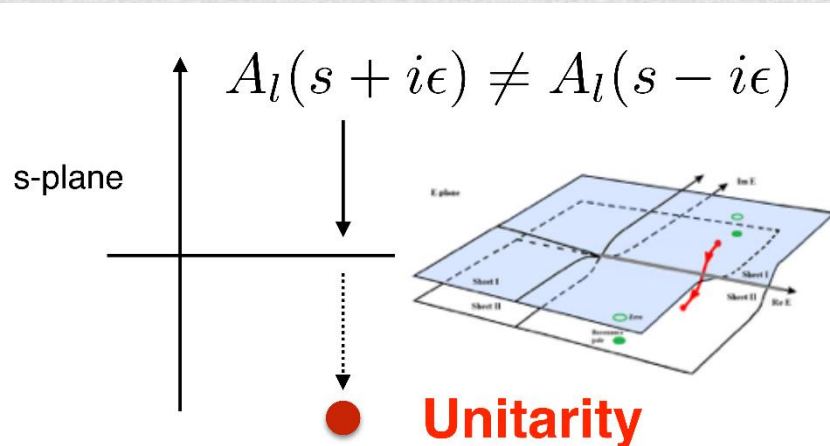
# S-Matrix principles



$$A(s, t) = \sum_l A_l(s) P_l(z_s)$$

**Analyticity**

$$A_l(s) = \lim_{\epsilon \rightarrow 0} A_l(s + i\epsilon)$$

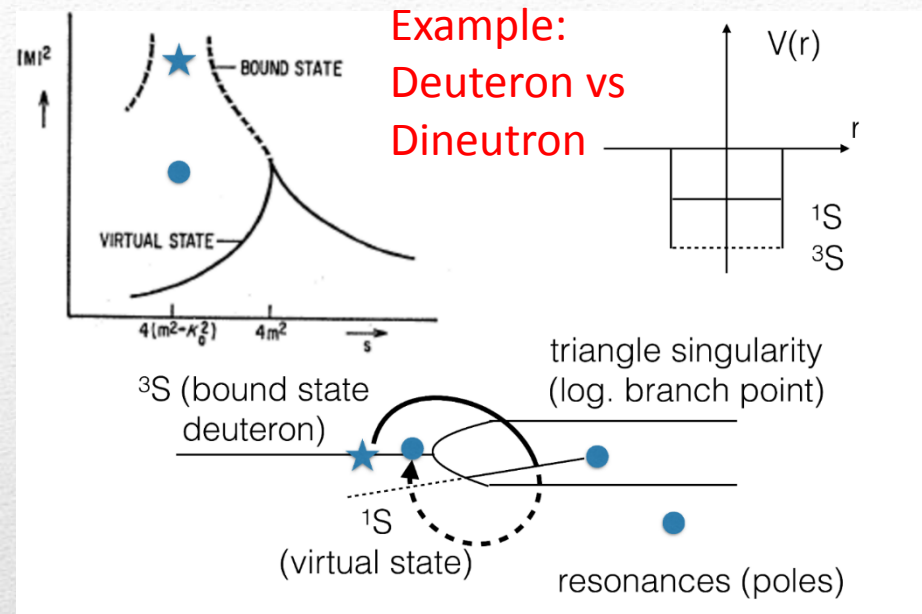


These are constraints the amplitudes have to satisfy, but do not fix the dynamics

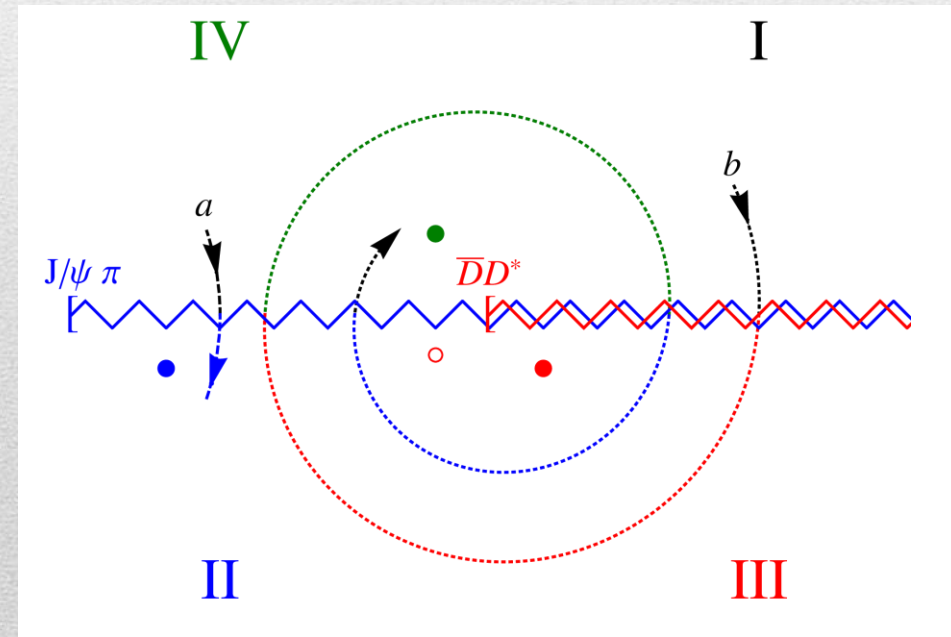
**Resonances (QCD states) are poles in the unphysical Riemann sheets**



# Pole hunting



More complicated structure when more thresholds arise:  
two sheets for each new threshold

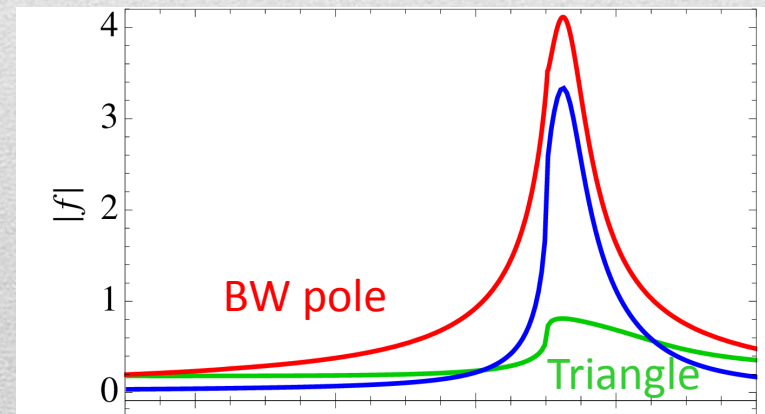
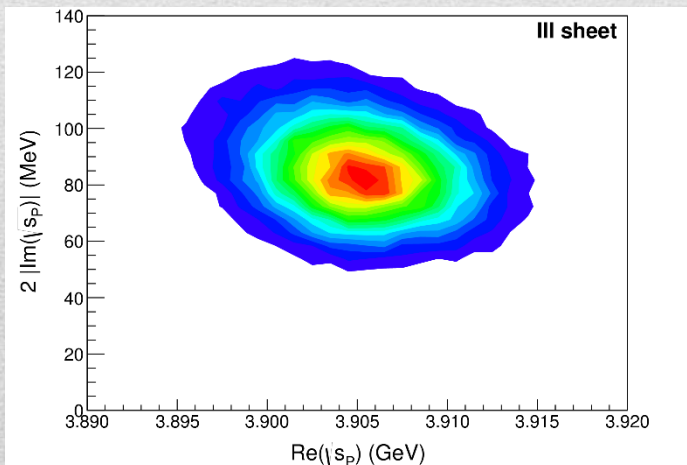
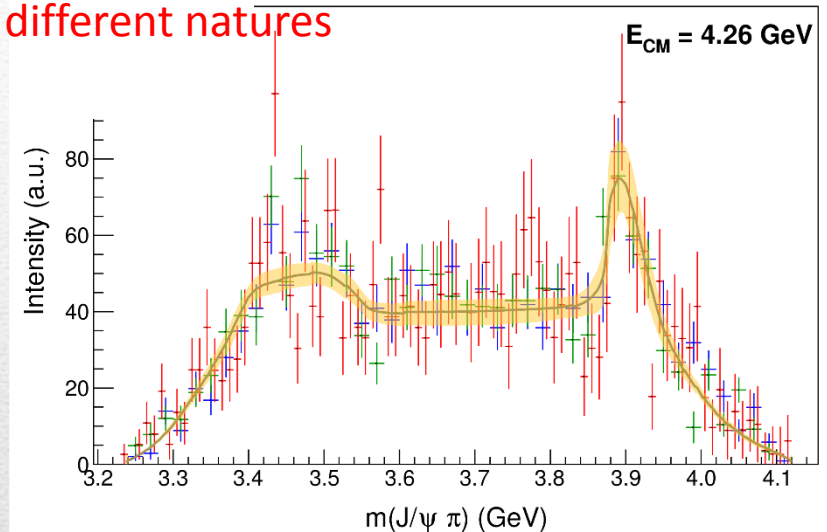
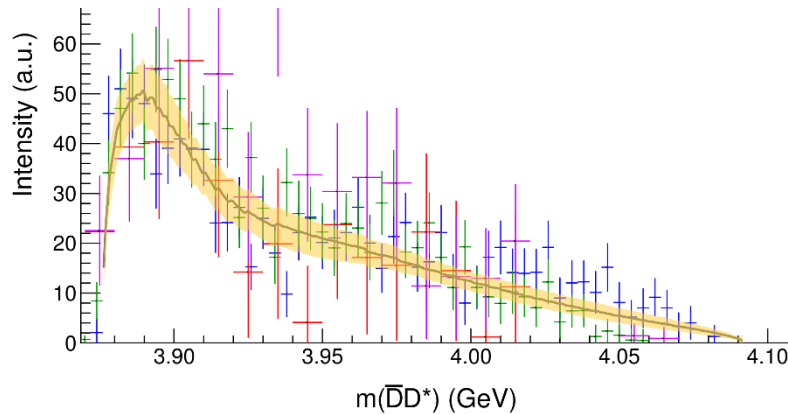


III sheet: usual resonances  
IV sheet: cusps (virtual states)

# Case study, $Z_c(3900)$

One can test different parametrizations of the amplitude,  
which correspond to **different singularities**  $\rightarrow$  **different natures**

**Case 1: Breit-Wigner-like singularity**

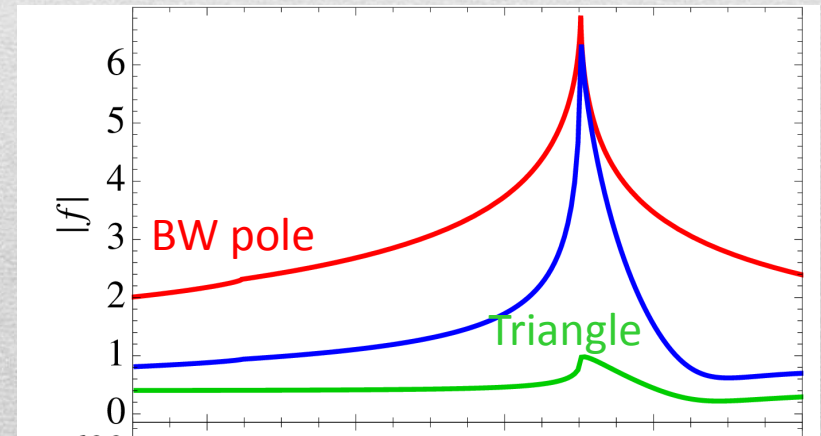
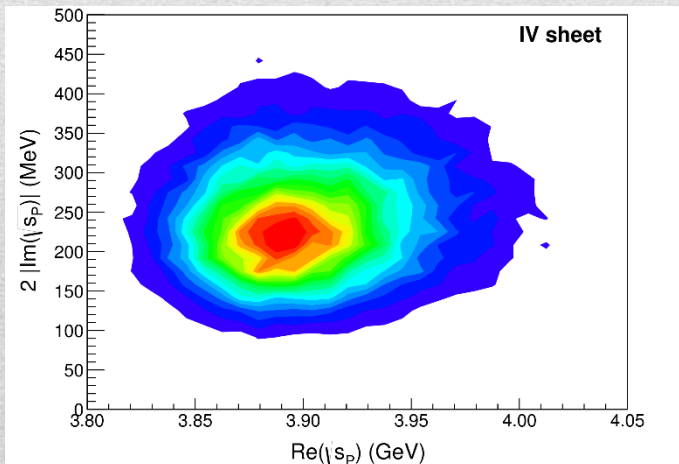
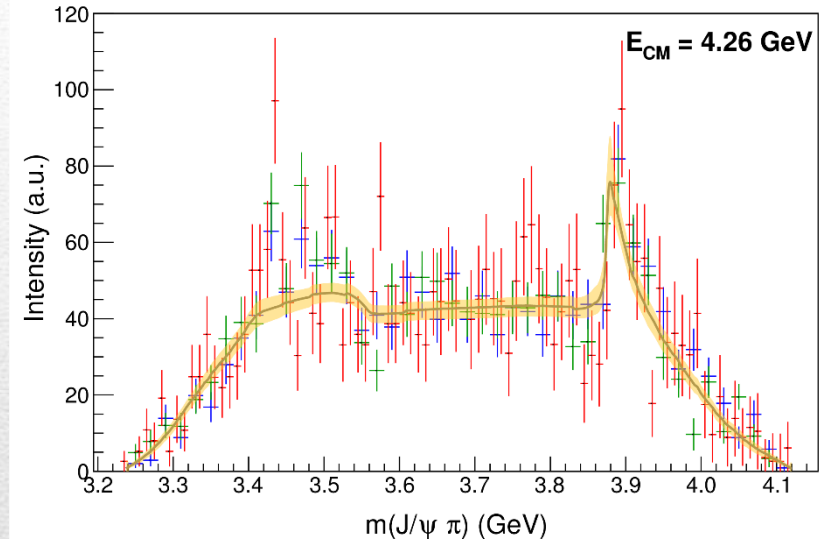
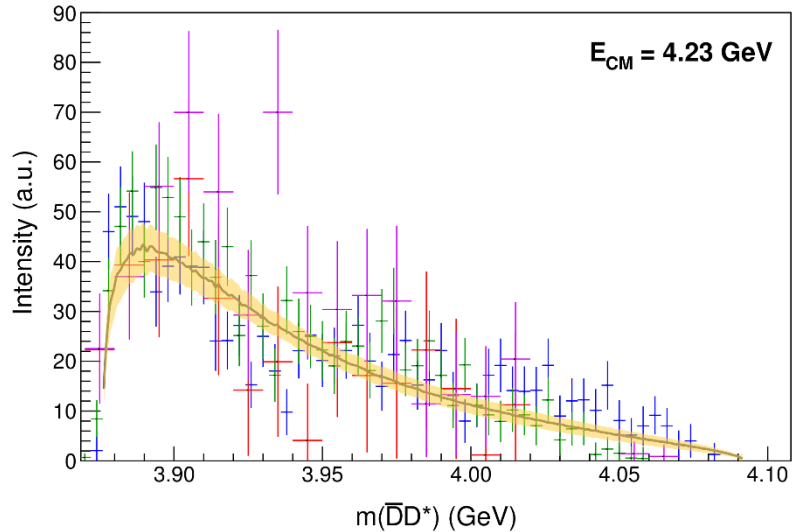


AP, A. Szczepaniak *et al.* (JPAC), to appear



# Case study, $Z_c(3900)$

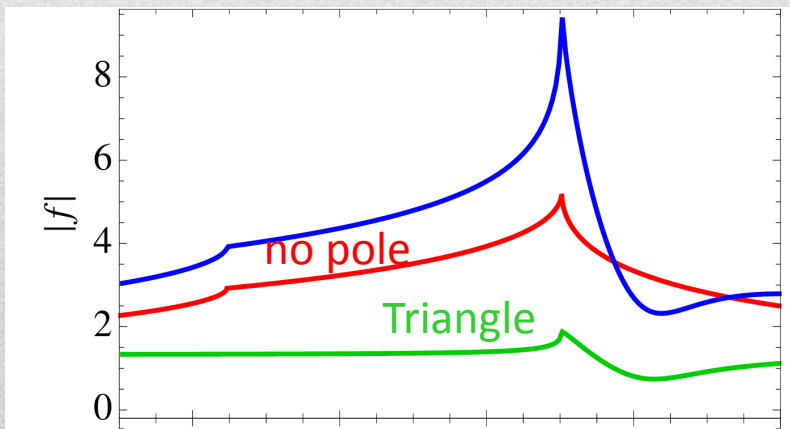
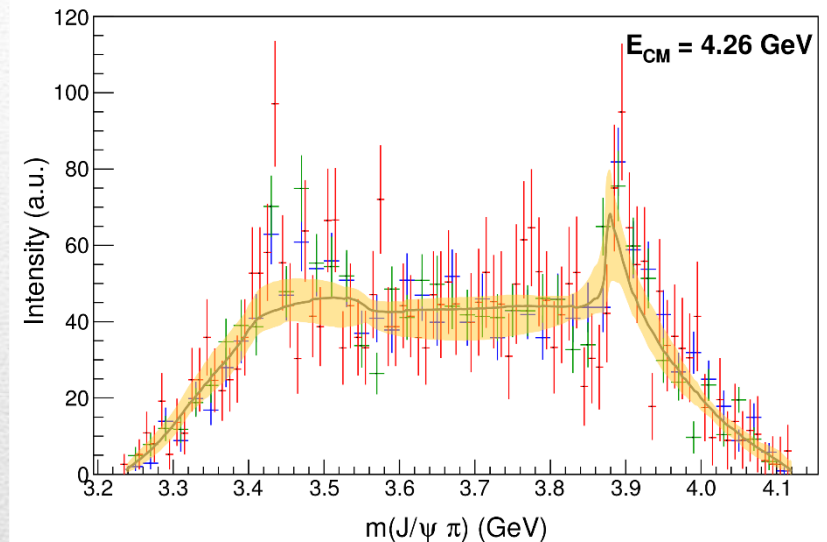
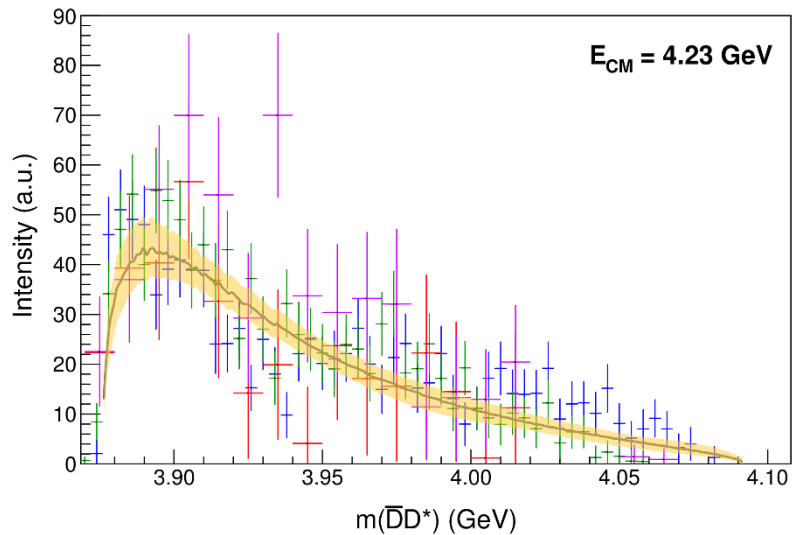
## Case 2: $4^\circ$ sheet singularity (virtual state)



AP, A. Szczepaniak *et al.* (JPAC), to appear

# Case study, $Z_c(3900)$

## Case 3: triangle singularity only



No strong conclusion can be driven yet, but we are establishing the method to use when higher statistics will be available (in particular to constrain the  $D_1(2420)$  contribution)

AP, A. Szczepaniak *et al.* (JPAC), to appear



# Conclusions & prospects

- The discovery of **exotic states** has challenged the well established Charmonium framework
- Some fantasy needed, many phenomenological models introduced.
- Experiments are very prolific! **Constant feedback on predictions**
- **Nuclei observation at hadron colliders** can give an unexpected help in testing some phenomenological hypotheses for the XYZP states
- Search for exotic states in **prompt production** is a necessary step to improve our understanding of the sector
- Hybridization mechanisms might be effective in **reducing the number of states** predicted by the tetraquark picture
- Thorough **amplitude analyses** might shed some light on the microscopic nature of the new states

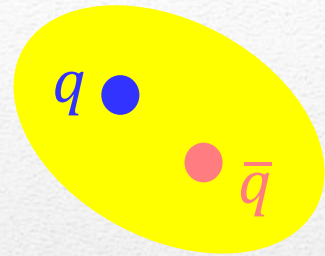
**Thank you**

# BACKUP





# Dictionary – Quark model



$L$  = orbital angular momentum

$S$  = spin  $q + \bar{q}$

$J$  = total angular momentum  
= exp. measured spin

$I$  = isospin = 0 for quarkonia

$$L - S \leq J \leq L + S$$

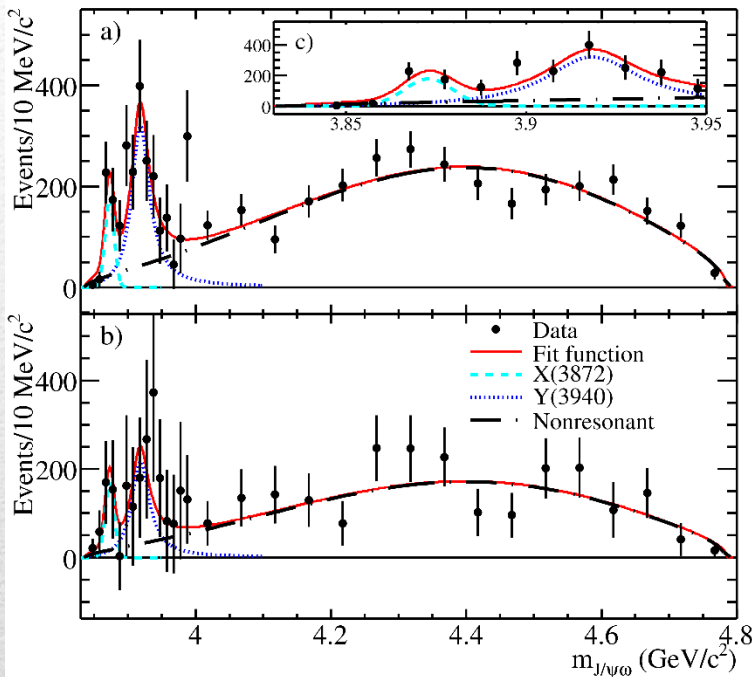
$$P = (-1)^{L+1}, C = (-1)^{L+S}$$

$$G = (-1)^{L+S+I}$$

$J^{PC}$	$L$	$S$	Charmonium ( $c\bar{c}$ )	Bottomonium ( $b\bar{b}$ )
$0^{-+}$	0 ( $S$ -wave)	0	$\eta_c(nS)$	$\eta_b(nS)$
$1^{--}$		1	$\psi(nS)$	$\Upsilon(nS)$
$1^{+-}$	1 ( $P$ -wave)	0	$h_c(nP)$	$h_b(nP)$
$0^{++}$		1	$\chi_{c0}(nP)$	$\chi_{b0}(nP)$
$1^{++}$		1	$\chi_{c1}(nP)$	$\chi_{b1}(nP)$
$2^{++}$		1	$\chi_{c2}(nP)$	$\chi_{b2}(nP)$

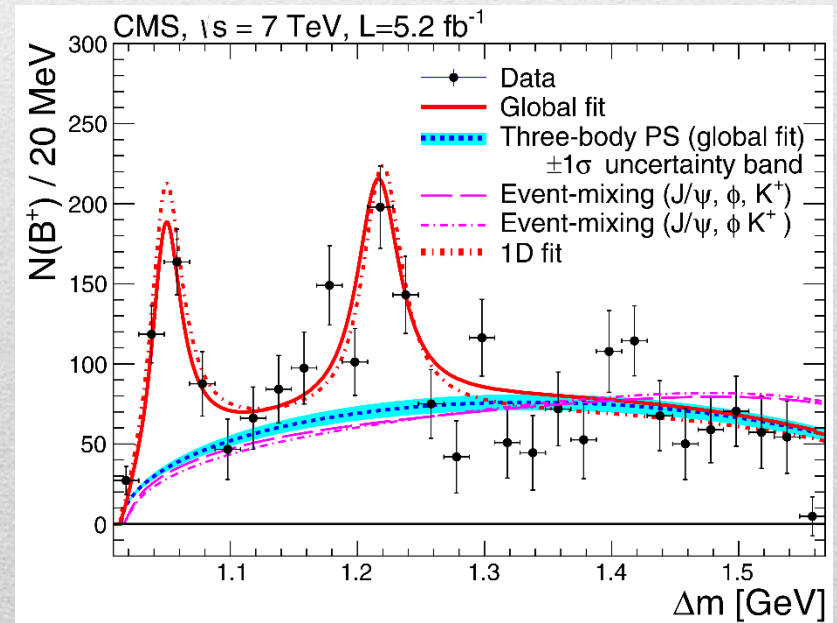
But  $J/\psi = \psi(1S)$ ,  $\psi' = \psi(2S)$

# Other beasts



One/two peaks seen in  $B \rightarrow X K \rightarrow J/\psi \phi K$ , close to threshold

$X(3915)$ , seen in  $B \rightarrow X K \rightarrow J/\psi \omega$   
 and  $\gamma\gamma \rightarrow X \rightarrow J/\psi \omega$   
 $J^{PC} = 0^{++}$ , candidate for  $\chi_{c0}(2P)$   
 But  $X(3915) \nrightarrow D\bar{D}$  as expected,  
 and the hyperfine splitting  
 $M(2^{++}) - M(0^{++})$  too small

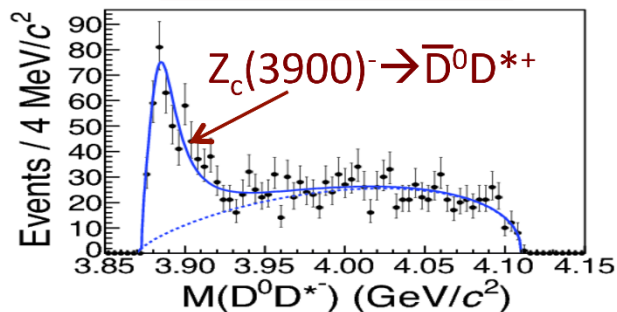




# $Y(4260) \rightarrow \bar{D} D_1?$

$e^+e^- \rightarrow Y(4260) \rightarrow \pi^- \bar{D}^0 D^{*+}$

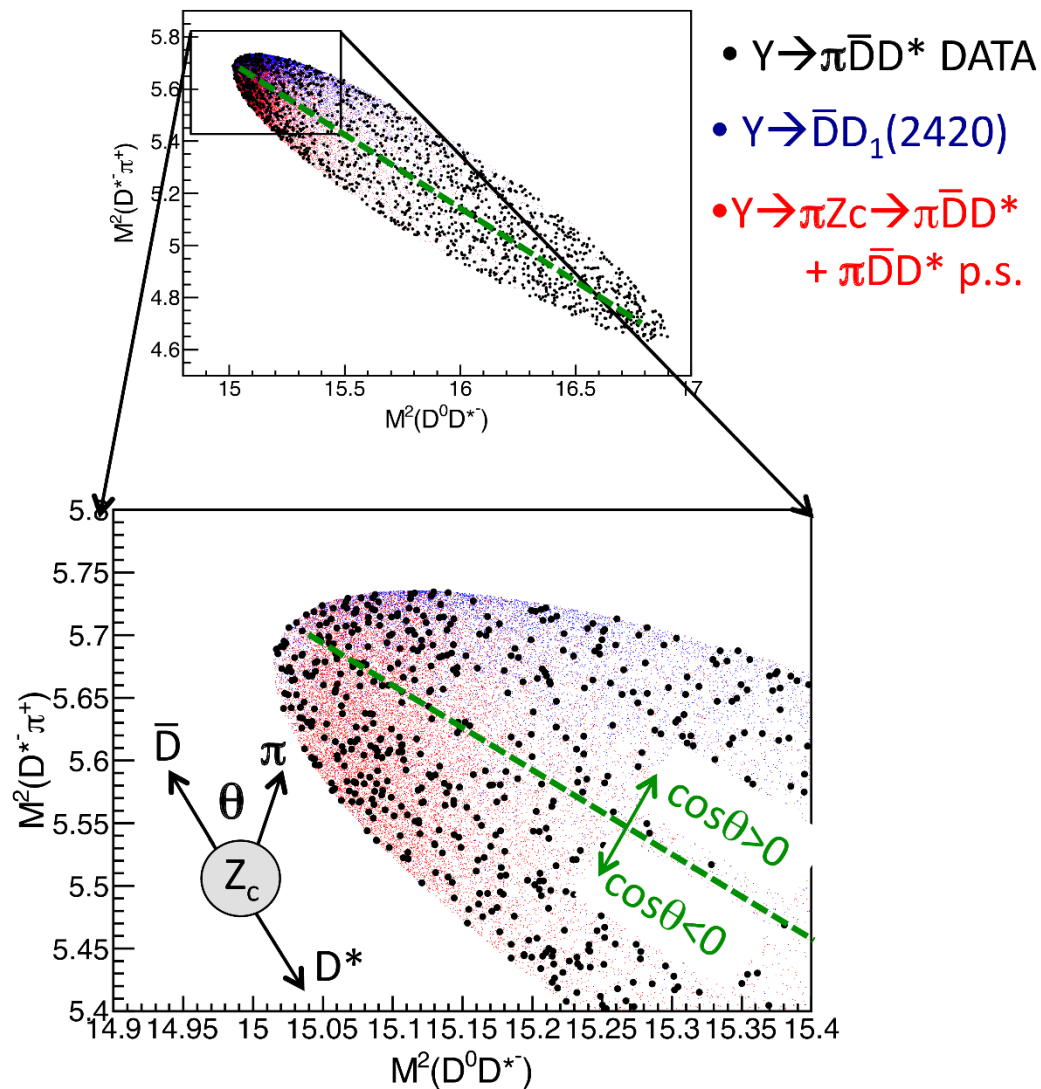
BESIII PRL 112, 022001



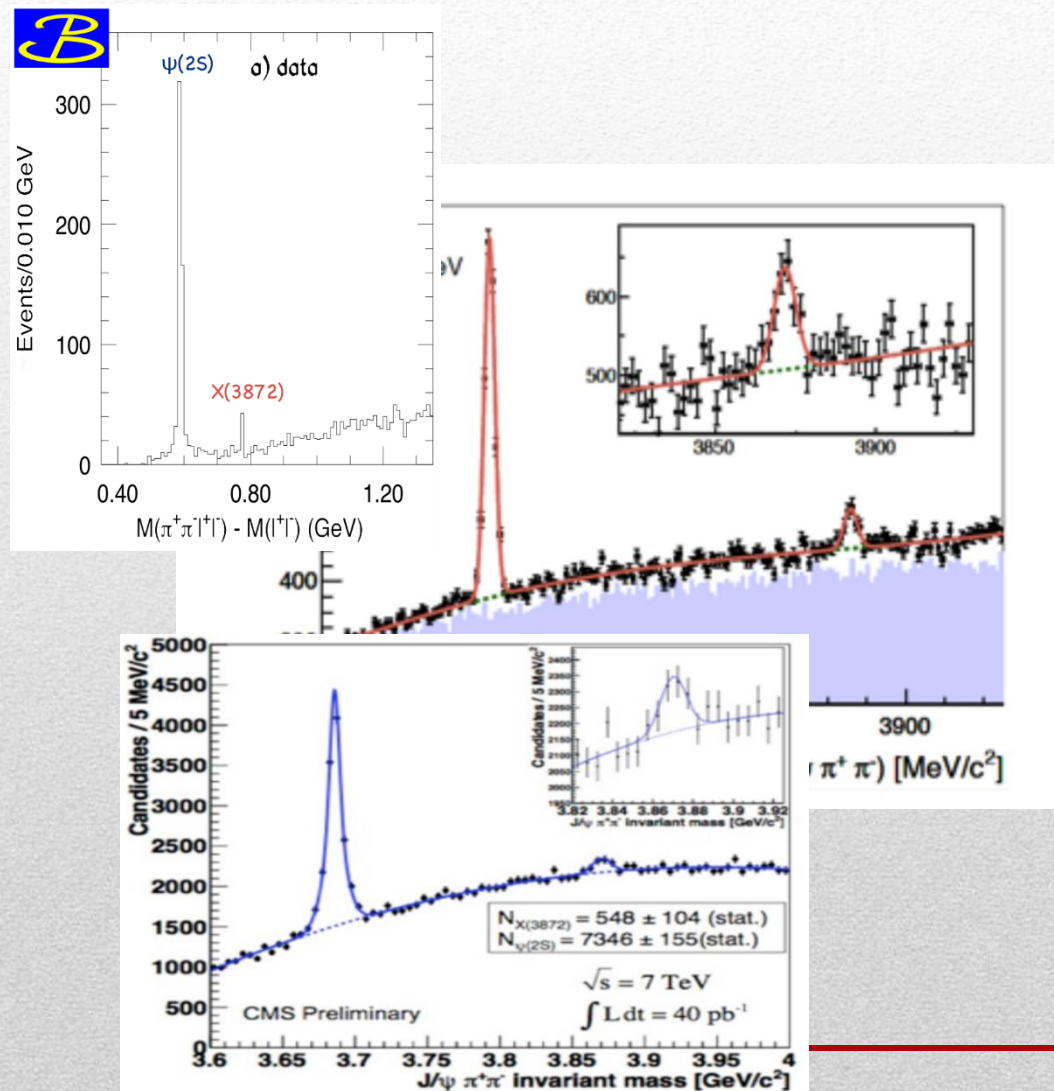
$$\mathcal{A} = \frac{N_{|\cos\theta|>0.5} - N_{|\cos\theta|<0.5}}{N_{|\cos\theta|>0.5} + N_{|\cos\theta|<0.5}}$$

	DD <sub>1</sub> MC	Z <sub>c</sub> +ps MC	data
$\mathcal{A}$	$0.43 \pm 0.04$	$0.02 \pm 0.02$	$0.12 \pm 0.06$

Not a lot of room for  $\bar{D} D_1(2410)$



# X(3872)



- Discovered in  
 $B \rightarrow K X \rightarrow K J/\psi \pi\pi$
- Very close to  $DD^*$  threshold
- Too narrow for an above-threshold charmonium
- Isospin violation too big  
 $\frac{\Gamma(X \rightarrow J/\psi \omega)}{\Gamma(X \rightarrow J/\psi \rho)} \sim 0.8 \pm 0.3$
- Mass prediction not compatible with  $\chi_{c1}(2P)$

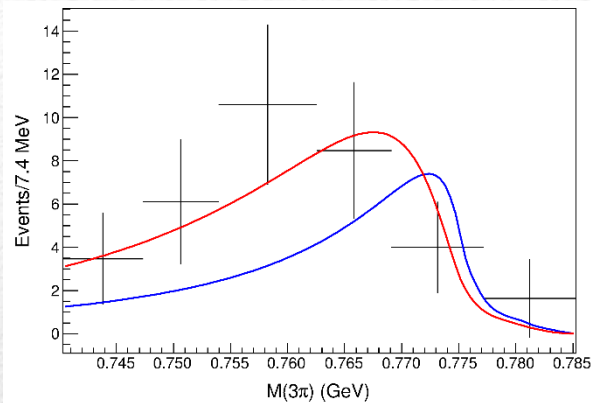
$$M = 3871.68 \pm 0.17 \text{ MeV}$$

$$M_X - M_{DD^*} = -3 \pm 192 \text{ keV}$$

$$\Gamma < 1.2 \text{ MeV @90\%}$$

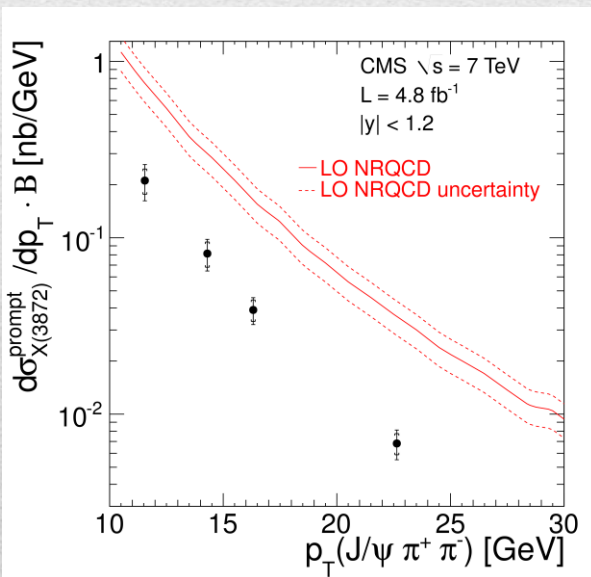
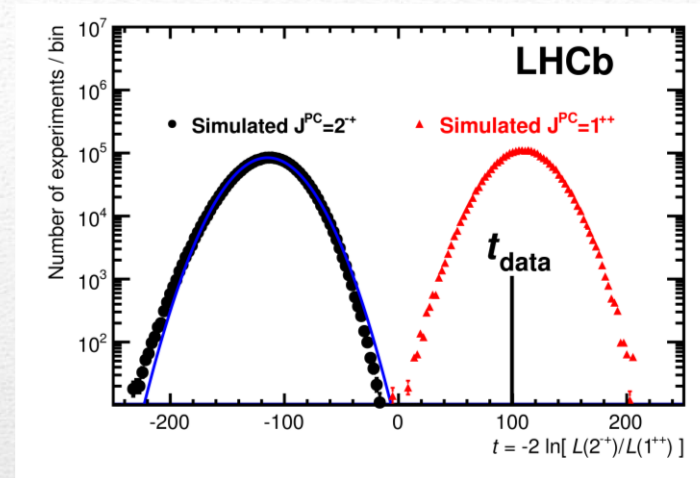


# X(3872)



BaBar data in  $X \rightarrow J/\psi \omega$   
 favor  $J^{PC} = 2^{-+}$ ,  
 but LHCb in  $X \rightarrow J/\psi \rho$   
 measures  $1^{++}$  at  $8\sigma$

Faccini, AP, Piccinini, Polosa  
 PRD 86, 054012  
 LHCb, PRL 110, 222001



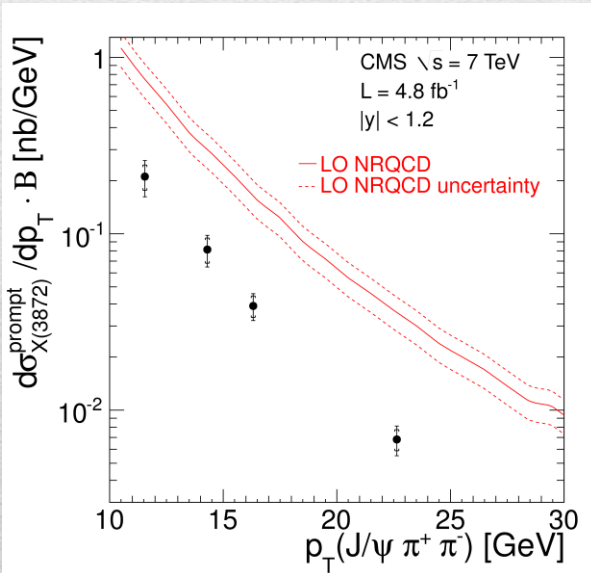
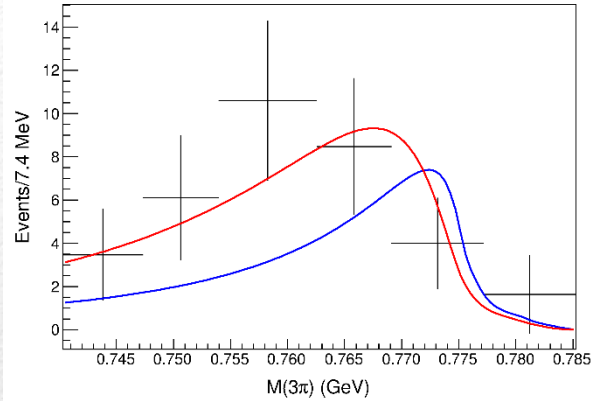
Large prompt production  
 at hadron colliders

$$\sigma_B / \sigma_{TOT} = (26.3 \pm 2.3 \pm 1.6)\%$$

$$\sigma_{PR} \times B(X \rightarrow J/\psi \pi \pi) = (1.06 \pm 0.11 \pm 0.15) \text{ nb}$$

CMS, JHEP 1304, 154

# X(3872)

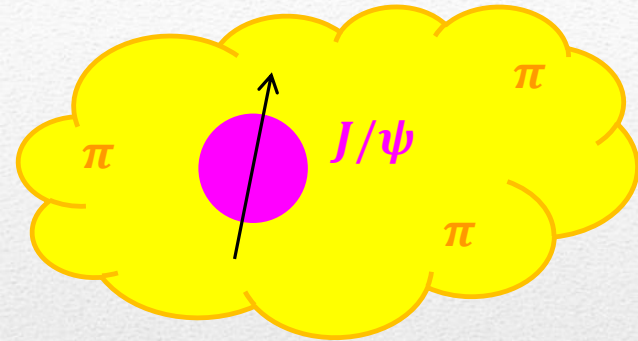


B decay mode	X decay mode	product branching fraction ( $\times 10^5$ )		$B_{fit}$	$R_{fit}$
$K^+ X$	$X \rightarrow \pi\pi J/\psi$	<b><math>0.86 \pm 0.08</math></b>	(BABAR <sup>[26]</sup> Belle <sup>[25]</sup> )	$0.081^{+0.019}_{-0.031}$	1
		$0.84 \pm 0.15 \pm 0.07$	BABAR <sup>[26]</sup>		
		$0.86 \pm 0.08 \pm 0.05$	Belle <sup>[25]</sup>		
$K^0 X$	$X \rightarrow \pi\pi J/\psi$	<b><math>0.41 \pm 0.11</math></b>	(BABAR <sup>[26]</sup> Belle <sup>[25]</sup> )		
		$0.35 \pm 0.19 \pm 0.04$	BABAR <sup>[26]</sup>		
		$0.43 \pm 0.12 \pm 0.04$	Belle <sup>[25]</sup>		
$(K^+\pi^-)_{NR} X$	$X \rightarrow \pi\pi J/\psi$	$0.81 \pm 0.20^{+0.11}_{-0.14}$	Belle <sup>[106]</sup>		
$K^{*0} X$	$X \rightarrow \pi\pi J/\psi$	$< 0.34$ , 90% C.L.	Belle <sup>[106]</sup>		
$K X$	$X \rightarrow \omega J/\psi$	$R = 0.8 \pm 0.3$	BABAR <sup>[33]</sup>	$0.061^{+0.024}_{-0.036}$	$0.77^{+0.28}_{-0.32}$
$K^+ X$		$0.6 \pm 0.2 \pm 0.1$	BABAR <sup>[33]</sup>		
$K^0 X$		$0.6 \pm 0.3 \pm 0.1$	BABAR <sup>[33]</sup>		
$K X$	$X \rightarrow \pi\pi\pi^0 J/\psi$	$R = 1.0 \pm 0.4 \pm 0.3$	Belle <sup>[32]</sup>		
$K^+ X$	$X \rightarrow D^{*0} \bar{D}^0$	<b><math>8.5 \pm 2.6</math></b>	(BABAR <sup>[38]</sup> Belle <sup>[37]</sup> )	$0.614^{+0.166}_{-0.074}$	$8.2^{+2.3}_{-2.8}$
		$16.7 \pm 3.6 \pm 4.7$	BABAR <sup>[38]</sup>		
		$7.7 \pm 1.6 \pm 1.0$	Belle <sup>[37]</sup>		
$K^0 X$	$X \rightarrow D^{*0} \bar{D}^0$	<b><math>12 \pm 4</math></b>	(BABAR <sup>[38]</sup> Belle <sup>[37]</sup> )		
		$22 \pm 10 \pm 4$	BABAR <sup>[38]</sup>		
		$9.7 \pm 4.6 \pm 1.3$	Belle <sup>[37]</sup>		
$K^+ X$	$X \rightarrow \gamma J/\psi$	<b><math>0.202 \pm 0.038</math></b>	(BABAR <sup>[35]</sup> Belle <sup>[34]</sup> )	$0.019^{+0.005}_{-0.009}$	$0.24^{+0.05}_{-0.06}$
$K^+ X$		$0.28 \pm 0.08 \pm 0.01$	BABAR <sup>[35]</sup>		
		$0.178^{+0.048}_{-0.044} \pm 0.012$	Belle <sup>[34]</sup>		
$K^0 X$		$0.26 \pm 0.18 \pm 0.02$	BABAR <sup>[35]</sup>		
		$0.124^{+0.076}_{-0.061} \pm 0.011$	Belle <sup>[34]</sup>		
$K^+ X$	$X \rightarrow \gamma\psi(2S)$	<b><math>0.44 \pm 0.12</math></b>	BABAR <sup>[35]</sup>	$0.04^{+0.015}_{-0.020}$	$0.51^{+0.13}_{-0.17}$
$K^+ X$		$0.95 \pm 0.27 \pm 0.06$	BABAR <sup>[35]</sup>		
		$0.083^{+0.198}_{-0.183} \pm 0.044$	Belle <sup>[34]</sup>		
		$R' = 2.46 \pm 0.64 \pm 0.29$	LHCb <sup>[36]</sup>		
$K^0 X$		$1.14 \pm 0.55 \pm 0.10$	BABAR <sup>[35]</sup>		
		$0.112^{+0.357}_{-0.290} \pm 0.057$	Belle <sup>[34]</sup>		
$K^+ X$	$X \rightarrow \gamma\chi_{c1}$	$< 9.6 \times 10^{-3}$	Belle <sup>[23]</sup>	$< 1.0 \times 10^{-3}$	$< 0.014$
$K^+ X$	$X \rightarrow \gamma\chi_{c2}$	$< 0.016$	Belle <sup>[23]</sup>	$< 1.7 \times 10^{-3}$	$< 0.024$
$K X$	$X \rightarrow \gamma\gamma$	$< 4.5 \times 10^{-3}$	Belle <sup>[111]</sup>	$< 4.7 \times 10^{-4}$	$< 6.6 \times 10^{-3}$
$K X$	$X \rightarrow \eta J/\psi$	$< 1.05$	BABAR <sup>[112]</sup>	$< 0.11$	$< 1.55$
$K^+ X$	$X \rightarrow p\bar{p}$	$< 9.6 \times 10^{-4}$	LHCb <sup>[110]</sup>	$< 1.6 \times 10^{-4}$	$< 2.2 \times 10^{-3}$



# Hadro-charmonium

Dubynskiy, Voloshin, PLB 666, 344  
Dubynskiy, Voloshin, PLB 671, 82  
Li, Voloshin, MPLA29, 1450060



Born in the context of QCD multipole expansion

$$H_{eff} = -\frac{1}{2} a_\psi E_i^a E_i^a$$
$$a_\psi = \langle \psi | (t_c^a - t_{\bar{c}}^a) r_i G r_i (t_c^a - t_{\bar{c}}^a) | \psi \rangle$$

the chromoelectric field interacts with soft light matter (highly excited light hadrons)

A bound state can occur via Van der Waals-like interactions

Expected to decay into core charmonium + light hadrons,  
Decay into open charm exponentially suppressed

# Charged Z states: $Z_c(3900)$ , $Z'_c(4020)$

Charged quarkonium-like resonances have been found, **4q needed**

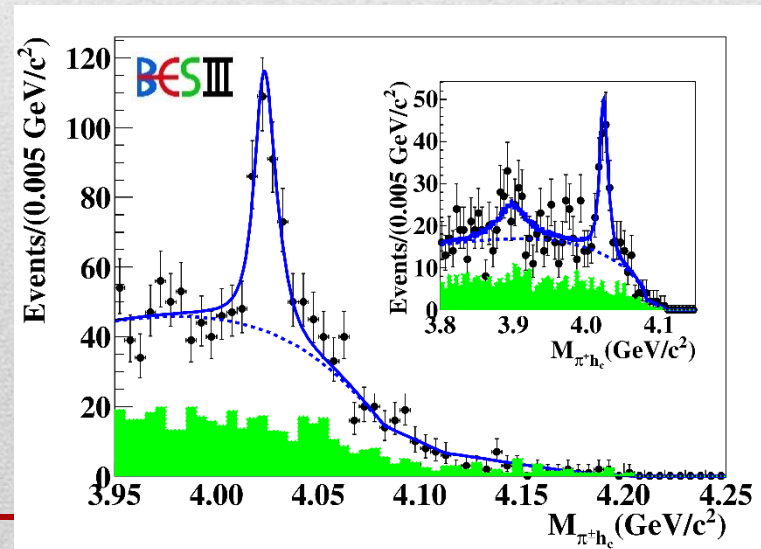
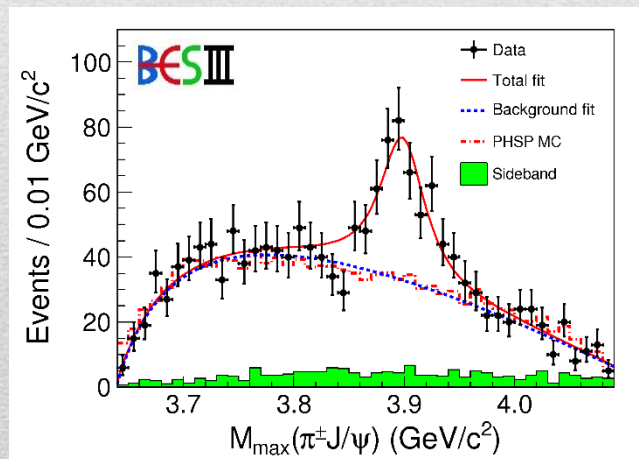
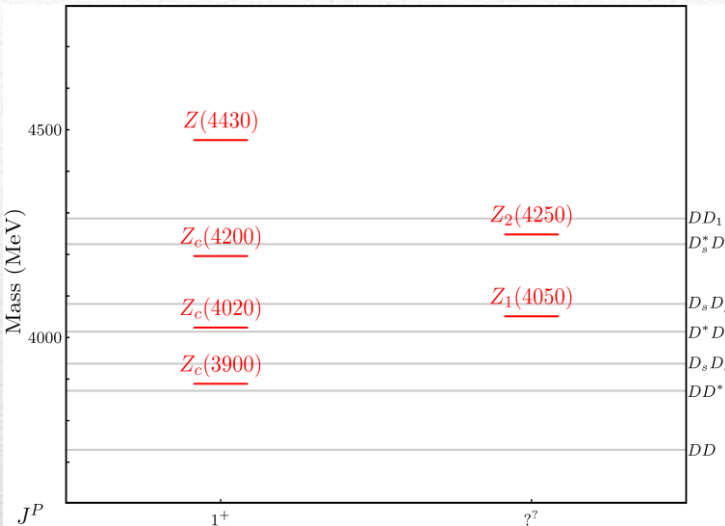
Two states  $J^{PC} = 1^{+-}$  appear  
slightly above  $D^{(*)}D^*$  thresholds

$$e^+e^- \rightarrow Z_c(3900)^+\pi^- \rightarrow J/\psi \pi^+\pi^- \text{ and } (DD^*)^+\pi^-$$

$$M = 3888.7 \pm 3.4 \text{ MeV}, \Gamma = 35 \pm 7 \text{ MeV}$$

$$e^+e^- \rightarrow Z'_c(4020)^+\pi^- \rightarrow h_c \pi^+\pi^- \text{ and } \bar{D}^{*0}D^{*+}\pi^-$$

$$M = 4023.9 \pm 2.4 \text{ MeV}, \Gamma = 10 \pm 6 \text{ MeV}$$





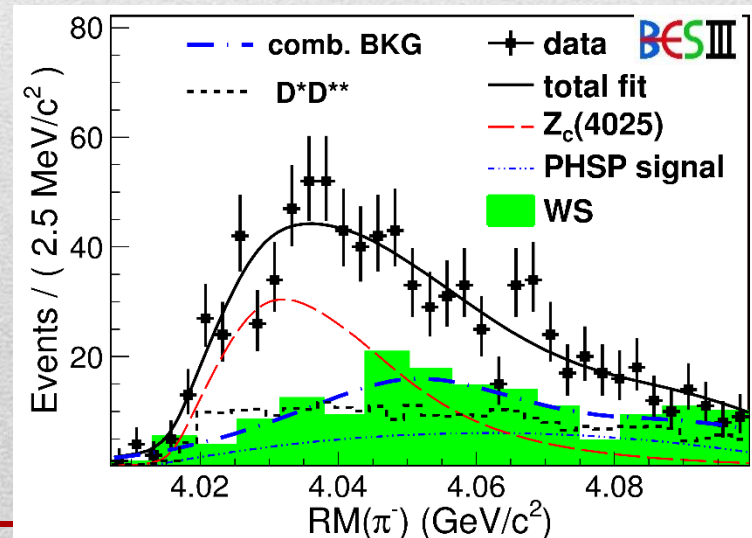
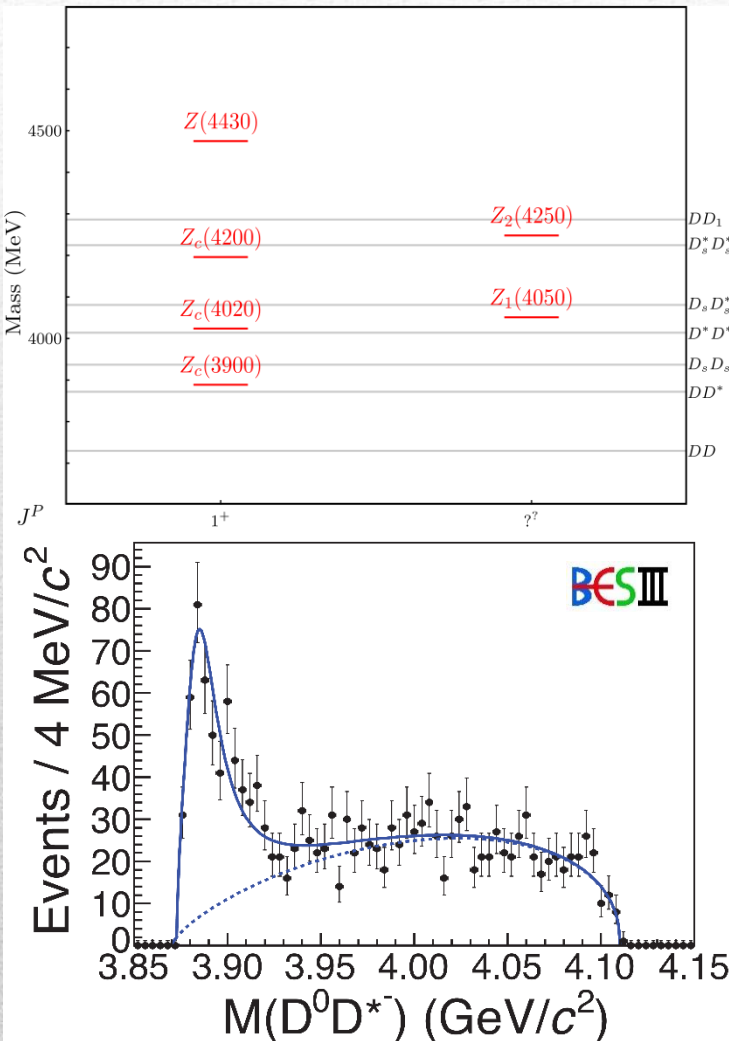
# Charged Z states: $Z_c(3900)$ , $Z'_c(4020)$

Charged quarkonium-like resonances have been found, **4q needed**

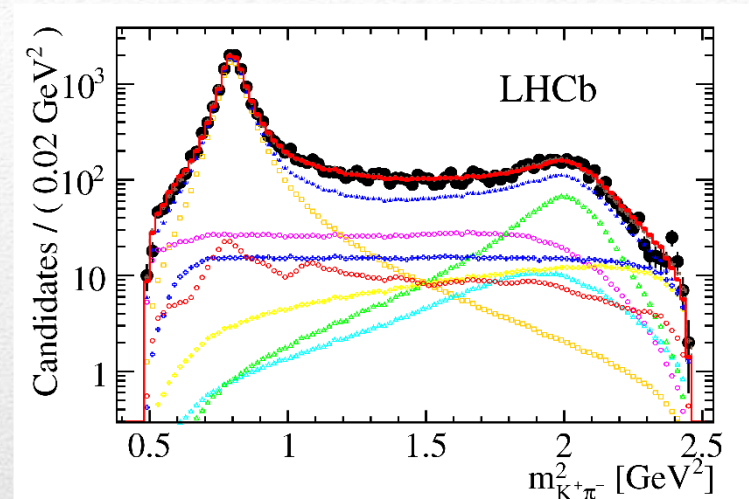
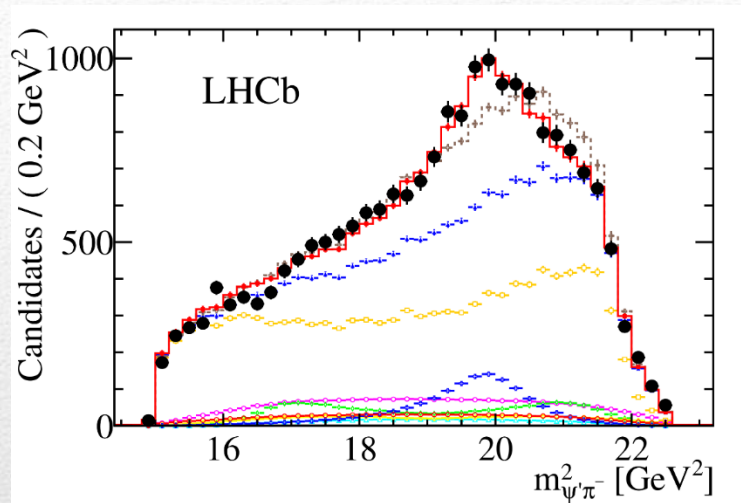
Two states  $J^{PC} = 1^{+-}$  appear  
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$e^+e^- \rightarrow Z_c(3900)^+\pi^- \rightarrow J/\psi \pi^+\pi^-$  and  $\rightarrow (DD^*)^+\pi^-$   
 $M = 3888.7 \pm 3.4 \text{ MeV}, \Gamma = 35 \pm 7 \text{ MeV}$

$e^+e^- \rightarrow Z'_c(4020)^+\pi^- \rightarrow h_c \pi^+\pi^-$  and  $\rightarrow \bar{D}^{*0}D^{*+}\pi^-$   
 $M = 4023.9 \pm 2.4 \text{ MeV}, \Gamma = 10 \pm 6 \text{ MeV}$



# Charged Z states: Z(4430)



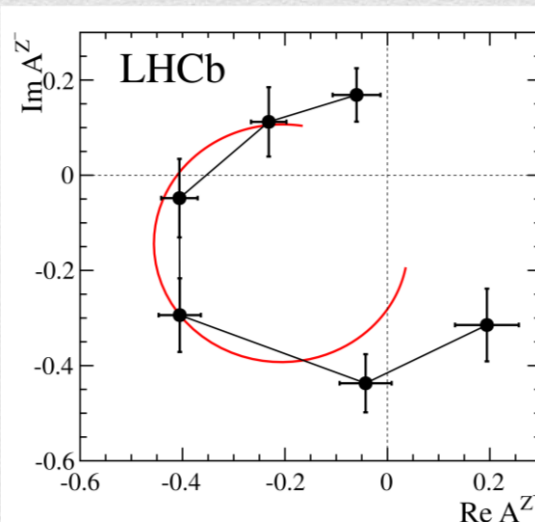
$$Z(4430)^+ \rightarrow \psi(2S) \pi^+$$

$$I^G J^{PC} = 1^+ 1^{+-}$$

$$M = 4475 \pm 7_{-25}^{+15} \text{ MeV}$$

$$\Gamma = 172 \pm 13_{-34}^{+37} \text{ MeV}$$

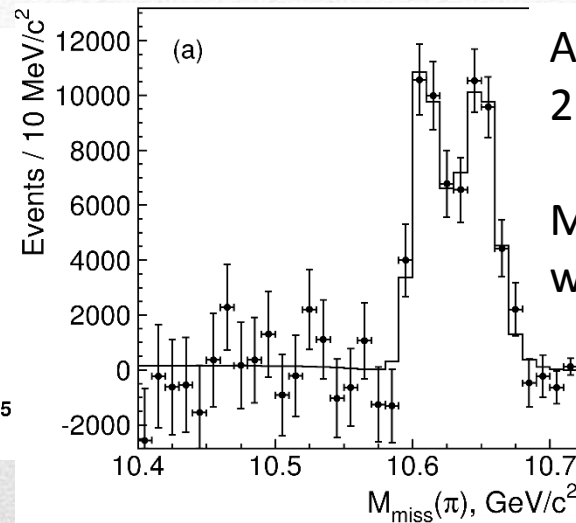
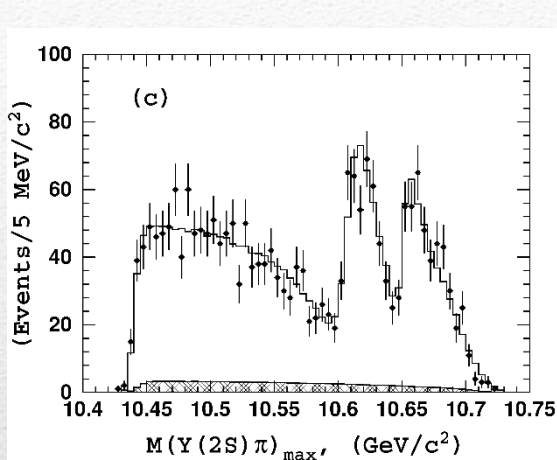
Far from open charm thresholds



If the amplitude is a free complex number, in each bin of  $m_{\psi'\pi^-}^2$ , the resonant behaviour appears as well



# Charged Z states: $Z_b(106010)$ , $Z'_b(10650)$



Anomalous dipion width in  $\Upsilon(5S)$ ,  
2 orders of magnitude larger than  $\Upsilon(nS)$

Moreover, observed  $\Upsilon(5S) \rightarrow h_b(nP)\pi\pi$   
which violates HQSS

2 twin resonances!

$$\Upsilon(5S) \rightarrow Z_b(10610)^+\pi^- \rightarrow \Upsilon(nS)\pi^+\pi^-, h_b(nP)\pi^+\pi^-$$

$$\text{and } \rightarrow (BB^*)^+\pi^-$$

$$M = 10607.2 \pm 2.0 \text{ MeV}, \Gamma = 18.4 \pm 2.4 \text{ MeV}$$

$$\Upsilon(5S) \rightarrow Z'_b(10650)^+\pi^- \rightarrow \Upsilon(nS)\pi^+\pi^-, h_b(nP)\pi^+\pi^-$$

$$\text{and } \rightarrow \bar{B}^{*0}B^{*+}\pi^-$$

$$M = 10652.2 \pm 1.5 \text{ MeV}, \Gamma = 11.5 \pm 2.2 \text{ MeV}$$

State	$M$ (MeV)	$\Gamma$ (MeV)	$J^{PC}$	Process (mode)	Experiment ( $\#\sigma$ )
$X(3823)$	$3823.1 \pm 1.9$	$< 24$	$?^{-}$	$B \rightarrow K(\chi_{c1}\gamma)$	Belle <sup>[23]</sup> (4.0)
$X(3872)$	$3871.68 \pm 0.17$	$< 1.2$	$1^{++}$	$B \rightarrow K(\pi^+\pi^-J/\psi)$	Belle <sup>[24,25]</sup> ( $>10$ ), BABAR <sup>[26]</sup> (8.6)
				$p\bar{p} \rightarrow (\pi^+\pi^-J/\psi) \dots$	CDR <sup>[27,28]</sup> (11.6), D0 <sup>[29]</sup> (5.2)
				$pp \rightarrow (\pi^+\pi^-J/\psi) \dots$	LHCb <sup>[30,31]</sup> (np)
				$B \rightarrow K(\pi^+\pi^-\pi^0J/\psi)$	Belle <sup>[32]</sup> (4.3), BABAR <sup>[33]</sup> (4.0)
				$B \rightarrow K(\gamma J/\psi)$	Belle <sup>[34]</sup> (5.5), BABAR <sup>[35]</sup> (3.5)
					LHCb <sup>[36]</sup> ( $>10$ )
				$B \rightarrow K(\gamma\psi(2S))$	BABAR <sup>[35]</sup> (3.6), Belle <sup>[34]</sup> (0.2)
					LHCb <sup>[36]</sup> (4.4)
				$B \rightarrow K(D\bar{D}^*)$	Belle <sup>[37]</sup> (6.4), BABAR <sup>[38]</sup> (4.9)
$Z_c(3900)^+$	$3888.7 \pm 3.4$	$35 \pm 7$	$1^{+-}$	$Y(4260) \rightarrow \pi^-(D\bar{D}^*)^+$	BES III <sup>[39]</sup> (np)
				$Y(4260) \rightarrow \pi^-(\pi^+J/\psi)$	BES III <sup>[40]</sup> (8), Belle <sup>[41]</sup> (5.2)
					CLEO data <sup>[42]</sup> ( $>5$ )
$Z_c(4020)^+$	$4023.9 \pm 2.4$	$10 \pm 6$	$1^{+-}$	$Y(4260) \rightarrow \pi^-(\pi^+h_c)$	BES III <sup>[43]</sup> (8.9)
				$Y(4260) \rightarrow \pi^-(D^*\bar{D}^*)^+$	BES III <sup>[44]</sup> (10)
$Y(3915)$	$3918.4 \pm 1.9$	$20 \pm 5$	$0^{++}$	$B \rightarrow K(\omega J/\psi)$	Belle <sup>[45]</sup> (8), BABAR <sup>[33,46]</sup> (19)
				$e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle <sup>[47]</sup> (7.7), BABAR <sup>[48]</sup> (7.6)
$Z(3930)$	$3927.2 \pm 2.6$	$24 \pm 6$	$2^{++}$	$e^+e^- \rightarrow e^+e^-(D\bar{D})$	Belle <sup>[49]</sup> (5.3), BABAR <sup>[50]</sup> (5.8)
$X(3940)$	$3942^{+9}_{-8}$	$37^{+27}_{-17}$	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D\bar{D}^*)$	Belle <sup>[51,52]</sup> (6)
$Y(4008)$	$3891 \pm 42$	$255 \pm 42$	$1^{--}$	$e^+e^- \rightarrow (\pi^+\pi^-J/\psi)$	Belle <sup>[41,53]</sup> (7.4)
$Z(4050)^+$	$4051^{+24}_{-43}$	$82^{+51}_{-55}$	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+\chi_{c1})$	Belle <sup>[54]</sup> (5.0), BABAR <sup>[55]</sup> (1.1)
$Y(4140)$	$4145.6 \pm 3.6$	$14.3 \pm 5.9$	$?^{?+}$	$B^+ \rightarrow K^+(\phi J/\psi)$	CDR <sup>[56,57]</sup> (5.0), Belle <sup>[58]</sup> (1.9), LHCb <sup>[59]</sup> (1.4), CMS <sup>[60]</sup> ( $>5$ ) D0 <sup>[61]</sup> (3.1)
$X(4160)$	$4156^{+29}_{-25}$	$139^{+113}_{-65}$	$?^{?+}$	$e^+e^- \rightarrow J/\psi(D^*\bar{D}^*)$	Belle <sup>[52]</sup> (5.5)
$Z(4200)^+$	$4196^{+35}_{-30}$	$370^{+99}_{-110}$	$1^{+-}$	$\bar{B}^0 \rightarrow K^-(\pi^+J/\psi)$	Belle <sup>[62]</sup> (7.2)

State	$M$ (MeV)	$\Gamma$ (MeV)	$J^{PC}$	Process (mode)	Experiment ( $\#\sigma$ )
$Y(4220)$	$4196^{+35}_{-30}$	$39 \pm 32$	$1^{--}$	$e^+e^- \rightarrow (\pi^+\pi^-h_c)$	BES III data <sup>[63,64]</sup> (4.5)
$Y(4230)$	$4230 \pm 8$	$38 \pm 12$	$1^{--}$	$e^+e^- \rightarrow (\chi_{c0}\omega)$	BES II <sup>[65]</sup> ( $>9$ )
$Z(4250)^+$	$4248^{+185}_{-45}$	$177^{+321}_{-72}$	$?^{?+}$	$\bar{B}^0 \rightarrow K^-(\pi^+\chi_{c1})$	Belle <sup>[54]</sup> (5.0), BABAR <sup>[55]</sup> (2.0)
$Y(4260)$	$4250 \pm 9$	$108 \pm 12$	$1^{--}$	$e^+e^- \rightarrow (\pi\pi J/\psi)$	BABAR <sup>[66,67]</sup> (8), CLEO <sup>[68,69]</sup> (11) Belle <sup>[41,53]</sup> (15), BES III <sup>[40]</sup> (np)
				$e^+e^- \rightarrow (f_0(980)J/\psi)$	BABAR <sup>[67]</sup> (np), Belle <sup>[41]</sup> (np)
				$e^+e^- \rightarrow (\pi^-Z_c(3900)^+)$	BES III <sup>[40]</sup> (8), Belle <sup>[41]</sup> (5.2)
				$e^+e^- \rightarrow (\gamma X(3872))$	BES II <sup>[70]</sup> (5.3)
$Y(4290)$	$4293 \pm 9$	$222 \pm 67$	$1^{--}$	$e^+e^- \rightarrow (\pi^+\pi^-h_c)$	BES III data <sup>[63,64]</sup> (np)
$X(4350)$	$4350.6^{+4.6}_{-5.1}$	$13^{+18}_{-10}$	$0/2^{?+}$	$e^+e^- \rightarrow e^+e^-(\phi J/\psi)$	Belle <sup>[58]</sup> (3.2)
$Y(4360)$	$4354 \pm 11$	$78 \pm 16$	$1^{--}$	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	Belle <sup>[71]</sup> (8), BABAR <sup>[72]</sup> (np)
$Z(4430)^+$	$4478 \pm 17$	$180 \pm 31$	$1^{+-}$	$\bar{B}^0 \rightarrow K^-(\pi^+\psi(2S))$	Belle <sup>[73,74]</sup> (6.4), BABAR <sup>[75]</sup> (2.4) LHCb <sup>[76]</sup> (13.9)
				$\bar{B}^0 \rightarrow K^-(\pi^+J/\psi)$	Belle <sup>[62]</sup> (4.0)
$Y(4630)$	$4634^{+9}_{-11}$	$92^{+41}_{-32}$	$1^{--}$	$e^+e^- \rightarrow (\Lambda_c^+\bar{\Lambda}_c^-)$	Belle <sup>[77]</sup> (8.2)
$Y(4660)$	$4665 \pm 10$	$53 \pm 14$	$1^{--}$	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	Belle <sup>[71]</sup> (5.8), BABAR <sup>[72]</sup> (5)
$Z_b(10610)^+$	$10607.2 \pm 2.0$	$18.4 \pm 2.4$	$1^{+-}$	$\Upsilon(5S) \rightarrow \pi(\pi\Upsilon(nS))$	Belle <sup>[78,79]</sup> ( $>10$ )
				$\Upsilon(5S) \rightarrow \pi^-(\pi^+h_b(nP))$	Belle <sup>[78]</sup> (16)
				$\Upsilon(5S) \rightarrow \pi^-(B\bar{B}^*)^+$	Belle <sup>[80]</sup> (8)
$Z_b(10650)^+$	$10652.2 \pm 1.5$	$11.5 \pm 2.2$	$1^{+-}$	$\Upsilon(5S) \rightarrow \pi^-(\pi^+\Upsilon(nS))$	Belle <sup>[78]</sup> ( $>10$ )
				$\Upsilon(5S) \rightarrow \pi^-(\pi^+h_b(nP))$	Belle <sup>[78]</sup> (16)
				$\Upsilon(5S) \rightarrow \pi^-(B^*\bar{B}^*)^+$	Belle <sup>[80]</sup> (6.8)

Guerrieri, AP, Piccinini, Polosa,  
IJMPA 30, 1530002



# $Z_c(3900) \rightarrow \eta_c \rho$

Esposito, Guerrieri, AP, PLB 746, 194-201

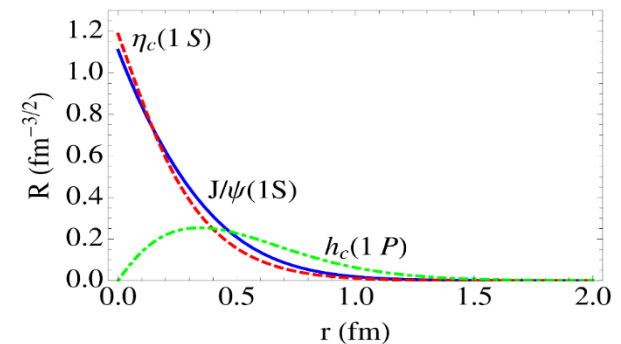
If tetraquark

Kinematics with HQSS, dynamics estimated according to Brodsky et al., PRL113, 112001

$$A = \langle \chi_{c\bar{c}} | \chi_c \otimes \chi_{\bar{c}} \rangle \langle \phi_{c\bar{c}} | \hat{T}_{\perp HQS} | \phi[cq][\bar{c}\bar{q}] \rangle + O\left(\frac{\Lambda_{QCD}}{m_c}\right)$$

Clebsch-Gordan

Uncertainty  
 $\sim 25\%$



Reduced matrix element

- approximated as a constant
- or  $\propto \psi_{c\bar{c}}(r_Z)$

	Kinematics only		Dynamics included	
	type I	type II	type I	type II
$\frac{\mathcal{BR}(Z_c \rightarrow \eta_c \rho)}{\mathcal{BR}(Z_c \rightarrow J/\psi \pi)}$	$(3.3^{+7.9}_{-1.4}) \times 10^2$	$0.41^{+0.96}_{-0.17}$	$(2.3^{+3.3}_{-1.4}) \times 10^2$	$0.27^{+0.40}_{-0.17}$
$\frac{\mathcal{BR}(Z'_c \rightarrow \eta_c \rho)}{\mathcal{BR}(Z'_c \rightarrow h_c \pi)}$	$(1.2^{+2.8}_{-0.5}) \times 10^2$		$6.6^{+56.8}_{-5.8}$	

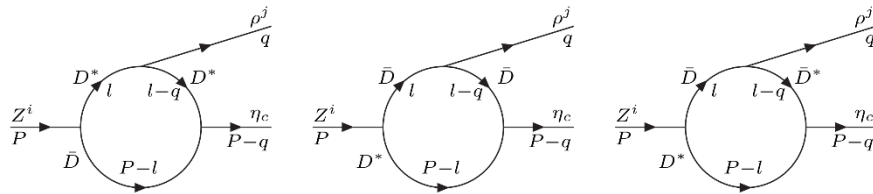
$$Z_c(3900) \rightarrow \eta_c \rho$$

Esposito, Guerrieri, AP, PLB 746, 194-201

If molecule

Non-Relativistic Effective Theory, HQET+NRQCD and Hidden gauge Lagrangian

Uncertainty estimated with power counting at NLO



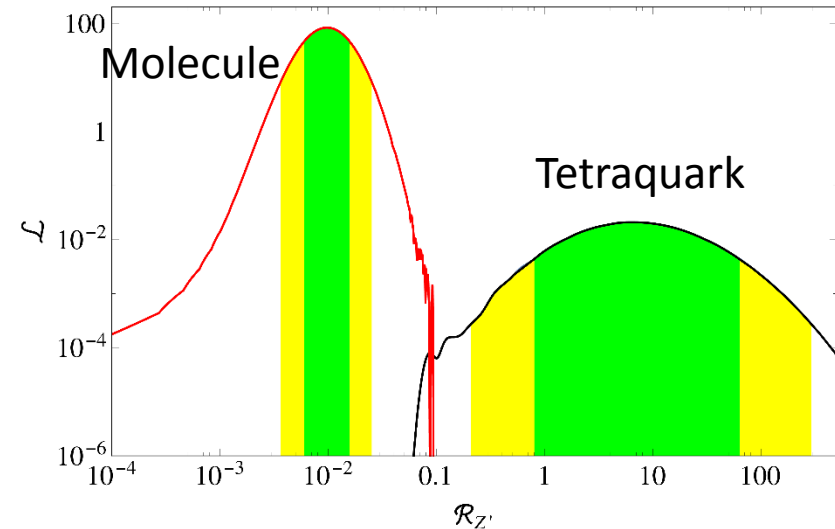
$$\mathcal{L}_{Z_c^{(\prime)}} = \frac{z^{(\prime)}}{2} \langle \mathcal{Z}_{\mu,ab}^{(\prime)} \bar{H}_{2b} \gamma^\mu \bar{H}_{1a} \rangle + h.c.,$$

$$\mathcal{L}_{c\bar{c}} = \frac{g_2}{2} \langle \bar{\Psi} H_{1a} \overleftrightarrow{\not{D}} H_{2a} \rangle + \frac{g_1}{2} \langle \bar{\chi}_\mu H_{1a} \gamma^\mu H_{2a} \rangle + h.c.,$$

$$\mathcal{L}_{\rho DD^*} = i\beta \langle H_{1b} v^\mu (\mathcal{V}_\mu - \rho_\mu)_{ba} \bar{H}_{1a} \rangle + i\lambda \langle H_{1b} \sigma^{\mu\nu} F_{\mu\nu}(\rho)_{ba} \bar{H}_{1a} \rangle + h.c.,$$

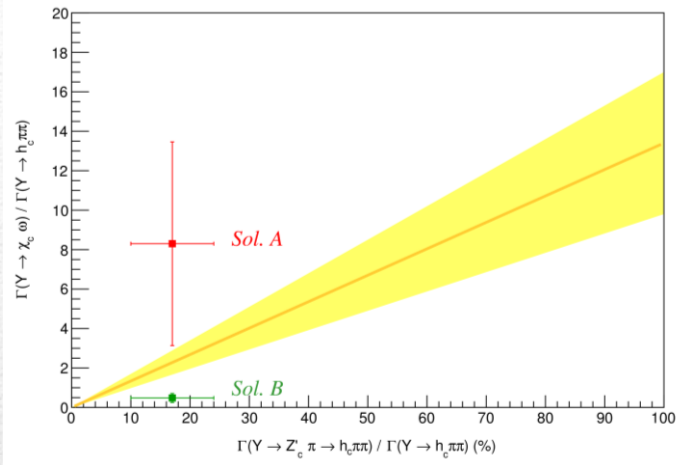
$$\frac{\mathcal{BR}(Z_c \rightarrow \eta_c \rho)}{\mathcal{BR}(Z_c \rightarrow J/\psi \pi)} = (4.6_{-1.7}^{+2.5}) \times 10^{-2}; \quad \frac{\mathcal{BR}(Z'_c \rightarrow \eta_c \rho)}{\mathcal{BR}(Z'_c \rightarrow h_c \pi)} = (1.0_{-0.4}^{+0.6}) \times 10^{-2}.$$

$$\frac{\mathcal{BR}(Z_c \rightarrow h_c \pi)}{\mathcal{BR}(Z'_c \rightarrow h_c \pi)} = 0.34_{-0.13}^{+0.21}; \quad \frac{\mathcal{BR}(Z_c \rightarrow J/\psi \pi)}{\mathcal{BR}(Z'_c \rightarrow J/\psi \pi)} = 0.35_{-0.21}^{+0.49}$$





# Tetraquark: the $Y(4220)$



$$\langle \chi_{c0}(p) \omega(\eta, q) | Y(\lambda, P) \rangle = g_\chi \eta \cdot \lambda,$$

$$\langle Z'_c(\eta, q) \pi(p) | Y(\lambda, P) \rangle = g_Z \eta \cdot \lambda \frac{P \cdot p}{f_\pi M_Y},$$

$$\langle h_c(\eta, q) \sigma(p) | Y(\lambda, P) \rangle = g_h \varepsilon_{\mu\nu\rho\sigma} \eta^\mu \lambda^\nu \frac{P^\rho q^\sigma}{P \cdot q},$$

$$\langle \pi(q) \pi(p) | \sigma(P) \rangle = \frac{P^2}{2f_\pi},$$

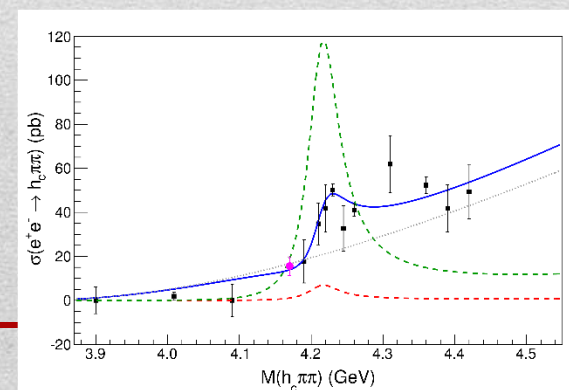
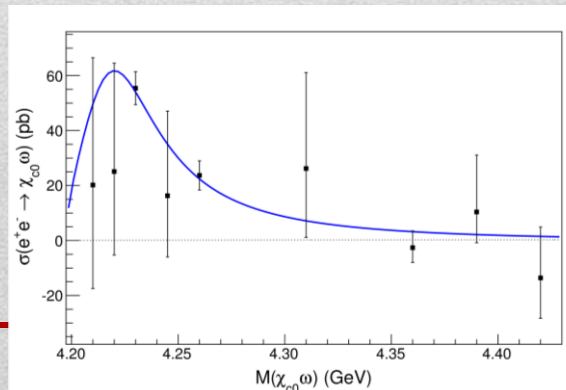
$$\frac{\Gamma(Y(4220) \rightarrow \chi_{c0} \omega)}{\Gamma(Y(4220) \rightarrow h_c \pi^+ \pi^-)} = (13.4 \pm 3.6) \times R_{YZ} = 2.3 \pm 1.2.$$

$$\frac{\Gamma(Y(4220) \rightarrow Z'_c{}^\pm \pi^\mp \rightarrow h_c \pi^+ \pi^-)}{\Gamma(Y(4220) \rightarrow h_c \sigma \rightarrow h_c \pi^+ \pi^-)} = 4.8 \pm 3.5,$$

A state apparently breaking HQSS has been observed

Compatible to be the  $Y_3$  state

Faccini, Filaci, Guerrieri, AP,  
Polosa, PRD 91, 117501



# Tetraquark: the $b$ sector

Ali, Maiani, Piccinini, Polosa, Riquer PRD91 017502

$$\begin{aligned}M(Z'_b) - M(Z_b) &= 2\kappa_b \\M(Z'_c) - M(Z_c) &= 2\kappa_c \sim 120 \text{ MeV} \\ \kappa_b : \kappa_c &= M_c : M_b \sim 0.30\end{aligned}$$

$$2\kappa_b \sim 36 \text{ MeV, vs. } 45 \text{ MeV (exp.)}$$

$$\begin{aligned}Z_b &= \frac{\alpha |1_{q\bar{q}}0_{b\bar{b}}\rangle - \beta |0_{q\bar{q}}1_{b\bar{b}}\rangle}{\sqrt{2}} \\ Z'_b &= \frac{\alpha |1_{q\bar{q}}0_{b\bar{b}}\rangle + \beta |0_{q\bar{q}}1_{b\bar{b}}\rangle}{\sqrt{2}}\end{aligned}$$

Data on  $\Upsilon(5S) \rightarrow \Upsilon(nS)\pi\pi$  and  $\Upsilon(5S) \rightarrow h_b(nP)\pi\pi$  strongly favor  $\alpha = \beta$

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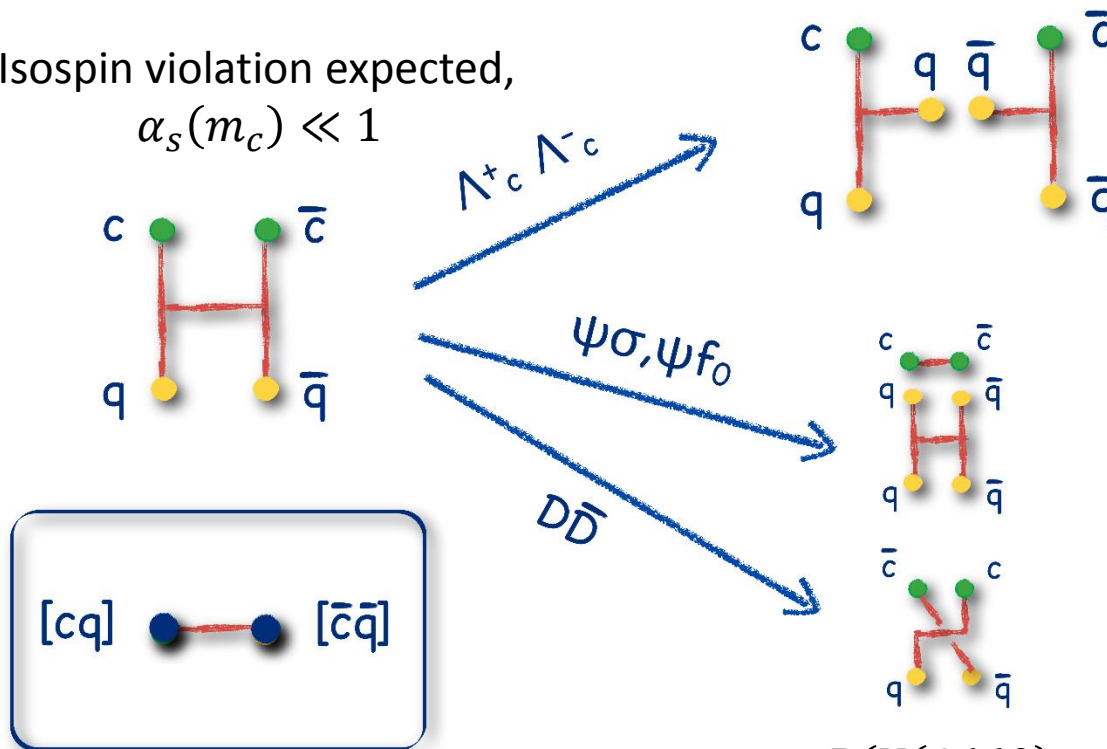


# Baryonium

C. Sabelli

a structure  $[cq][\bar{c}\bar{q}]$  can explain the dominance of baryon channel

Isospin violation expected,  
 $\alpha_s(m_c) \ll 1$



Rossi, Veneziano,  
 NPB 123, 507;  
 Phys.Rept. 63, 149;  
 PLB70, 255

$$\frac{B(Y(4660) \rightarrow \Lambda_c^+ \Lambda_c^-)}{B(Y(4660) \rightarrow \psi(2S)\pi\pi)} = 25 \pm 7$$

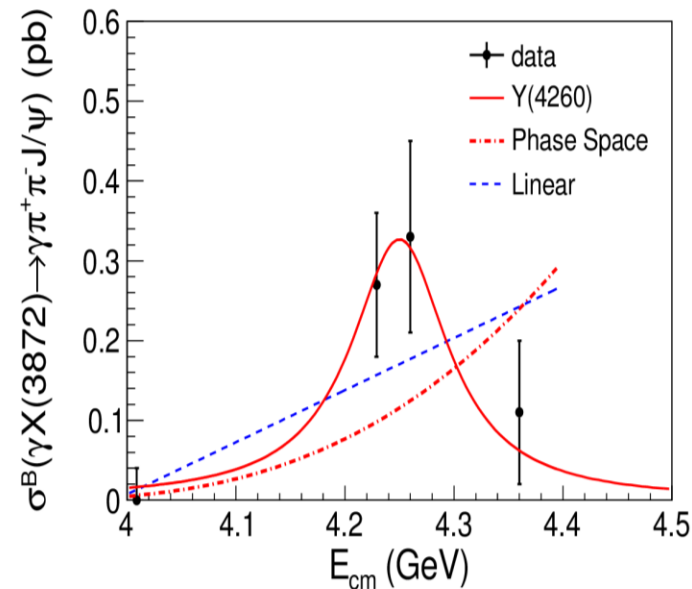
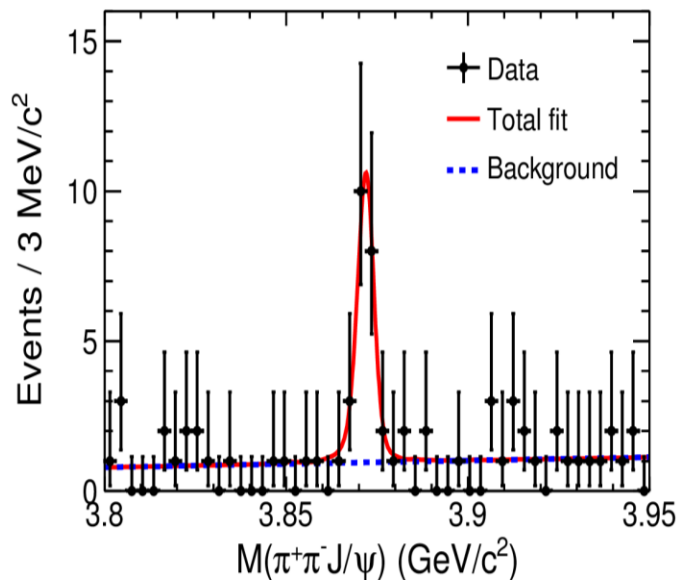
Cotugno, Faccini, Polosa, Sabelli,  
 PRL 104, 132005

# $Y(4260) \rightarrow \gamma X(3872)$

M. Ablikim et al., Phys. Rev. Lett. 112 (2014) 092001

F. Piccinini

BESIII:  $e^+e^- \rightarrow Y(4260) \rightarrow X(3872)\gamma$



With  $\mathcal{B}[X(3872) \rightarrow \pi^+\pi^-J/\psi] = 5\%$

$$\frac{\mathcal{B}[Y(4260) \rightarrow \gamma X(3872)]}{\mathcal{B}(Y(4260) \rightarrow \pi^+\pi^-J/\psi)} = 0.1$$

Strong indication that  $Y(4260)$  and  $X(3872)$  share a similar structure

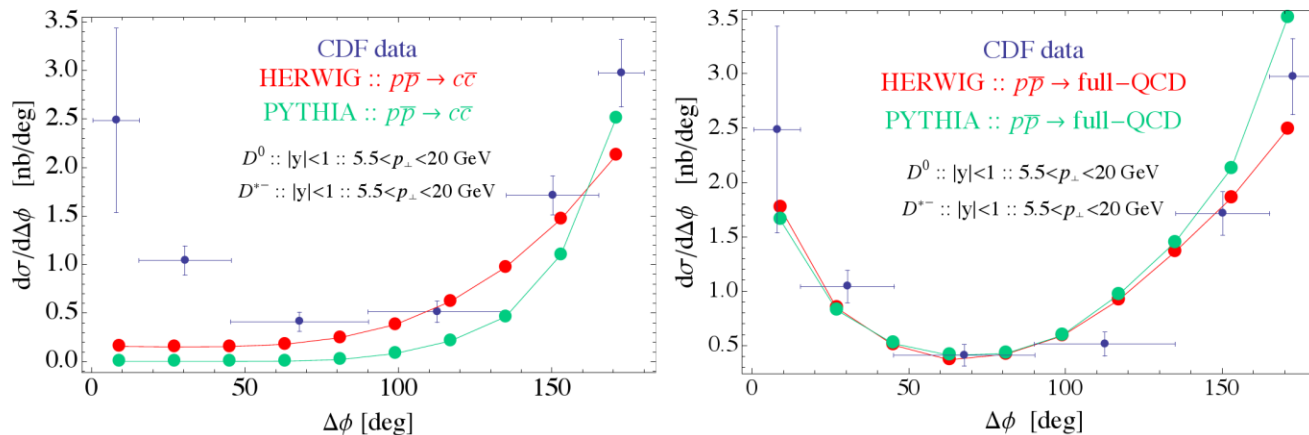


# Tuning of MC

## Monte Carlo simulations

A. Esposito

- We compare the  $D^0 D^{*-}$  pairs produced as a function of relative azimuthal angle with the results from CDF:



*The c-cbar run underestimate the low angles (low- $k_T$ ) region!*

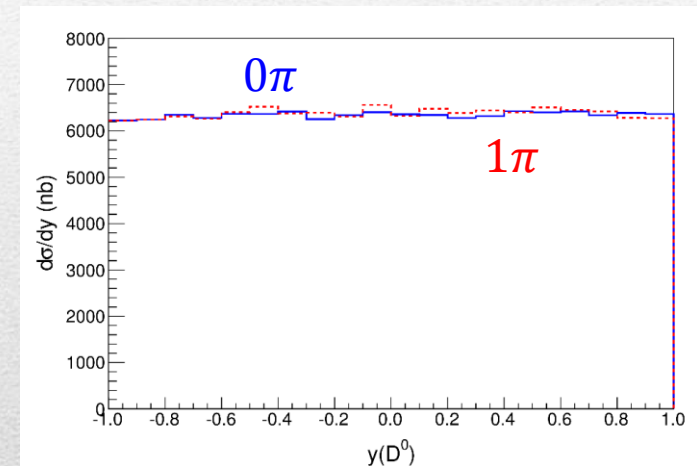
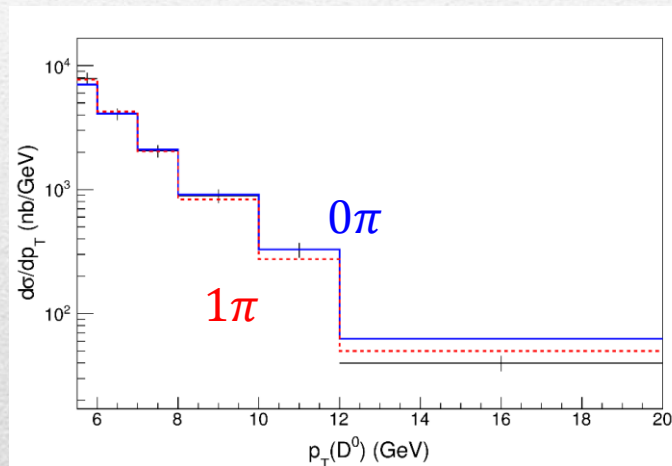
Such distributions of charm mesons are available at Tevatron  
No distribution has been published (yet) at LHC

# Tuning pions

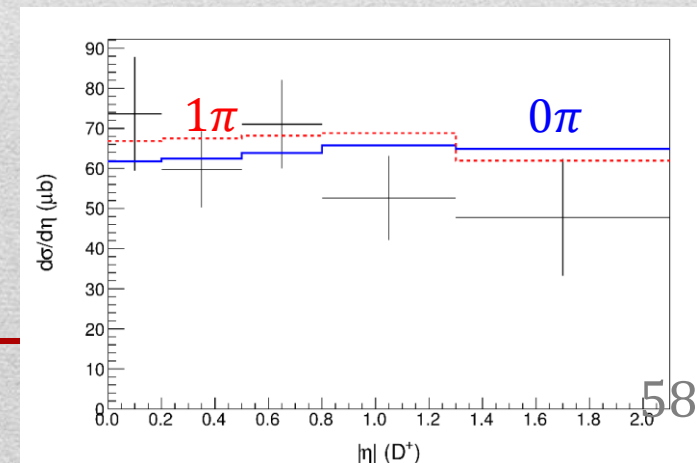
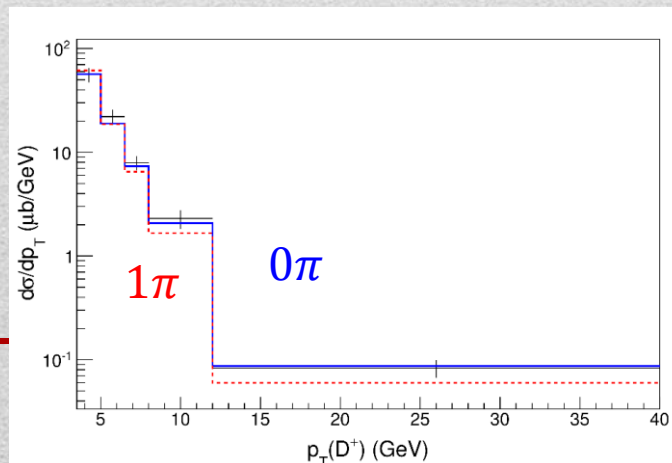
This picture could spoil existing meson distributions used to tune MC  
We verify this is not the case up to an overall  $K$  factor

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

Neither at CDF...

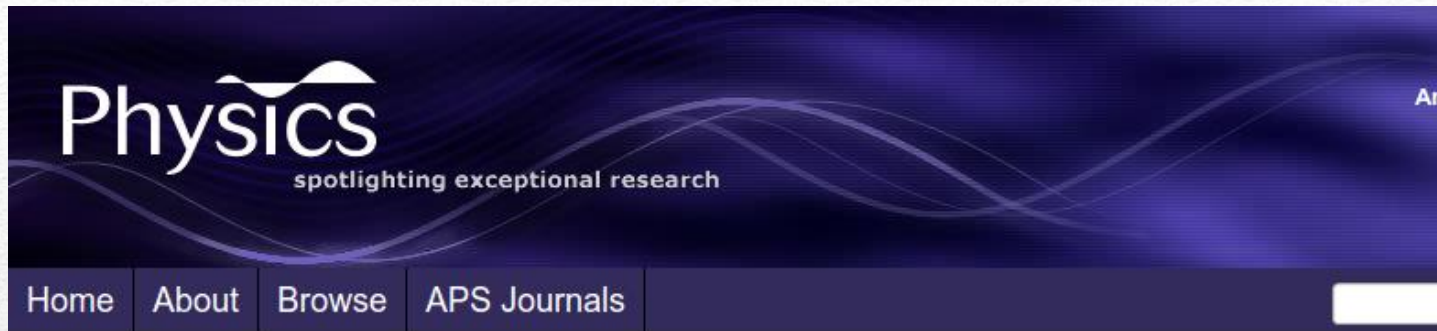


...nor at ATLAS





$$Z_c(3900)$$



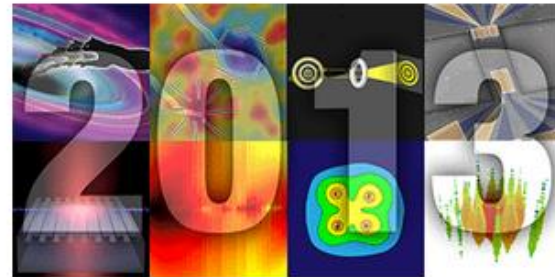
## Notes from the Editors: Highlights of the Year

Published December 30, 2013 | Physics 6, 139 (2013) | DOI: 10.1103/Physics.6.139

### **Physics looks back at the standout stories of 2013.**

As 2013 draws to a close, we look back on the research covered in *Physics* that really made waves in and beyond the physics community. In thinking about which stories to highlight, we considered a combination of factors: popularity on the website, a clear element of surprise or discovery, or signs that the work could lead to better technology. On behalf of the *Physics* staff, we wish everyone an excellent New Year.

— Matteo Rini and Jessica Thomas



Images from popular *Physics* stories in 2013.

### **Four-Quark Matter**

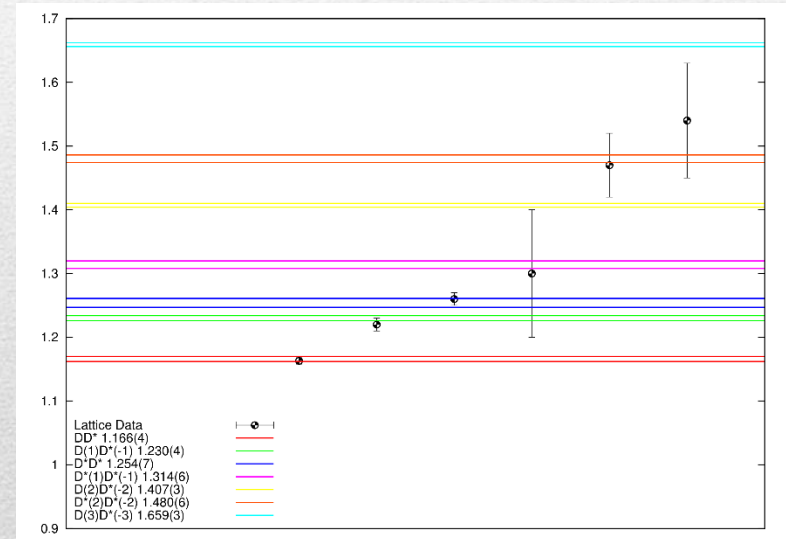
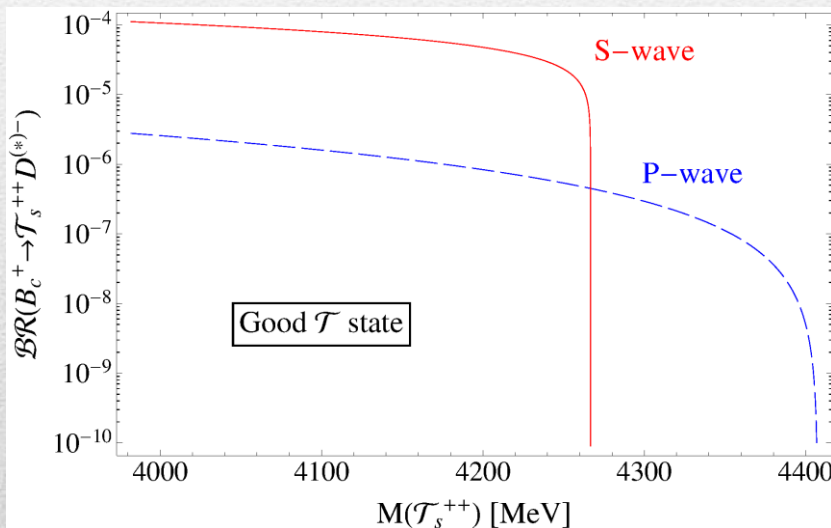
Quarks come in twos and threes—or so nearly every experiment has told us. This summer, the BESIII Collaboration in China and the Belle Collaboration in Japan reported they had sorted through the debris of high-energy electron-positron collisions and seen a **mysterious particle** that appeared to contain four quarks. Though other explanations for the nature of the particle, dubbed  $Z_c(3900)$ , are possible, the “tetraquark” interpretation may be gaining traction: BESIII has since **seen** a series of other particles that appear to contain four quarks.

mysterious particle

# Doubly charmed states

For example, we proposed to look for **doubly charmed states**, which in tetraquark model are  $[cc]_{S=1}[\bar{q}\bar{q}]_{S=0,1}$

These states could be observed in  **$B_c$  decays** @LHC and sought on the lattice  
Esposito, Papinutto, AP, Polosa, Tantalò, PRD88 (2013) 054029

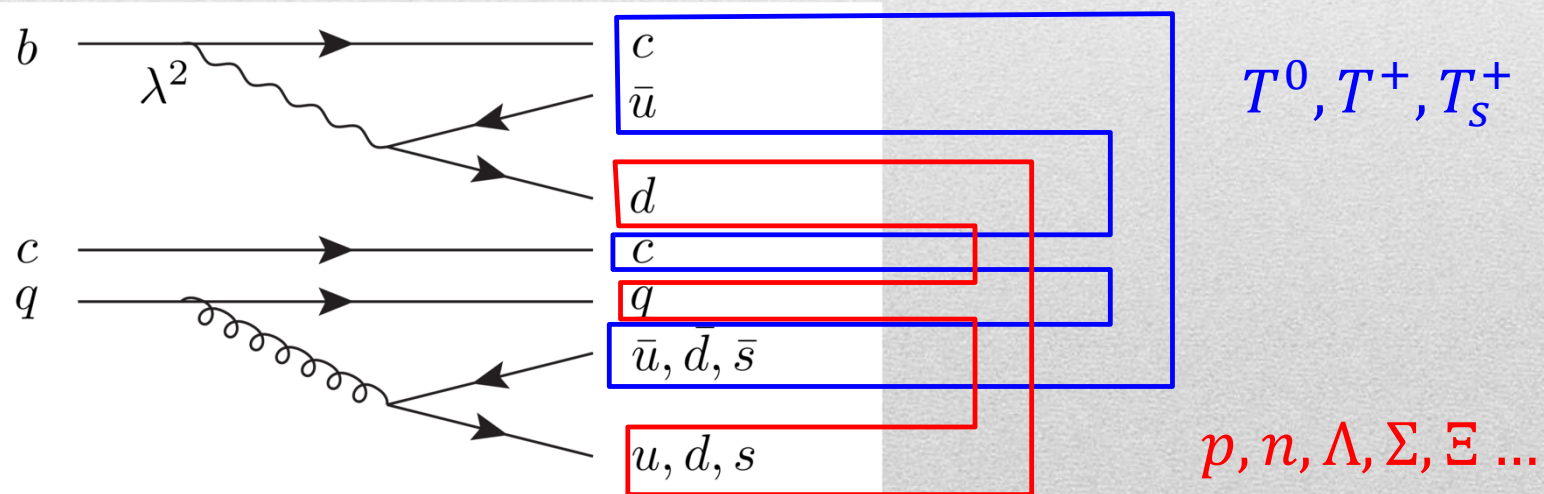
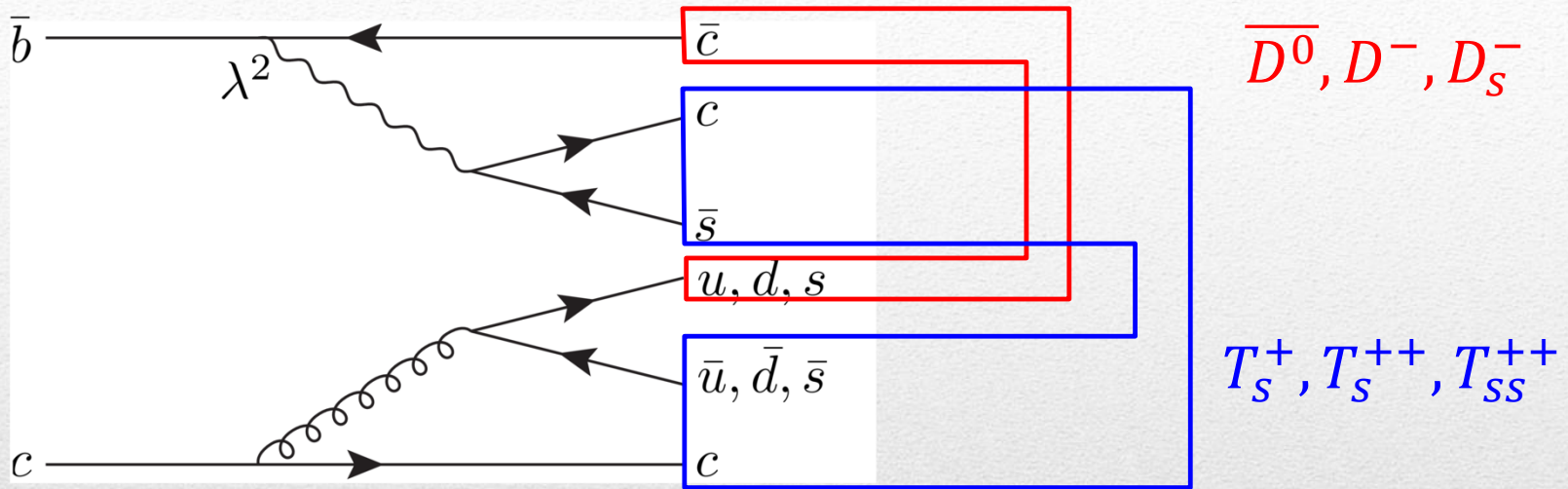


Preliminary results on spectrum for  $m_\pi = 490$  MeV,  $32^3 \times 64$  lattice,  $a = 0.075$  fm

Guerrieri, Papinutto, AP, Polosa, Tantalò, PoS LATTICE2014 106



# $T$ states production



# Prompt production of $X(3872)$

$X(3872)$  is the Queen of exotic resonances, the most popular interpretation is a  $D^0\bar{D}^{0*}$  **molecule** (bound state, pole in the 1<sup>st</sup> Riemann sheet?)

We aim to evaluate prompt production cross section at hadron colliders via Monte-Carlo simulations

**Q.** What is a molecule in MC? **A.** «Coalescence» model



$$\sigma(p\bar{p} \rightarrow X(3872)) \sim \int d^3k |\langle X | D\bar{D}^* \rangle \langle D\bar{D}^* | p\bar{p} \rangle|^2 < \int_{k < k_{max}} d^3k |\langle D\bar{D}^* | p\bar{p} \rangle|^2$$

This should provide an upper bound for the cross section



# Estimating $k_{max}$

The binding energy is  $E_B \approx -0.16 \pm 0.31$  MeV: **very small!**

In a simple square well model this corresponds to:

$$\sqrt{\langle k^2 \rangle} \approx 50 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 10 \text{ fm}$$

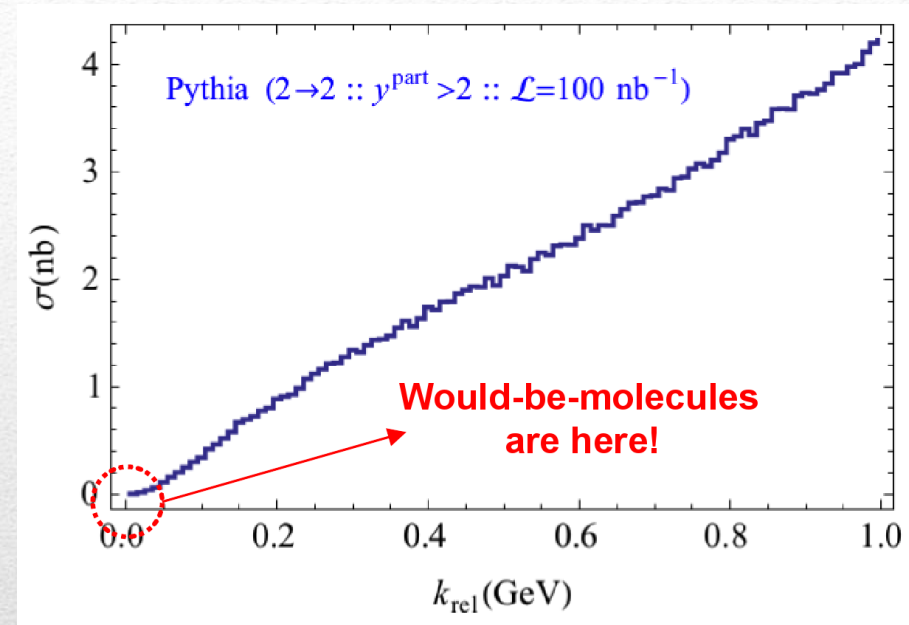
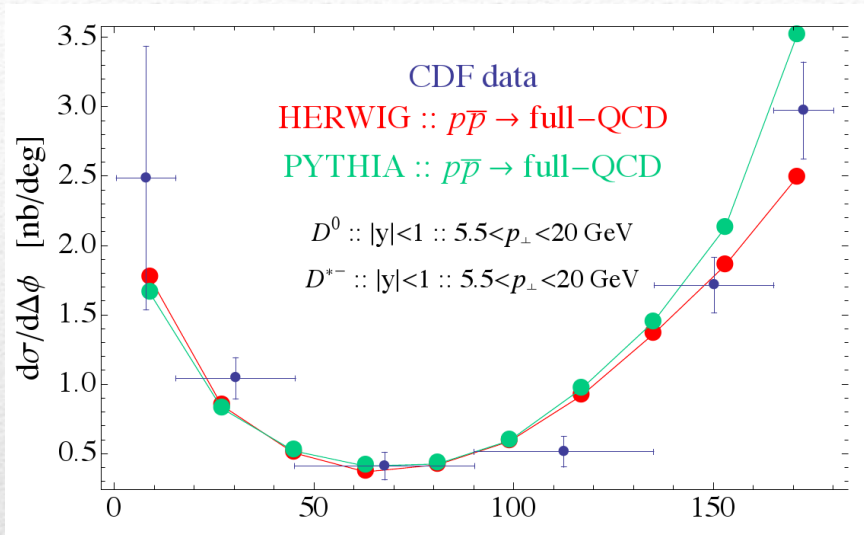
$$\left( \begin{array}{l} \text{binding energy reported in Kamal Seth's talk is } E_B \approx -0.013 \pm 0.192 \text{ MeV:} \\ \sqrt{\langle k^2 \rangle} \approx 30 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 30 \text{ fm} \end{array} \right)$$

to compare with deuteron:  $E_B = -2.2$  MeV

$$\sqrt{\langle k^2 \rangle} \approx 80 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 4 \text{ fm}$$

We assume  $k_{max} \sim \sqrt{\langle k^2 \rangle} \approx 50 \text{ MeV}$ , some other choices are commented later

# 2009 results



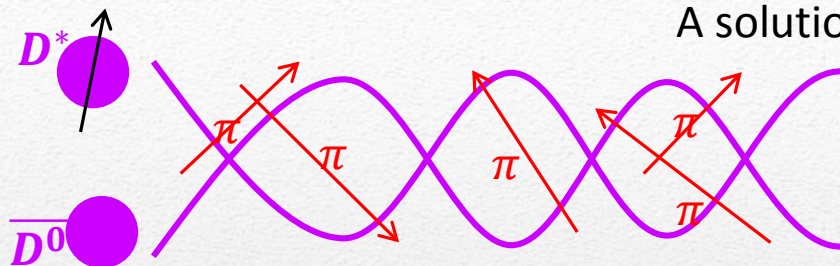
We tune our MC to reproduce CDF distribution of  $\frac{d\sigma}{d\Delta\phi} (p\bar{p} \rightarrow D^0 D^{*-})$

We get  $\sigma(p\bar{p} \rightarrow DD^* | k < k_{\text{max}}) \approx 0.1 \text{ nb}$  @  $\sqrt{s} = 1.96 \text{ TeV}$

Experimentally  $\sigma(p\bar{p} \rightarrow X(3872)) \approx 30 - 70 \text{ nb}!!!$



# Estimating $k_{max}$



A solution can be FSI (rescattering of  $DD^*$ ), which allow  $k_{max}$  to be as large as  $5m_\pi \sim 700$  MeV

$$\sigma(p\bar{p} \rightarrow DD^* | k < k_{max}) \approx 230 \text{ nb}$$

Artoisenet and Braaten, PRD81, 114018

However, the applicability of Watson theorem is challenged by the presence of pions that interfere with  $DD^*$  propagation

Bignamini, Grinstein, Piccinini, Polosa, Riquer, Sabelli, PLB684, 228-230

FSI saturate unitarity bound? Influence of pions small?

Artoisenet and Braaten, PRD83, 014019

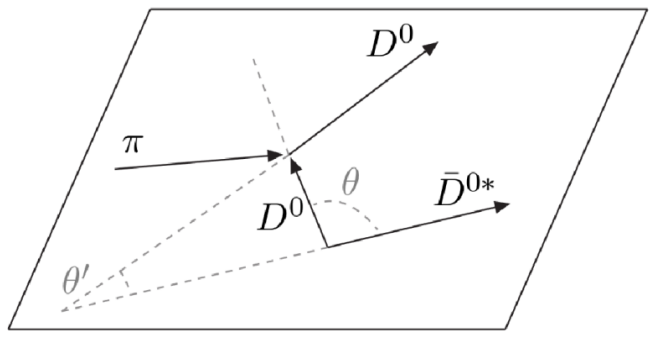
Guo, Meissner, Wang, Yang, JHEP 1405, 138; EPJC74 9, 3063; CTP 61 354  
use  $E_{max} = M_X + \Gamma_X$  for above-threshold unstable states

With different choices, 2 orders of magnitude uncertainty,  
limits on predictive power

# A new mechanism?

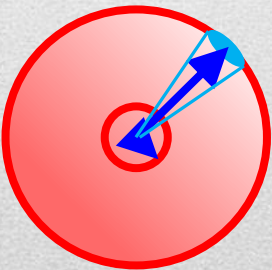
In a more **billiard-like** point of view, the comoving pions can **elastically interact** with  $D(D^*)$ , and **slow down** the pairs  $DD^*$

Esposito, Piccinini, AP, Polosa, JMP 4, 1569  
Guerrieri, Piccinini, AP, Polosa, PRD90, 034003



The mechanism also implies:  $D$  mesons actually **“pushed”** **inside** the potential well (the **classical 3-body problem!**)

$X(3872)$  is a **real, negative energy bound state** (stable)  
It also explains a small width  $\Gamma_X \sim \Gamma_{D^*} \sim 100$  keV



By comparing hadronization times of heavy and light mesons, we estimate up to  $\sim 3$  collisions can occur before the heavy pair to fly apart

We get  $\sigma(p\bar{p} \rightarrow X(3872)) \sim 5$  nb, **still not sufficient** to explain all the experimental cross section

