Modeling XYZ states at JPAC

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Outline

- Joint Physics Analysis Center
- The exotic landscape: XYZ
- Compact tetraquarks
- Other models
- Production of exotics at LHC
- Hybridized Tetraquarks
- Conclusions

Joint Physics Analysis Center

- JPAC was funded to support the extraction of physics results from analysis of experimental data from JLab12 and other accelerator laboratories
- This is achieved through work on theoretical, phenomenological and data analysis tools
- JPAC aims to facilitate close collaboration between theorists, phenomenologists, and experimentalists worldwide
- It is engaged in education of further generation of hadron physics practitioners

Joint Physics Analysis Center



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Production

- > 40 Research Papers (Phys.Rev., Phys.Lett, Eur.J. Phys.)
- ~120 Invited Talks and Seminars
- O(10) ongoing analyses
- Summer School on Reaction Theory (IU, 2015)
- Workshop "Future Directions in Hadron Spectroscopy" (JLab, 2014)

$P_{c}(4450)$	A. Blin <i>et al.,</i>	PRD94, 034002
Λ(1405)	C. Fernandez-Ramirez et al.,	PRD93, 074015
$K N \rightarrow K N$	C. Fernandez-Ramirez et al.,	PRD93, 034029
$\pi N \rightarrow \pi N$	V. Mathieu <i>et al.,</i>	PRD92, 074004
$\gamma p \rightarrow \pi^0 p$	V. Mathieu <i>et al.,</i>	PRD92, 074013
$\eta \to \pi^+ \pi^- \pi^0$	P. Guo <i>et al.,</i>	PRD92, 054016; arXiv:1608.01447
$\omega,\phi ightarrow \pi^+ \pi^- \pi^0$	I. Danilkin <i>et al.,</i>	PRD91, 094029
$\gamma p \rightarrow K^+ K^- p$	M. Shi <i>et al.,</i>	PRD91, 034007
Data	Amplitude analysis (JPAC)	Spectrum and properties

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INDIANA UNIVERSITY



THE GEORGE WASHINGTON UNIVERSITY WASHINGTON, DC

Interactive tools

- Completed projects are fully documented on interactive portals
- These include description on physics, conventions, formalism, etc.
- The web pages contain source codes with detailed explanation how to use them. Users can run codes online, change parameters, display results.

http://www.indiana.edu/~jpac/

Joint Physics Analysis Center						
	HOME	PROJECTS	PUBLICATIONS	LINKS		
		This project is	National S Foundation	Science Sn		
		πN	$ ightarrow \pi N$			

Formalism

The pion-nucleon scattering is a function of 2 variables. The first is the beam momentum in the laboratory frame $p_{\rm lab}$ (in GeV) or the total energy squared $s=W^2$ (in ${\rm GeV^2}$). The second is the cosine of

Resources

- Publications: [Mat15a] and [Wor12a]
- SAID partial waves: compressed zip file
- C/C++: C/C++ file
- Input file: param.txt
 Output files: output0.txt , output1.txt , SigTot.txt , Observables0.txt , Observables1.txt
- Contact person: Vincent Mathieu
- Last update: June 2016

The SAID partial waves are in the format provided online on the SAID webpage :

```
p_{
m lab} \quad \delta \quad \epsilon(\delta) \quad 1 - \eta^2 \quad \epsilon(1 - \eta^2) \quad {
m Re \, PW} \quad {
m Im \, PW} \quad SGT \quad SGR
```

 δ and η are the phase-shift and the inelasticity. $\epsilon(x)$ is the error on x. SGT is the total cross section and SGR is the total reaction cross section.

Format of the input and output files: [show/hide] Description of the C/C++ code: [show/hide]

Simulation

Range of th	e running variab	le:			
s in GeV^2	(min max step)	1,2 ‡	6 ‡	0,01	÷
$p_{ m lab}$ in GeV	(min max step)	0,1 ‡	4 ‡	0,01	\$
u in GeV	(min max step)	0,3 ‡	4 ‡	0,01	÷
$t~{ m in~GeV^2}$	(min max step)	-1 ‡	0 ‡	0,01	\$

The fixed variable:

in Ge	V^2	0
_{lab} in	GeV	5
Start	rese	t

Results



Dictionary – Quark model

- L = orbital angular momentum S = spin $q + \overline{q}$
- J = total angular momentum = exp. measured spin

I = isospin = 0 for quarkonia

 $L - S \le J \le L + S$ $P = (-1)^{L+1}, C = (-1)^{L+S}$ $G = (-1)^{L+S+I}$

J^{PC}	L	S	Charmonium $(c\bar{c})$	Bottomonium $(b\bar{b})$
0^{-+}	0 (S wave)	0	$\eta_c(nS)$	$\eta_b(nS)$
1	0 (S-wave)	1	$\psi(nS)$	$\Upsilon(nS)$
1^{+-}		0	$h_c(nP)$	$h_b(nP)$
0^{++}	1 (P wave)	1	$\chi_{c0}(nP)$	$\chi_{b0}(nP)$
1^{++}	1 (F - wave)	1	$\chi_{c1}(nP)$	$\chi_{b1}(nP)$
2^{++}		1	$\chi_{c2}(nP)$	$\chi_{b2}(nP)$

But
$$J/\psi = \psi(1S), \ \psi' = \psi(2S)$$

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(meaningful when $M_Q \rightarrow \infty$) $V(r) = -\frac{C_F \alpha_S}{r} + \sigma r$ (Cornell potential)

Solve NR Schrödinger eq. → spectrum

Effective theories

(HQET, NRQCD, pNRQCD...)

Integrate out heavy DOF

(spectrum), decay & production rates



Factorization (to be proved) of universal LDMEs

Good description of many production channels, some known puzzles (polarizations)

Exotic landscape



X(3872)



- Discovered in $B \to K X \to K J/\psi \pi \pi$
- Very close to DD* threshold
- Too narrow for an abovetreshold charmonium
- Isospin violation too big $\frac{\Gamma(X \to J/\psi \ \omega)}{\Gamma(X \to J/\psi \ \rho)} \sim 0.8 \pm 0.3$
- Mass prediction not compatible with $\chi_{c1}(2P)$

$$\begin{split} M &= 3871.68 \pm 0.17 \; \text{MeV} \\ M_X - M_{DD^*} &= -3 \pm 192 \; \text{keV} \\ \Gamma &< 1.2 \; \text{MeV} @ 90\% \end{split}$$

X(3872)



BaBar data in $X \rightarrow J/\psi \omega$ favor $J^{PC} = 2^{-+}$, but LHCb in $X \rightarrow J/\psi \rho$ measures 1^{++} at 8σ

Faccini, AP, Piccinini, Polosa PRD 86, 054012 LHCb, PRL 110, 222001





Large prompt production at hadron colliders $\sigma_B / \sigma_{TOT} = (26.3 \pm 2.3 \pm 1.6)\%$

 $\sigma_{PR} \times B(X \to J/\psi \pi \pi) = (1.06 \pm 0.11 \pm 0.15) \text{ nb}$

CMS, JHEP 1304, 154

X(3872)



${\cal B}$ decay mode	X decay mode	product branchin	g fraction ($\times 10^5$)	B_{fit}	R_{fit}
K^+X	$X \to \pi \pi J\!/\!\psi$	0.86 ± 0.08	$(BABAR, 26 Belle^{25})$	$0.081\substack{+0.019\\-0.031}$	1
		$0.84 \pm 0.15 \pm 0.07$	BABAR ²⁶		
		$0.86 \pm 0.08 \pm 0.05$	Belle ²⁵		
$K^0 X$	$X \to \pi \pi J\!/\!\psi$	0.41 ± 0.11	$(BABAR, 26 Belle^{25})$		
		$0.35 \pm 0.19 \pm 0.04$	BABAR ²⁶		
		$0.43 \pm 0.12 \pm 0.04$	Belle ²⁵		
$(K^+\pi^-)_{NR}X$	$X \to \pi \pi J\!/\!\psi$	$0.81 \pm 0.20^{+0.11}_{-0.14}$	Bellc^{106}		
$K^{*0}X$	$X \to \pi \pi J\!/\!\psi$	< 0.34, 90% C.L.	Belle ¹⁰⁶		
KX	$X ightarrow \omega J/\psi$	$R=0.8\pm0.3$	BABAR ³³	$0.061^{+0.024}_{-0.036}$	$0.77^{+0.28}_{-0.32}$
K^+X		$0.6\pm0.2\pm0.1$	BABAR ³³		
$K^0 X$		$0.6\pm0.3\pm0.1$	BABAR ³³		
KX	$X \to \pi \pi \pi^0 J/\psi$	$R=1.0\pm0.4\pm0.3$	Belle^{32}		
K^+X	$X \to D^{*0} \bar{D}^0$	8.5 ± 2.6	$(BABAR, \frac{38}{38} Belle^{37})$	$0.614^{+0.166}_{-0.074}$	$8.2^{+2.3}_{-2.8}$
		$16.7\pm3.6\pm4.7$	BABAR ³⁸		
		$7.7\pm1.6\pm1.0$	Belle ³⁷		
K^0X	$X \to D^{*0} \bar{D}^0$	$f 12\pm4$	$(BABAR, \frac{38}{38} Belle^{37})$		
		$22\pm10\pm4$	BABAR ³⁸		
		$9.7\pm4.6\pm1.3$	Belle ³⁷		
K^+X	$X \to \gamma J/\psi$	0.202 ± 0.038	$(BABAR, \frac{35}{35} Bellc \frac{34}{35})$	$0.019^{+0.005}_{-0.009}$	$0.24_{-0.06}^{+0.05}$
K^+X		$0.28 \pm 0.08 \pm 0.01$	BABAR ³⁵		
		$0.178^{+0.048}_{-0.044} \pm 0.012$	Bellc ³⁴		
$K^0 X$		$0.26 \pm 0.18 \pm 0.02$	BABAR ³⁵		
		$0.124^{+0.076}_{-0.061} \pm 0.011$	Belle^{34}		
K^+X	$X \to \gamma \psi(2S)$	0.44 ± 0.12	BABAR ³⁵	$0.04^{+0.015}_{-0.020}$	$0.51^{+0.13}_{-0.17}$
K^+X		$0.95 \pm 0.27 \pm 0.06$	BABAR ³⁵		
		$0.083^{+0.198}_{-0.183} \pm 0.044$	Belle^{34}		
		$R' = 2.46 \pm 0.64 \pm 0.29$	LHCb ³⁶		
$K^0 X$		$1.14 \pm 0.55 \pm 0.10$	BABAR ³⁵		
		$0.112^{+0.357}_{-0.290} \pm 0.057$	Belle^{34}		
K^+X	$X \to \gamma \chi_{c1}$	$< 9.6 \times 10^{-3}$	Belle ²³	$< 1.0 \times 10^{-3}$	< 0.014
K^+X	$X \to \gamma \chi_{c2}$	< 0.016	Belle ²³	$< 1.7 \times 10^{-3}$	< 0.024
KX	$X \to \gamma \gamma$	$< 4.5 \times 10^{-3}$	Belle^{111}	$< 4.7 \times 10^{-4}$	$< 6.6 \times 10^{-3}$
KX	$X \to \eta J/\psi$	< 1.05	$BABAR^{112}$	< 0.11	< 1.55
K^+X	$X \to p\bar{p}$	$< 9.6 \times 10^{-4}$	LHCb ¹¹⁰	$< 1.6 \times 10^{-4}$	$< 2.2 \times 10^{-3}$

Vector Y states

Lots of unexpected $J^{PC} = 1^{--}$ states found in ISR analyses (and nowhere else!)



Seen in few final states, mostly $J/\psi \pi \pi$ and $\psi(2S) \pi \pi$

Not seen decaying into open charm pairs, to compare with $\frac{B(\psi(3770) \rightarrow D\overline{D})}{B(\psi(3770) \rightarrow J/\psi\pi\pi)} > 480$



Vector Y states



The lineshape in $h_c \pi \pi$ looks pretty different Different states contributing?



Charged *Z* states: $Z_c(3900), Z'_c(4020)$

Charged quarkonium-like resonances have been found, 4q needed



Two states $J^{PC} = 1^{+-}$ appear slightly above $D^{(*)}D^*$ thresholds

$$e^+e^- \rightarrow Z_c(3900)^+\pi^- \rightarrow J/\psi \ \pi^+\pi^- \text{ and } \rightarrow (DD^*)^+\pi^-$$

 $M = 3888.7 \pm 3.4 \text{ MeV}, \ \Gamma = 35 \pm 7 \text{ MeV}$
 $e^+e^- \rightarrow Z'_c(4020)^+\pi^- \rightarrow h_c \ \pi^+\pi^- \text{ and } \rightarrow \overline{D}^{*0}D^{*+}\pi^-$
 $M = 4023.9 \pm 2.4 \text{ MeV}, \ \Gamma = 10 \pm 6 \text{ MeV}$



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Charged *Z* states: $Z_c(3900), Z'_c(4020)$

Charged quarkonium-like resonances have been found, 4q needed



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$M = 4475 \pm 7^{+15}_{-25} \text{ MeV}$ -0.2 $\Gamma = 172 \pm 13^{+37}_{-34}$ MeV -0.4

If the amplitude is a free complex number, in each bin of $m_{\psi'\pi^-}^2$, the resonant behaviour appears as well

Charged Z states: Z(4430)



Charged *Z* states: $Z_b(106010), Z'_b(10650)$



Pentaquarks



LHCb, PRL 115, 072001 LHCb, PRL 117, 082003

Two states seen in $\Lambda_b \to (J/\psi p) K^-$, evidence in $\Lambda_b \to (J/\psi p) \pi^ M_1 = 4380 \pm 8 \pm 29 \text{ MeV}$ $\Gamma_1 = 205 \pm 18 \pm 86 \text{ MeV}$ $M_2 = 4449.8 \pm 1.7 \pm 2.5 \text{ MeV}$ $\Gamma_2 = 39 \pm 5 \pm 19 \text{ MeV}$

Quantum numbers $J^{P} = \begin{pmatrix} 3^{-}, 5^{+} \\ \frac{5}{2}, \frac{5^{+}}{2} \end{pmatrix} \text{ or } \begin{pmatrix} 3^{+}, 5^{-} \\ \frac{5}{2}, \frac{5^{+}}{2} \end{pmatrix} \text{ or } \begin{pmatrix} 5^{+}, 3^{-} \\ \frac{5^{+}, 2^{-}}{2} \end{pmatrix}$ Opposite parities needed for the interference to correctly describe angular distributions

No obvious threshold nearby

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Pentaguark photoproduction

We propose to search the $P_c(4450)$ state in photoproduction

> Q. Wang *et al.* PRD92, 034022 M. Karliner et al. PLB752, 329-332 Kubarovsky et al. PRD92, 031502



We use the (few) existing data and VMD + pomeron inspired bkg to estimate the cross section

 $J^{P} = (3/2)^{-1}$

$\sigma_s \; ({ m MeV})$	0	60	120
A	$0.156\substack{+0.029\\-0.020}$	$0.157\substack{+0.039\\-0.021}$	$0.157\substack{+0.037\\-0.022}$
$lpha_0$	$1.151\substack{+0.018\\-0.020}$	$1.150\substack{+0.018\\-0.026}$	$1.150\substack{+0.015\\-0.023}$
$\alpha' \; ({\rm GeV}^{-2})$	$0.112\substack{+0.033\\-0.054}$	$0.111\substack{+0.037\\-0.064}$	$0.111\substack{+0.038\\-0.054}$
$s_t \; ({\rm GeV}^2)$	$16.8^{+1.7}_{-0.9}$	$16.9^{+2.0}_{-1.6}$	$16.9^{+2.0}_{-1.1}$
$b_0 \; (\text{GeV}^{-2})$	$1.01\substack{+0.47 \\ -0.29}$	$1.02\substack{+0.61\\-0.32}$	$1.03\substack{+0.49\\-0.31}$
$\mathcal{B}_{\psi p}$ (95% CL)	$\leq 29~\%$	$\leq 30~\%$	$\leq 23~\%$





A. Blin et al. (JPAC), PRD94, 034002

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State	M (MeV)	Γ (MeV)	J^{PC}	Process (mode)	Experiment $(\#\sigma)$	State	M (MeV)	Γ (MeV)	J^{PC}	Process (mode)	Experiment $(\#\sigma)$
X(3823)	3823.1 ± 1.9	< 24	??-	$B \to K(\chi_{c1}\gamma)$	$Belle^{23}(4.0)$	Y(4220)	4196^{+35}_{-30}	39 ± 32	1	$e^+e^- \rightarrow (\pi^+\pi^-h_c)$	BES III data ^{63,64} (4.5)
X(3872)	3871.68 ± 0.17	< 1.2	1^{++}	$B \to K(\pi^+\pi^-J\!/\!\psi)$	$Belle^{24,25}$ (>10), $BABAR^{26}$ (8.6)	Y(4230)	4230 ± 8	38 ± 12	1	$e^+e^- \to (\chi_{c0}\omega)$	BES III <mark>65</mark> (>9)
				$p\bar{p} \rightarrow (\pi^+\pi^- J/\psi) \dots$	$CDF^{27,28}(11.6), D0^{29}(5.2)$	$Z(4250)^+$	4248^{+185}_{-45}	177^{+321}_{-72}	$?^{+}$	$\bar{B}^0 \to K^-(\pi^+\chi_{c1})$	Belle ⁵⁴ (5.0), BABAR ⁵⁵ (2.0)
				$pp \rightarrow (\pi^+\pi^- J/\psi) \dots$	LHCb ^{30,31} (np)	Y(4260)	4250 ± 9	108 ± 12	1	$e^+e^- \rightarrow (\pi\pi J/\psi)$	$BABAR^{66,67}(8), CLEO^{68,69}(11)$
				$B \to K (\pi^+ \pi^- \pi^0 J / \psi)$	Belle ³² (4.3), $BABAR^{33}$ (4.0)	()					Belle ^{41,53} (15), BES III ⁴⁰ (np)
				$B \to K(\gamma J\!/\!\psi)$	$Belle^{34}(5.5), BABAR^{35}(3.5)$					$e^+e^- \rightarrow (f_0(980)J/\psi)$	$BABAR^{67}$ (np), $Belle^{41}$ (np)
					LHCb ³⁶ (> 10)					$e^+e^- \to (\pi^- Z_c(3900)^+)$	BES III ⁴⁰ (8), Belle ⁴¹ (5.2)
				$B \to K(\gamma\psi(2S))$	$BABAR^{35}(3.6), Belle^{34}(0.2)$					$e^+e^- \rightarrow (\gamma X(3872))$	BES $II^{70}(5.3)$
					$LHCb^{36}(4.4)$	Y(4290)	4293 ± 9	222 ± 67	1	$e^+e^- \rightarrow (\pi^+\pi^-h_c)$	BES III data $63,64$ (np)
				$B \to K(D\bar{D}^*)$	Belle ³⁷ (6.4), BABAR ³⁸ (4.9)	X(4350)	$4350.6^{+4.6}$	13^{+18}	$\frac{1}{0/2^{2+}}$	$e^+e^- \rightarrow e^+e^-(\phi Ibb)$	$\frac{Bell}{58}(3.2)$
$Z_c(3900)^+$	3888.7 ± 3.4	35 ± 7	1^{+-}	$Y(4260) \to \pi^- (D\bar{D}^*)^+$	BES III ³⁹ (np)	V(4360)	4350.0 - 5.1 4354 ± 11	10 - 10 78 + 16	1	$e^+e^- \rightarrow (\pi^+\pi^-\psi(2S))$	Bell (71) (8) BABAR (72) (np)
				$Y(4260) \to \pi^-(\pi^+ J/\psi)$	BES III ⁴⁰ (8), Belle ⁴¹ (5.2)	7(4300)+	4334 ± 11	10 ± 10 100 ± 21	1 1+-	$\bar{\mathcal{D}}^{0} \rightarrow K^{-}(\pi^{+}\pi^{0}\psi(2S))$	$D_{\text{oll}}(73,74)$ (6.4) $D_{\text{A}}D_{\text{A}}D_{\text{A}}T_{\text{C}}^{75}$ (2.4)
					CLEO data $\frac{42}{(>5)}$	$Z(4430)^{+}$	4470 ± 17	100 ± 31	1,	$D \rightarrow K (\pi^+ \psi(2S))$	$Dene_{-1} (0.4), DADAt (2.4)$
$Z_c(4020)^+$	4023.9 ± 2.4	10 ± 6	1^{+-}	$Y(4260) \to \pi^-(\pi^+ h_c)$	BES III $\frac{43}{(8.9)}$					\overline{p} , $W = (+U/L)$	$LHOD^{-1}(13.9)$
				$Y(4260) \to \pi^- (D^* \bar{D}^*)^+$	BES III ⁴⁴ (10)	TT((coc))	+02.1+0	aa+41		$B^{\circ} \rightarrow K^{\circ}(\pi^+ J/\psi)$	$\operatorname{Bell}_{\overline{22}}(4.0)$
Y(3915)	3918.4 ± 1.9	20 ± 5	0^{++}	$B \to K(\omega J/\psi)$	Belle ⁴⁵ (8), <i>BABA</i> (19)	Y(4630)	4634_{-11}^{+5}	92^{+41}_{-32}	1	$e^+e^- \to (\Lambda_c^+\Lambda_c^-)$	$\operatorname{Bell}_{\bullet}^{\bullet}(8.2)$
				$e^+e^- \rightarrow e^+e^-(\omega J/\psi)$	Belle ⁴⁷ (7.7), BABAR ⁴⁸ (7.6)	Y(4660)	4665 ± 10	53 ± 14	1	$e^+e^- \to (\pi^+\pi^-\psi(2S))$	Belle ⁽¹¹⁾ (5.8), BABAR ⁽²⁾ (5)
Z(3930)	3927.2 ± 2.6	24 ± 6	2^{++}	$e^+e^- \rightarrow e^+e^-(D\bar{D})$	Belle ⁴⁹ (5.3), BABAR ⁵⁰ (5.8)	$Z_b(10610)^+$	10607.2 ± 2.0	18.4 ± 2.4	1^{+-}	$\Upsilon(5S) \to \pi(\pi\Upsilon(nS))$	Belle ^{78,79} (>10)
X(3940)	3942^{+9}_{-8}	37^{+27}_{-17}	;;+	$e^+e^- \rightarrow J/\psi \; (D\bar{D}^*)$	$\operatorname{Bell}_{6}^{51,52}(6)$					$\Upsilon(5S) \to \pi^-(\pi^+ h_b(nP))$	$\text{Belle}^{\overline{78}}(16)$
Y(4008)	3891 ± 42	255 ± 42	1	$e^+e^- \rightarrow (\pi^+\pi^- J/\psi)$	$\text{Bell}e^{41,53}(7.4)$					$\Upsilon(5S) \to \pi^- (B\bar{B}^*)^+$	$\operatorname{Belle}^{80}(8)$
$Z(4050)^+$	4051_{-43}^{+24}	82^{+51}_{-55}	??+	$\bar{B}^0 \to K^-(\pi^+\chi_{c1})$	Belle ⁵⁴ (5.0), BABAR ⁵⁵ (1.1)	$Z_b(10650)^+$	10652.2 ± 1.5	11.5 ± 2.2	1^{+-}	$\Upsilon(5S) \to \pi^-(\pi^+\Upsilon(nS))$	Belle ⁷⁸ (>10)
Y(4140)	4145.6 ± 3.6	14.3 ± 5.9	$\dot{5}_{i+1}$	$B^+ \to K^+(\phi J/\psi)$	$CDF^{56,57}(5.0), Belle^{58}(1.9),$					$\Upsilon(5S) \to \pi^-(\pi^+ h_b(nP))$	$\operatorname{Belle}^{\overline{78}}(16)$
					LHC 159 (1.4), CMS 60 (>5)					$\Upsilon(5S) \to \pi^- (B^* \bar{B}^*)^+$	$\operatorname{Belle}^{\underline{80}}(6.8)$
		1110			$D \varnothing^{61}(3.1)$						
X(4160)	4156^{+29}_{-25}	139^{+113}_{-65}	??+	$e^+e^- \to J/\psi \ (D^*\bar{D}^*)$	$\operatorname{Belle}^{\underline{52}}(5.5)$						
$Z(4200)^+$	4196_{-30}^{+35}	370^{+99}_{-110}	1^{+-}	$\bar{B}^0 \to K^-(\pi^+ J/\psi)$	$Belle^{62}(7.2)$						Delese

Guerrieri, AP, Piccinini, Polosa, IJMPA 30, 1530002

X(3872) on the lattice: spectrum



Prelovsek et al. PRL 111 (2013) 192001 arXiv: 1307.5172

Proposed models

Molecule of hadrons (loosely bound)



 $\mathbf{3}_c \times \overline{\mathbf{3}}_c \in \mathbf{1}_c$ Diquark-antidiquark (tetraquark)

24

Hadrocharmonium (Van der Waals forces)

 $\mathbf{1}_c \times \mathbf{1}_c \in \mathbf{1}_c$



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Diquarks

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Attraction and repulsion in 1-gluon exchange approximation is given by

 $l \quad R = \frac{1}{2} \left(C_2(R_{12}) - C_2(R_1) - C_2(R_2) \right)$ $T_{kl}^a \quad R_1 = -\frac{4}{3}, R_8 = +\frac{1}{6}$ $R_3 = -\frac{2}{3}, R_6 = +\frac{1}{3}$ $\mathbf{3}_{c} \times \mathbf{3}_{c} \in \overline{\mathbf{3}}_{c}$ T_{ii}^{a} T_{ij}^a β=5.8 1.0 0.8 0.6 The singlet $\mathbf{1}_c$ is attractive 0.4 0.2 a=5.1,0) 0.0 A diquark in $\overline{\mathbf{3}}_{c}$ is attractive 10 *scalar *scala $(a=5.1,\theta)/C_{\gamma_{5}}(r/c_{\gamma_{5}})$ Evidence (?) of diquarks in LQCD, Alexandrou, de Forcrand, Lucini, PRL 97, 222002 c_r(r/ 0.0 H-shape with a 4 guark system **B**=6.2 B=6.2 1.0 Cardoso, Cardoso, Bicudo, 0.8 0.6 PRD84, 054508 0.40.2 0.0 ∟ 0.0

0.5

0.0

 $\cos(\theta)$

0.5

0.0 0.2 0.6 0.8 1.0

0.4 r_{ud} (fm)

Tetraquark

In a constituent (di)quark model, we can think of a diquark-antidiquark compact state

 $[cq]_{S=0}[\overline{c}\overline{q}]_{S=1}+h.c.$

Maiani, Piccinini, Polosa, Riquer PRD71 014028 Faccini, Maiani, Piccinini, AP, Polosa, Riquer PRD87 111102 Maiani, Piccinini, Polosa, Riquer PRD89 114010

Spectrum according to color-spin hamiltonian (all the terms of the Breit-Fermi hamiltonian are absorbed into a constant diquark mass):

$$H = \sum_{dq} m_{dq} + 2 \sum_{i < j} \kappa_{ij} \, \overrightarrow{S_i} \cdot \overrightarrow{S_j} \, \frac{\lambda_i^a}{2} \frac{\lambda_j^a}{2}$$

Decay pattern mostly driven by HQSS ✓ Fair understanding of existing spectrum ✓ A full nonet for each level is expected ×



New ansatz: the diquarks are compact objects spacially separated from each other,

only $\kappa_{cq} \neq 0$ Existing spectrum is fitted if $\kappa_{cq} = 67$ MeV

Tetraquark: new ansatz

Maiani, Piccinini, Polosa, Riquer PRD89 114010

Contraction of the second								
J^{PC}	$cq \ \bar{c}\bar{q}$		$car{c} qar{q}$	Resonance Assig.	Decays		-	
0++	0,0 angle		$1/2 0,0 angle + \sqrt{3}/2 1,1 angle$	$\lambda_0 = X_0 (\sim 3770 \text{ MeV})$	$\eta_c, J/\psi + 1$	ight mesons	_	$_{2}$
0++	$ 1,1 angle_0$		$\sqrt{3}/2 0,0 angle - 1/2 1,1 angle$	$X_0' (\sim 4000 \text{ MeV})$	$\eta_c, J/\psi + 1$	ight mesons	B_{α}	$_{c}L^{2}$
1++	$1/\sqrt{2}(1,0)$	$\rangle + 0,1\rangle)$	$ 1,1 angle_1$	$X_1 = X(3872)$	$J/\psi + \rho/\omega,$	DD^*	$\Delta H = -$	$\overline{2}$
1+-	$1/\sqrt{2}(1,0)$	$\rangle - 0,1\rangle)$	$1/\sqrt{2}(1,0 angle- 0,1 angle)$	Z = Z(3900)	$J/\psi + \pi, h_{c}$	$_{c}/\eta_{c}+\pi/ ho$		
1+-	$ 1,1\rangle_1$		$1/\sqrt{2}(1,0 angle+ 0,1 angle)$	Z' = Z(4020)	$J/\psi + \pi, h_{c}$	$_{c}/\eta_{c}+\pi/ ho$		$2aL \cdot S$
2++	$ 1,1\rangle_2$		$ 1,1\rangle_2$	$X_2 (\sim 4000 \text{ MeV})$	J/ψ + light	mesons		
				<u> </u>			=	
	L	= 1 P($S_{c\bar{c}} = 1) : P(S_{c\bar{c}} = 0)$)) Assignment	Radiat	ive Decay	_	
$/10 \pi\pi$	_	Y_1	3:1	Y(4008)	γ .	$+X_0$		
γφ ππ		Y_2	1:0	Y(4260)	γ	+X	actually ob	oserved
$h_c \pi \pi$		Y_3	1:3	Y(4290)/Y(4220)	$)) \gamma$	$+X'_{0}$	BESIII P	RL 112,
$\Lambda_c^+ \Lambda_c^-$		Y_4	1:0	Y(4630)	γ .	$+X_2$		092001
ũ ũ					30	⁵⁰⁰ μ(2S		
Ra	dial exci	tations				<u>Ψ(20</u>		
7()		(11013)			36	500-		
Ζ(,	23) = 2	(4430)	$M_{Z(4430)}$	$-M_{Z_c} = 586^{+17}_{-26}$	MeV	100-	589 MoV	
$Y_1($	2P) = Y	(4360)	to compa	are with charmor	ium	FUU		
$Y_2($	2P) = Y	(4660)			32	200		
Decav i	$n \frac{1}{10}(2S)$) nrefer;	ably			<u>J/ψ</u>	V	
Leccuy					30	00-		
. Pilloni -	 Modelin 	ng XYZ st	ates at JPAC		28	300		27



$$J^{PC} = 0^{++} \quad X_0 = |0,0\rangle_0, \ X'_0 = |1,1\rangle_0$$

$$J^{PC} = 2^{++} \quad X_2 = |1,1\rangle_2$$

$$J^{PC} = 1^{++} \quad X = \frac{1}{\sqrt{2}} (|1,0\rangle_1 + |0,1\rangle_1)$$

$$J^{PC} = 1^{+-} \quad Z = \frac{1}{\sqrt{2}} (|1,0\rangle_1 - |0,1\rangle_1)$$

$$Z' = |1,1\rangle_1$$

Tetraquark: the *ccss* states $\frac{0^{++'}}{\kappa}$ + κ $\frac{1^{+-1}}{1} + \kappa$ $\frac{2^{++}}{X(4274)} + \kappa$ X(4274) $\frac{1^{++}}{X(4140)} - \kappa \qquad \frac{1^{+-}}{-\kappa} - \kappa$ $+ 2 m_{[cs]} = M$ $\frac{0^{++}}{2} - 3 \kappa$

> Good description of the spectrum but one has to assume the axial assignment for the X(4274) to be incorrect (two unresolved states with 0^{++} and 2^{++})

> > Maiani, Polosa and Riquer, arXiv:1607.02405 Esposito, AP, Polosa, to appear



• Since this is still a $3 \leftrightarrow \overline{3}$ color interaction, just use the Cornell potential:

e.g. Barnes et al., PRD 72, 054026

 $\frac{B(Z^+(4430) \to \psi(2S)\pi^+)}{B(Z^+(4430) \to J/\psi \pi^+)} \sim 72$

(> 10 exp.)

$$V(r) = -\frac{4}{3}\frac{\alpha_s}{r} + br + \frac{32\pi\alpha_s}{9m_{cq}^2} \left(\frac{\sigma}{\sqrt{\pi}}\right)^3 e^{-\sigma^2 r^2} \mathbf{S}_{cq} \cdot \mathbf{S}_{\overline{cq}},$$

- Use that the kinetic energy released in $\overline{B}^0 \to K^- Z^+(4430)$ converts into potential energy until the diquarks come to rest
- Hadronization most effective at this point (WKB turning point)

$$r_Z = 1.16 \text{ fm}, \langle r_{\psi(2S)} \rangle = 0.80 \text{ fm}, \langle r_{J/\psi} \rangle = 0.39 \text{ fm}$$

Hadro-charmonium



Dubynskiy, Voloshin, PLB 666, 344 Dubynskiy, Voloshin, PLB 671, 82 Li, Voloshin, MPLA29, 1450060

Born in the context of QCD multipole expansion

$$\begin{split} H_{eff} &= -\frac{1}{2} a_{\psi} E^a_i E^a_i \\ a_{\psi} &= \left\langle \psi | (t^a_c - t^a_{\bar{c}}) r_i \; G \; r_i (t^a_c - t^a_{\bar{c}}) | \psi \right\rangle \end{split}$$

the chromoelectric field interacts with soft light matter (highly excited light hadrons)

A bound state can occur via Van der Waals-like interactions

Expected to decay into core charmonium + light hadrons, Decay into open charm exponentially suppressed

Triangle singularity (kinematics)



Logarithmic branch points due to exchanges in the cross channels can simulate a resonant behavior, only in very special kinematical conditions (Coleman and Norton, Nuovo Cim. 38, 438), However, this effects cancels in Dalitz projections, no peaks (Schmid, Phys.Rev. 154, 1363)

$$f_{0,i}(s) = b_{0,i}(s) + \frac{t_{ij}}{\pi} \int_{s_i}^{\infty} ds' \frac{\rho_j(s')b_{0,j}(s')}{s'-s}$$

...but the cancellation can be spread in different channels, you might still see peaks in other channels only! Szczepaniak, PLB747, 410-416 Szczepaniak, PLB757, 61-64 Guo, Meissner, Wang, Yang PRD92, 071502

A. Pilloni – Modeling XYZ states at JPAC



Tornqvist, Z.Phys. C61, 525 Braaten and Kusunoki, PRD69 074005 Swanson, Phys.Rept. 429 243-305

$$\begin{split} X(3872) &\sim \overline{D}{}^0 D^{*0} \\ Z_c(3900) &\sim \overline{D}{}^0 D^{*+} \\ Z_c'(4020) &\sim \overline{D}{}^{*0} D^{*+} \\ Y(4260) &\sim \overline{D} D_1 \end{split}$$

A deuteron-like meson pair, the interaction is mediated by the exchange of light mesons

- Some model-independent relations (Weinberg's theorem)
- Good description of decay patterns (mostly to constituents) and X(3872) isospin violation ✓
- States appear close to thresholds ✓ (but Z(4430) ×)
- Lifetime of costituents has to be $\gg 1/m_{\pi}$, (but why $\Gamma_{Y} \gg \Gamma_{D_{1}}$?)
- Binding energy varies from −70 to −0.1 MeV, or even positive (repulsive interaction) ×
- Unclear spectrum (a state for each threshold?) depends on potential models ×

$$V_{\pi}(r) = \frac{g_{\pi N}^2}{3} (\overrightarrow{\tau_1} \cdot \overrightarrow{\tau_2}) \left\{ [3(\overrightarrow{\sigma_1} \cdot \hat{r})(\overrightarrow{\sigma_2} \cdot \hat{r}) - (\overrightarrow{\sigma_1} \cdot \overrightarrow{\sigma_2})] \left(1 + \frac{3}{(m_{\pi}r)^2} + \frac{3}{m_{\pi}r} \right) + (\overrightarrow{\sigma_1} \cdot \overrightarrow{\sigma_2}) \right\} \frac{e^{-m_{\pi}r}}{r}$$

Needs regularization, cutoff dependence

Weinberg theorem

Resonant scattering amplitude

$$f(ab \to c \to ab) = -\frac{1}{8\pi E_{CM}}g^2 \frac{1}{(p_a + p_b)^2 - m_c^2}$$

with $m_c = m_a + m_b - B$, and $B, T \ll m_{a,b}$

$$f(ab \to c \to ab) = -\frac{1}{16\pi (m_a + m_b)^2} g^2 \frac{1}{B+T}$$

This has to be compared with the potential scattering for slow particles $(kR \ll 1, \text{ being } R \sim 1/m_{\pi}$ the range of interaction) in an attractive potential U with a superficial level at -B

$$f(ab \to ab) = -\frac{1}{\sqrt{2\mu}} \frac{\sqrt{B} - i\sqrt{T}}{B+T}, B = \frac{g^4}{512\pi^2} \frac{\mu^5}{(m_a m_b)^2}$$

This has to be fulfilled by EVERY molecular state, but:

- $X(3872), B = 0, g \neq 0$
- *Zs*, *B* < 0, repulsive interaction!
- $Y(4260), kR \sim 1.4$



Weinberg, PR 130, 776 Weinberg, PR 137, B672 Polosa, PLB 746, 248

S-Matrix principles



 $A(s,t) = \sum_{l} A_{l}(s)P_{l}(z_{s})$ **Analyticity** $A_{l}(s) = \lim_{\epsilon \to 0} A_{l}(s+i\epsilon)$

These are constraints the amplitudes have to satisfy, but do not fix the dynamics

Resonances (QCD states) are poles in the unphysical Riemann sheets

Pole hunting



Case study, $Z_c(3900)$

One can test different parametrizations of the amplitude, which correspond to different singularities \rightarrow different natures



Case 1: Breit-Wigner-like singularity, $\chi^2/DOF = 641/533$

AP and A. Szczepaniak (JPAC), in progress



A. Pilloni – Modeling XYZ states at JPAC

Case study, $Z_c(3900)$



Prompt production of *X*(3872)

X(3872) is the Queen of exotic resonances, the most popular interpretation is a $D^0 \overline{D}^{0*}$ molecule (bound state, pole in the 1st Riemann sheet?) but it is copiously promptly produced at hadron colliders





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Towards hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

The absence of many of the predicted states might point to the need for selection rules It is unlikely that the many close-by thresholds play no role whatsoever All the well assessed 4-quark resonances lie close and above some meson-meson thresholds:

	Thr.	δ (MeV)	$A \sqrt{\delta}$ (MeV)	Γ (MeV)
X(3872)	$ar{D}^0 D^{*0}$	0^{\dagger}	0^{\dagger}	0^{\dagger}
$Z_c(3900)$	$ar{D}^0 D^{*+}$	7.8	27.9	27.9
$Z_{c}^{\prime}(4020)$	$ar{D}^{*0}D^{*+}$	6.7	25.9	24.8 [¶]
$\mathbf{V}(\mathbf{A}1\mathbf{A}0)$	Ibk A	<i>a</i>) 31.6	52.7	28.0
A(4140)	J /Ψ Φ	<i>b</i>) 30.1	54.7	83.0
$Z_b(10610)$	$ar{B}^0B^{*+}$	2.7	16.6	18.4
$Z_b'(10650)$	$ar{B}^{*0}B^{*+}$	1.8	13.4	11.5
<i>X</i> (5568)	$\overline{B^0_{s}\pi^+}$	61.4	78.4	21.9
X_{bs}	$B^+ar{K}^0$	5.8	24.1	

We introduce a mechanism that might provide "dynamical selection rules" to explain the presence/absence of resonances from the experimental data.

Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

Feshbach mechanism occurs when two atoms can interact with two potentials, resp. with continuum (meson-meson) and discrete (4q) spectrum \rightarrow hybridization



Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

$$\Gamma = -16\pi^{3} \rho \Im(T) \sim 16\pi^{4} \rho |H_{PQ}|^{2} \delta \left(\frac{p_{1}^{2}}{2M} + \frac{p_{2}^{2}}{2M} - \delta\right)$$

The expected width is the average over momenta that allow for the existence of a tetraquark $p < \bar{p} = 50 \div 100 \text{ MeV}$

 $\Gamma \sim A\sqrt{\delta}$

We therefore expect to see a level if:

- δ > 0 the state lies above threshold
- $\delta < \frac{\bar{p}^2}{2M}$, only the closest threshold contributes
- The states ψ_Q and ψ_P are orthogonal

X(3872) should be a I = 0 state, but $M(1^{++}) < M(D^{+*}D^{-})$ $\delta < 0$, so $a > 0 \rightarrow$ Repulsive interaction No charged component, isospin violation!

Hybridized tetraquarks

Esposito, AP, Polosa, PLB758, 292

The model works only if no direct transition between closed channel levels can occur This prevents the straightforward generalization to L = 1 and radially excited states (like the *Ys* or the *Z*(4430))

In this picture, a $[bu][\bar{s}\bar{d}]$ state with resonance parameters of the X(5568)observed by D0 is not likely

Also, one has to ensure the orthogonality between the two Hilbert subspaces P and Q. This might affect the estimate for the X(4140)

All the resonances can be fitted with $A = (10.3 \pm 1.3) \text{ MeV}^{1/2}$ $\chi^2/\text{DOF} = 1.2/5$



Conclusions & prospects

- The discovery of exotic states has challenged the well established Charmonium framework
- Some fantasy needed, many phenomenological models introduced.
- Experiments are very prolific! Constant feedback on predictions
- Nuclei observation at hadron colliders can give an unexpected help in testing some phenomenological hypotheses for the XYZ states
- Search for exotic states in prompt production is a necessary step to improve our understanding of the sector
- Feshbach mechanism might be effective in reducing the number of states predicted by the tetraquark picture
- Thorough amplitude anlyses might shed some light on the microscopic nature of the new states

Thank you

BACKUP



Other beasts



One/two peaks seen in $B \rightarrow XK \rightarrow J/\psi \phi K$, close to threshold

X(3915), seen in $B \rightarrow X K \rightarrow J/\psi \omega$ and $\gamma \gamma \rightarrow X \rightarrow J/\psi \omega$ $J^{PC} = 0^{++}$, candidate for $\chi_{c0}(2P)$ But X(3915) $\not\rightarrow D\overline{D}$ as expected, and the hyperfine splitting M(2^{++}) - M(0^{++}) too small



$Y(4260) \rightarrow \overline{D}D_1?$ e⁺e⁻ \rightarrow Y(4260) $\rightarrow \pi^- \overline{D}^0 D^{*+}$



$Z_c(3900) \to \eta_c \rho$

Esposito, Guerrieri, AP, PLB 746, 194-201

If tetraquark

Kinematics with HQSS, dynamics estimated according to Brodsky et al., PRL113, 112001



	Kinematics	Sonry	Dynamics in	lenudeu
	type I	type II	type I	type II
$\frac{\mathcal{BR}(Z_c \to \eta_c \rho)}{\mathcal{BR}(Z_c \to J/\psi \pi)}$	$(3.3^{+7.9}_{-1.4}) \times 10^2$	$0.41^{+0.96}_{-0.17}$	$(2.3^{+3.3}_{-1.4}) \times 10^2$	$0.27^{+0.40}_{-0.17}$
$\frac{\mathcal{BR}(Z_c' \to \eta_c \rho)}{\mathcal{BR}(Z_c' \to h_c \pi)}$	$(1.2^{+2.8}_{-0.5}) \times 10^2$		6.6 ^{+56.}	8

 $Z_c(3900) \rightarrow \eta_c \rho$

Esposito, Guerrieri, AP, PLB 746, 194-201

If molecule

Non-Relativistic Effective Theory, HQET+NRQCD and Hidden gauge Lagrangian Uncertainty estimated with power counting at NLO



$$\begin{split} \mathcal{L}_{Z_{c}^{(\prime)}} &= \frac{z^{(\prime)}}{2} \left\langle \mathcal{Z}_{\mu,ab}^{(\prime)} \bar{H}_{2b} \gamma^{\mu} \bar{H}_{1a} \right\rangle + h.c., \\ \mathcal{L}_{c\bar{c}} &= \frac{g_{2}}{2} \left\langle \bar{\Psi} H_{1a} \overleftrightarrow{\partial} H_{2a} \right\rangle + \frac{g_{1}}{2} \left\langle \bar{\chi}_{\mu} H_{1a} \gamma^{\mu} H_{2a} \right\rangle + h.c., \\ \mathcal{L}_{\rho DD^{*}} &= i\beta \left\langle H_{1b} v^{\mu} \left(\mathcal{V}_{\mu} - \rho_{\mu} \right)_{ba} \bar{H}_{1a} \right\rangle + i\lambda \left\langle H_{1b} \sigma^{\mu\nu} F_{\mu\nu}(\rho)_{ba} \bar{H}_{1a} \right\rangle + h.c., \end{split}$$



A. Pilloni – Modeling XYZ states at JPAC

Tetraquark: the *Y*(4220)



$$\begin{split} \langle \chi_{c0}(p) \,\omega(\eta,q) | Y(\lambda,P) \rangle &= g_{\chi} \,\eta \cdot \lambda, \\ \langle Z_{c}'(\eta,q) \,\pi(p) | Y(\lambda,P) \rangle &= g_{Z} \,\eta \cdot \lambda \frac{P \cdot p}{f_{\pi} M_{Y}}, \\ \langle h_{c}(\eta,q) \,\sigma(p) | Y(\lambda,P) \rangle &= g_{h} \,\varepsilon_{\mu\nu\rho\sigma} \eta^{\mu} \lambda^{\nu} \frac{P^{\rho} q^{\sigma}}{P \cdot q}, \\ \langle \pi(q) \pi(p) | \sigma(P) \rangle &= \frac{P^{2}}{2f_{\pi}}, \end{split}$$

A state apparently breaking HQSS has been observed

Compatible to be the Y_3 state

Faccini, Filaci, Guerrieri, AP, Polosa, PRD 91, 117501

A. Pilloni – Exotic Hadron Spectroscopy



Tetraquark: the *b* sector

Ali, Maiani, Piccinini, Polosa, Riquer PRD91 017502

$$M(Z'_b) - M(Z_b) = 2\kappa_b$$

$$M(Z'_c) - M(Z_c) = 2\kappa_c \sim 120 \text{ MeV}$$

$$\kappa_b : \kappa_c = M_c : M_b \sim 0.30$$

 $2\kappa_b \sim 36$ MeV, vs. 45 MeV (exp.)

$$Z_{b} = \frac{\alpha \left| 1_{q\bar{q}} 0_{b\bar{b}} \right\rangle - \beta \left| 0_{q\bar{q}} 1_{b\bar{b}} \right\rangle}{\sqrt{2}}$$
$$Z_{b}' = \frac{\alpha \left| 1_{q\bar{q}} 0_{b\bar{b}} \right\rangle + \beta \left| 0_{q\bar{q}} 1_{b\bar{b}} \right\rangle}{\sqrt{2}}$$

Data on $\Upsilon(5S) \rightarrow \Upsilon(nS)\pi\pi$ and $\Upsilon(5S) \rightarrow h_b(nP)\pi\pi$ strongly favor $\alpha = \beta$



 $Y(4260) \rightarrow \gamma X(3872)$

M. Ablikim et al., Phys. Rev. Lett. 112 (2014) 092001

F. Piccinini

BESIII: $e^+e^- \rightarrow Y(4260) \rightarrow X(3872)\gamma$



F. Piccinini (INFN)

54

4 / 24

Tuning of MC

Monte Carlo simulations A. Esposito

• We compare the $D^0 D^{*-}$ pairs produced as a function of relative azimuthal angle with the results from CDF:



Such distributions of charm mesons are available at Tevatron No distribution has been published (yet) at LHC

Tuning pions

This picture could spoil existing meson distributions used to tune MC We verify this is not the case up to an overall *K* factor

Guerrieri, Piccinini, AP, Polosa, PRD90, 034003



 $Z_{c}(3900)$



Notes from the Editors: Highlights of the Year

Published December 30, 2013 | Physics 6, 139 (2013) | DOI: 10.1103/Physics.6.139

Physics looks back at the standout stories of 2013.

As 2013 draws to a close, we look back on the research covered in *Physics* that really made waves in and beyond the physics community. In thinking about which stories to highlight, we considered a combination of factors: popularity on the website, a clear element of surprise or discovery, or signs that the work could lead to better technology. On behalf of the *Physics* staff, we wish everyone an excellent New Year.

- Matteo Rini and Jessica Thomas



Images from popular Physics stories in 2013.

Four-Quark Matter

Quarks come in twos and threes—or so nearly every experiment has told us. This summer, the BESIII Collaboration in China and the Belle Collaboration in Japan reported they had sorted through the debris of high-energy electron-positron collisions and seen a mysterious particle that appeared to contain four quarks. Though other explanations for the nature of the particle, dubbed Z_c (3900), are possible, the "tetraquark" interpretation may be gaining traction: BESIII has since seen a series of other particles that appear to contain four quarks.

Doubly charmed states

For example, we proposed to look for doubly charmed states, which in tetraquark model are $[cc]_{S=1}[\bar{q}\bar{q}]_{S=0,1}$

These states could be observed in B_c decays @LHC and sought on the lattice Esposito, Papinutto, AP, Polosa, Tantalo, PRD88 (2013) 054029



Preliminary results on spectrum for $m_{\pi} = 490$ MeV, $32^3 \times 64$ lattice, a = 0.075 fm

Guerrieri, Papinutto, AP, Polosa, Tantalo, PoS LATTICE2014 106

T states production





Prompt production of *X*(3872)

X(3872) is the Queen of exotic resonances, the most popular interpretation is a $D^0 \overline{D}^{0*}$ molecule (bound state, pole in the 1st Riemann sheet?)

We aim to evaluate prompt production cross section at hadron colliders via Monte-Carlo simulations

Q. What is a molecule in MC? A. «Coalescence» model



This should provide an upper bound for the cross section

Bignamini, Piccinini, Polosa, Sabelli PRL103 (2009) 162001 Kadastic, Raidan, Strumia PLB683 (2010) 248 60

Estimating *k*_{max}

The binding energy is $E_B \approx -0.16 \pm 0.31$ MeV: very small! In a simple square well model this corresponds to:

 $\sqrt{\langle k^2 \rangle} \approx 50 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 10 \text{ fm}$

binding energy reported in Kamal Seth's talk is $E_B \approx -0.013 \pm 0.192$ MeV: $\sqrt{\langle k^2 \rangle} \approx 30$ MeV, $\sqrt{\langle r^2 \rangle} \approx 30$ fm

to compare with deuteron: $E_B = -2.2 \text{ MeV}$

$$\sqrt{\langle k^2 \rangle} \approx 80 \text{ MeV}, \sqrt{\langle r^2 \rangle} \approx 4 \text{ fm}$$

We assume $k_{max} \sim \sqrt{\langle k^2 \rangle} \approx 50$ MeV, some other choices are commented later

2009 results



We tune our MC to reproduce CDF distribution of $\frac{d\sigma}{d\Delta\phi}(p\bar{p} \rightarrow D^0 D^{*-})$ We get $\sigma(p\bar{p} \rightarrow DD^*|k < k_{max}) \approx 0.1$ nb $@\sqrt{s} = 1.96$ TeV Experimentally $\sigma(p\bar{p} \rightarrow X(3872)) \approx 30 - 70$ nb!!!

Bignamini, Piccinini, Polosa, Sabelli PRL103 (2009) 162001

Estimating *k*_{max}

A solution can be FSI (rescattering of DD^*), which allow k_{max} to be as large as $5m_{\pi} \sim 700$ MeV $\sigma(p\bar{p} \rightarrow DD^*|k < k_{max}) \approx 230$ nb Artoisenet and Braaten, PRD81, 114018

However, the applicability of Watson theorem is challenged by the presence of pions that interfere with DD^* propagation Bignamini, Grinstein, Piccinini, Polosa, Riquer, Sabelli, PLB684, 228-230

> FSI saturate unitarity bound? Influence of pions small? Artoisenet and Braaten, PRD83, 014019

Guo, Meissner, Wang, Yang, JHEP 1405, 138; EPJC74 9, 3063; CTP 61 354 use $E_{max} = M_X + \Gamma_X$ for above-threshold unstable states

With different choices, 2 orders of magnitude uncertainty, limits on predictive power

A new mechanism?

In a more billiard-like point of view, the comoving pions can elastically interact with $D(D^*)$, and slow down the pairs DD^*



Esposito, Piccinini, AP, Polosa, JMP 4, 1569 Guerrieri, Piccinini, AP, Polosa, PRD90, 034003

The mechanism also implies: *D* mesons actually "pushed" inside the potential well (the classical 3-body problem!)

X(3872) is a real, negative energy bound state (stable) It also explains a small width $\Gamma_X \sim \Gamma_{D^*} \sim 100 \text{ keV}$



By comparing hadronization times of heavy and light mesons, we estimate up to ~ 3 collisions can occur before the heavy pair to fly apart

We get $\sigma(p\bar{p} \rightarrow X(3872)) \sim 5 \text{ nb}$, still not sufficient to explain all the experimental cross section



Counting rules

Brodsky, Lebed, 1505.00803

- Exotic states can be produced in threshold regions in e⁺e⁻ (BES, Belle), electroproduction (JLab 12), hadronic beam facilities (PANDA at FAIR, AFTER@LHC) and are best characterized by cross section ratios
- Two examples:

1)
$$\frac{\sigma(e^+e^- \to Z_c^+ \pi^-)}{\sigma(e^+e^- \to \mu^+\mu^-)} \propto \frac{1}{s^6} \text{ as } s \to \infty$$

2)
$$\frac{\sigma(e^+e^- \to Z_c^+ (\overline{c}c\overline{d}u) + \pi^- (\overline{u}d))}{\sigma(e^+e^- \to \Lambda_c(cud) + \overline{\Lambda}_c(\overline{c}\,\overline{u}\overline{d}))} \to \text{ const as } s \to \infty$$

 Ratio numerically smaller if Z_c behaves like weakly-bound dimeson molecule instead of diquark-antidiquark bound state due to weaker meson color van der Waals forces

Production & Feshbach?

Going back to $pp(\bar{p})$ collisions, we can imagine hadronization to produce a state

 $|\psi\rangle = \alpha |[qQ][\bar{q}\bar{Q}]\rangle_{c} + \beta |(\bar{q}q)(\bar{Q}Q)\rangle_{o} + \gamma |(\bar{q}Q)(\bar{Q}q)\rangle_{o}$

If $\beta, \gamma \gg \alpha$, an initial tetraquark state is not likely to be produced The open channel mesons fly apart (see MC simulations)

If Feshbach mechanism is at work, an open state can resonate in a closed one

No prompt production without Feshbach resonances!

Note that only the X(3872) has been observed promptly so far...

...and a narrow X(4140) not compatible with the LHCb one \rightarrow needs confirmation

SELECTION RULES ISOSPIN VIOLATION OF THE X(3872)

- An example of selection rule:
- Consider the down quark part of the X(3872) in the diquarkonium picture: $\Psi_{\mathbf{d}} = X_d = [cd]_0 [\bar{c}\bar{d}]_1 + [cd]_1 [\bar{c}\bar{d}]_0 \sim (D^{*-}D^+ - D^{*+}D^-) + i(\psi \times \rho^0 - \psi \times \omega^0)$ $\int_{\mathcal{T}}_{\text{Fierz rearrangement}} V_{\mathbf{d}} = V_d = [cd]_0 [\bar{c}\bar{d}]_1 + [cd]_1 [\bar{c}\bar{d}]_0 \sim (D^{*-}D^+ - D^{*+}D^-) + i(\psi \times \rho^0 - \psi \times \omega^0)$
- The <u>closest threshold from below</u> is $\Psi_m \sim \bar{D}^0 D^{*0} \longrightarrow \Psi_d \perp \Psi_m$
- But if we consider the up quark part of the X(3872): $\Psi_{\mathbf{d}} = X_u = [cu]_0 [\bar{c}\bar{u}]_1 + [cu]_1 [\bar{c}\bar{u}]_0 \sim (\bar{D}^{*0}D^0 - D^{*0}\bar{D}^0) - i(\psi \times \rho^0 + \psi \times \omega^0)$
- But then $\longrightarrow \Psi_{\mathbf{d}} \not\perp \Psi_{m} \qquad \mathcal{X}$
- Only X_d is produced via this mechanism \longrightarrow isospin violation • no hyperfine neutral doublet

SELECTION RULES THE X^{\pm} AND THE X_b

- The procedure can be applied to other cases:
- X⁺ (A) Diquark model predicts M(X[±]) ≃ M(X⁰) (B) Closest orthogonal threshold is D⁺D^{*0}, D⁰D^{*+}
 (C) Detuning is populity 5 or 5 M eV ≤ 0.
 - (C) Detuning is negative $\delta \simeq -5 \text{ MeV} < 0 \longrightarrow$ the state is not formed!
 - X_b (A) Diquark model predicts $M(X_b) \simeq M(Z_b) \simeq (10607 \pm 2)$ MeV (B) The closest orthogonal threshold is $M(B^0B^{*0}) = (10604.4 \pm 0.3)$ MeV (C) This could either be <u>above</u> threshold (very narrow state) or <u>below</u> (no state at all) (D) Experimentally the diquark model overpredicts the mass of the X:

 $M(Z_c) - M(X) \simeq 32 \text{ MeV}$

(E) We favor the below threshold scenario \longrightarrow no X_b should be seen